

# QUANTUM SIMULATION WITH OPTICAL LATTICES

QACTUS workshop Barcelona, 7<sup>th</sup> September 2023

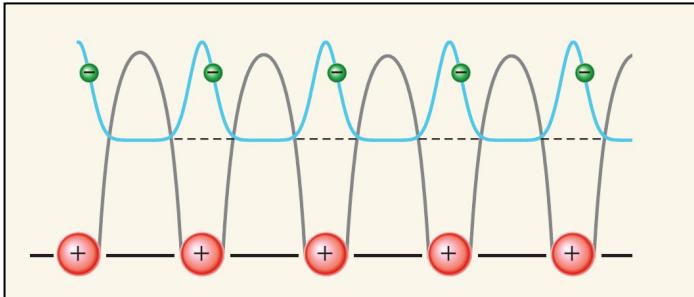


Julian Leonard  
TU Wien/Harvard University

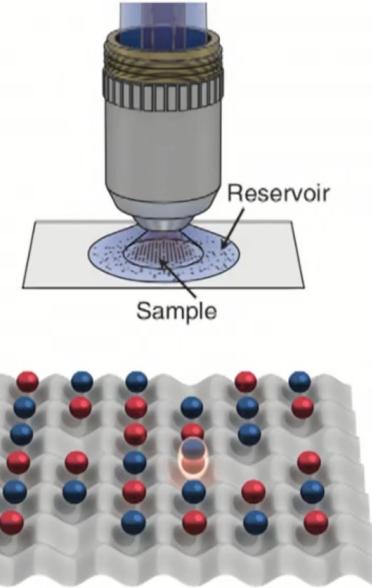
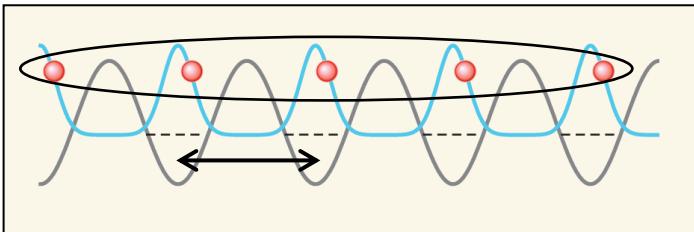


# OPTICAL LATTICES

Electrons in a crystal lattice



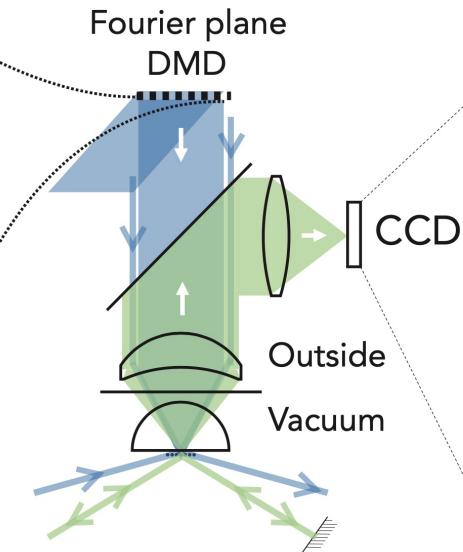
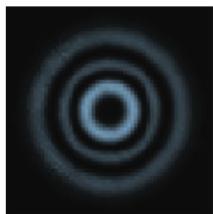
Atoms in an optical lattice



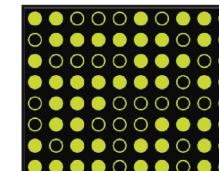
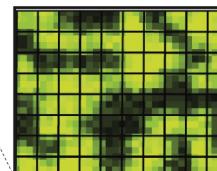
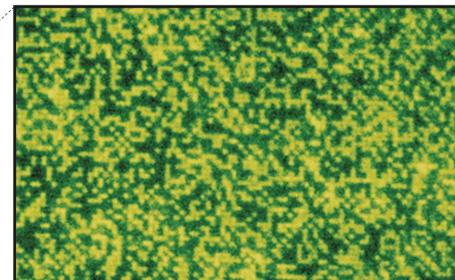
- Excellent coherence
- Scalable
- Site-resolved control
- Single-atom readout

# QUANTUM GAS MICROSCOPE

## Site-resolved control

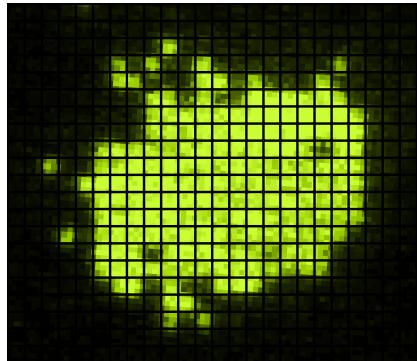


## Single-atom readout

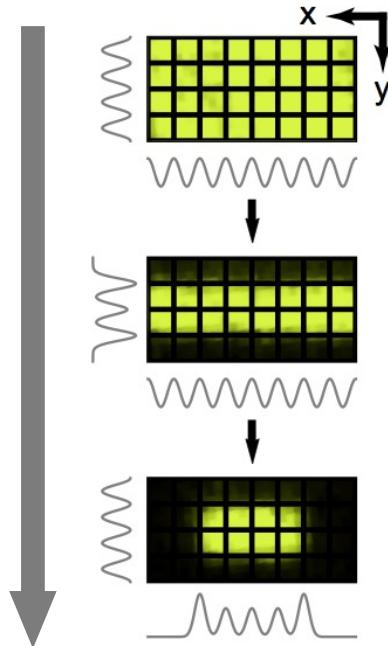


# ARBITRARY POTENTIALS

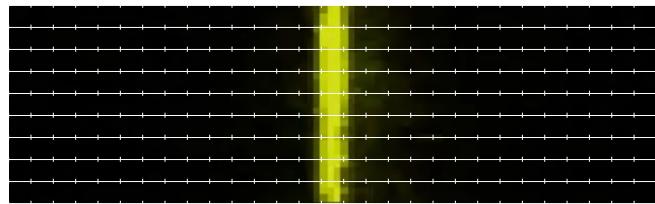
Low-entropy  
Mott insulator



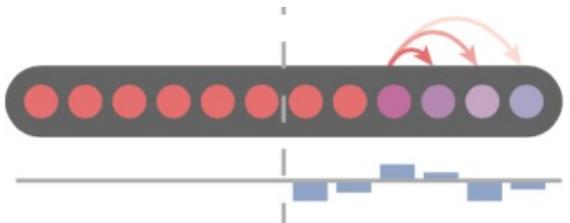
Local potentials



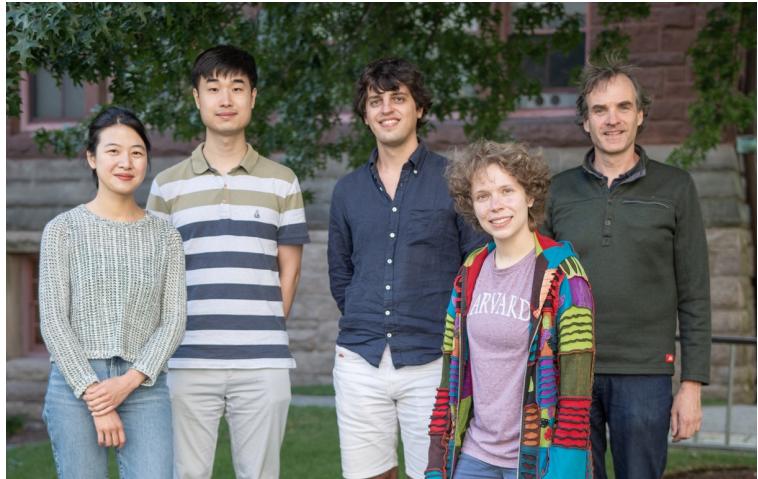
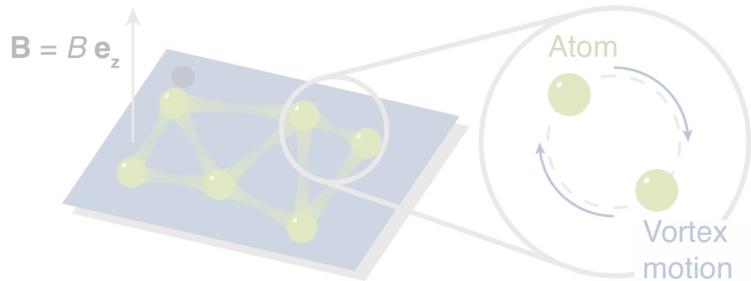
high fidelity  
state preparation



## QUANTUM AVALANCHES



## FRACTIONAL QUANTUM HALL STATES



Joyce  
Kwan

Sooshin  
Kim

J. L.  
Perrin  
Segura

Markus  
Greiner



Dries Sels,  
NYU/Flatiron



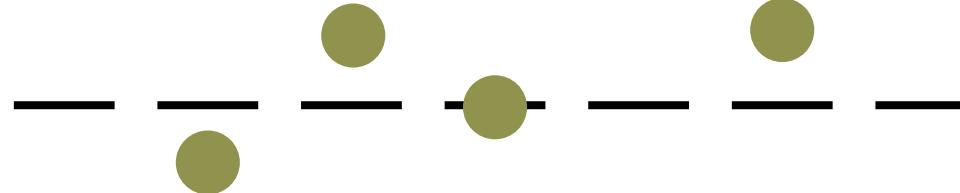
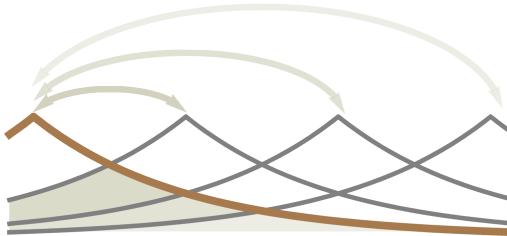
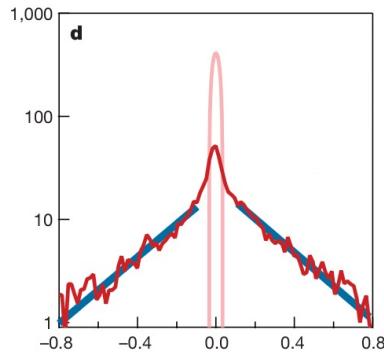
Eugene Demler  
ETH Zürich

# MANY-BODY LOCALIZATION

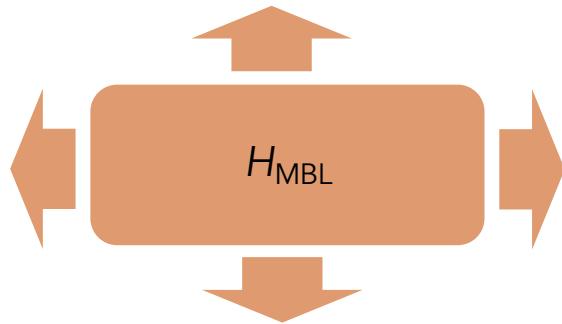
Disorder:  
Anderson localization

+

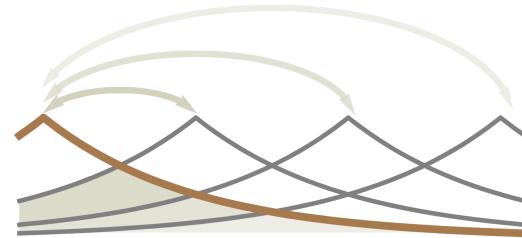
Interactions:  
Many-body localization



## TWO COMPETING EXPONENTIALS



**Hilbert space**  
grows exponentially  
→ thermalization,  
ergodicity breaking

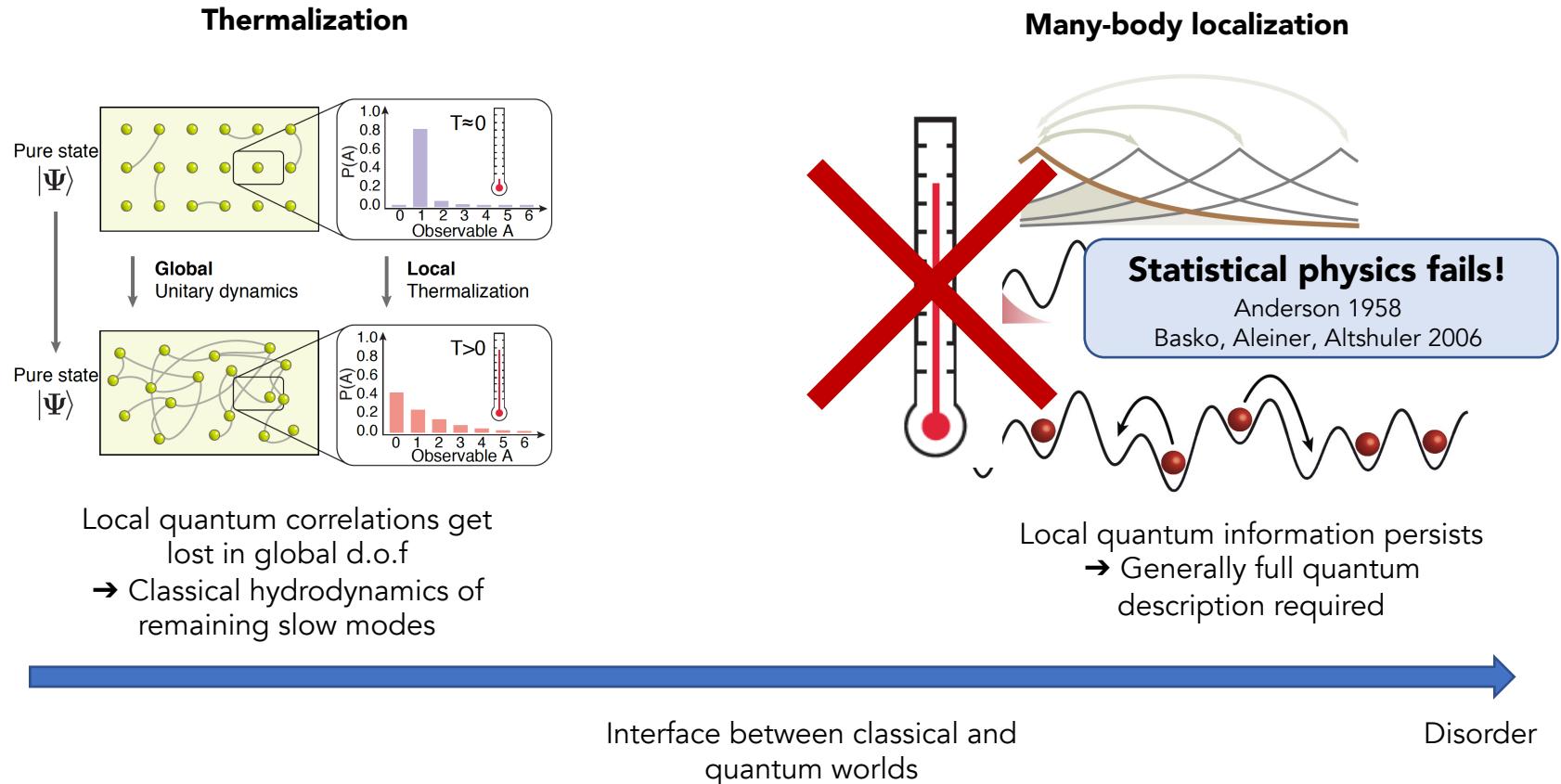


**Localization**  
Integrals of motion,  
reduces number of  
degrees of freedom

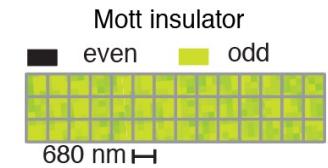
### Which one wins?

Basko, Aleiner, Altshuler 2006: localization wins  
Also Anderson 1958, Imbrie 2014

# THERMALIZATION VS LOCALIZATION



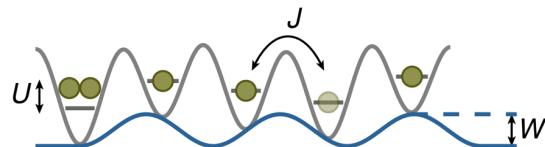
# NON-EQUILIBRIUM DYNAMICS



1xN initial state

Unitary evolution

$$|\Psi\rangle = e^{i\hat{\mathcal{H}}t/\hbar} |\Psi_0\rangle$$



Bose-Hubbard model  
programmable site offsets

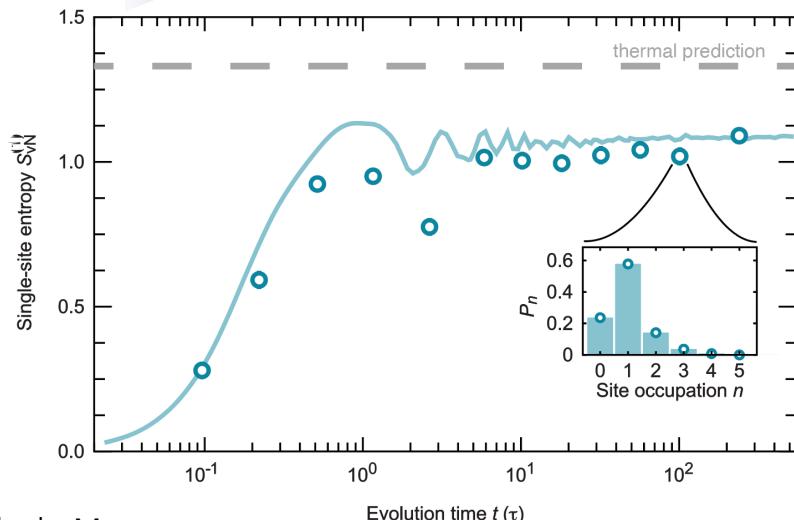
$$\hat{\mathcal{H}} = -J \sum_i \left( \hat{a}_i^\dagger \hat{a}_{i+1} + h.c. \right) + \frac{U}{2} \sum_i \hat{n}_i (\hat{n}_i - 1) + W \sum_i h_i \hat{n}_i$$

$$U = 3J$$

$h_i$  quasi-periodic with golden ratio 1.618



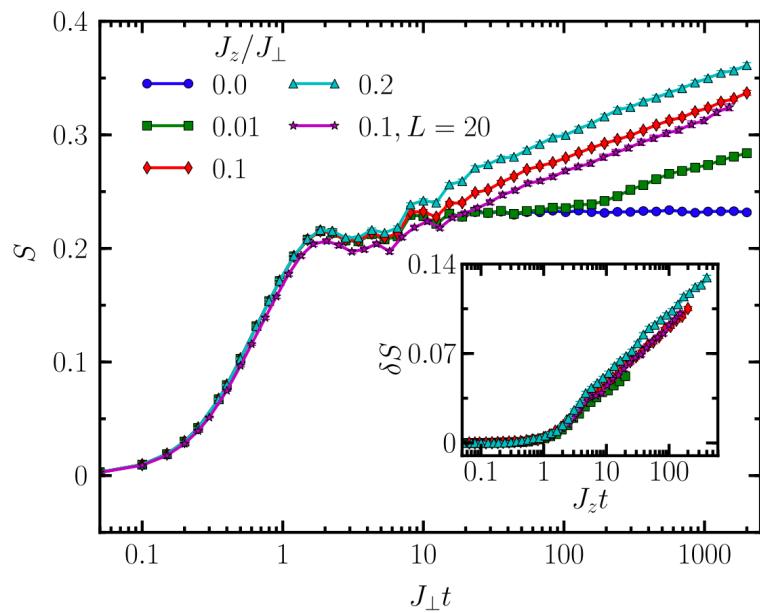
$$S_n = - \sum_n p_n \log p_n$$



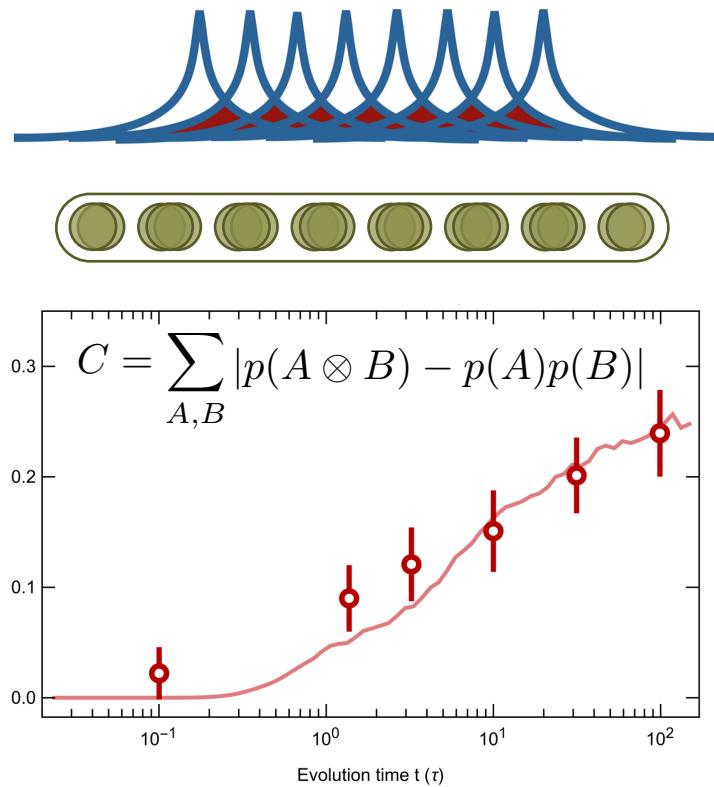
Also: Bloch, Monroe,  
DeMarco, Inguscio...

A. Lukin et al., Science 364, 6437 (2019)

# DEPHASING



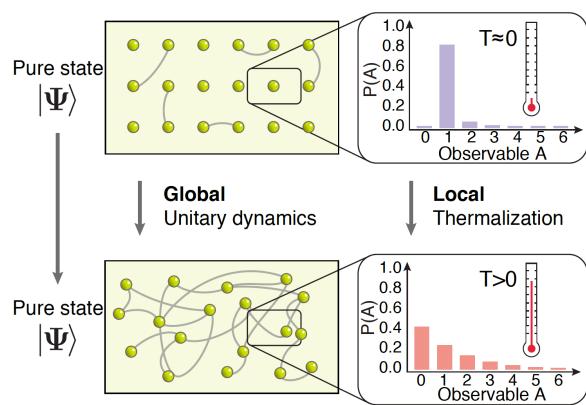
J. H. Bardarson et al., *PRL* **109**, 017202 (2012)



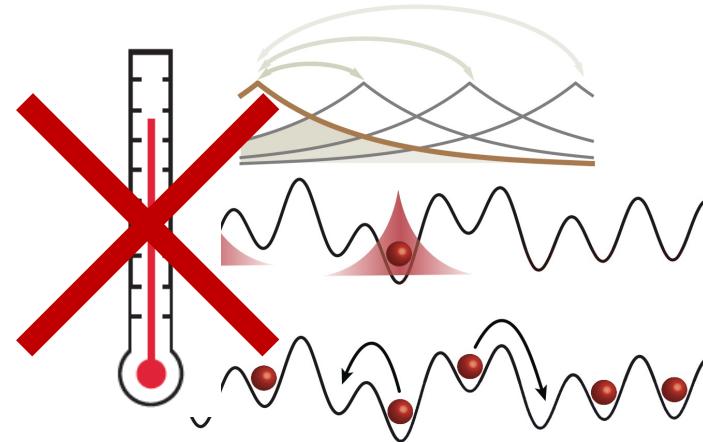
A. Lukin et al., *Science* **364**, 6437 (2019)

# THERMALIZATION VS LOCALIZATION

## Thermalization

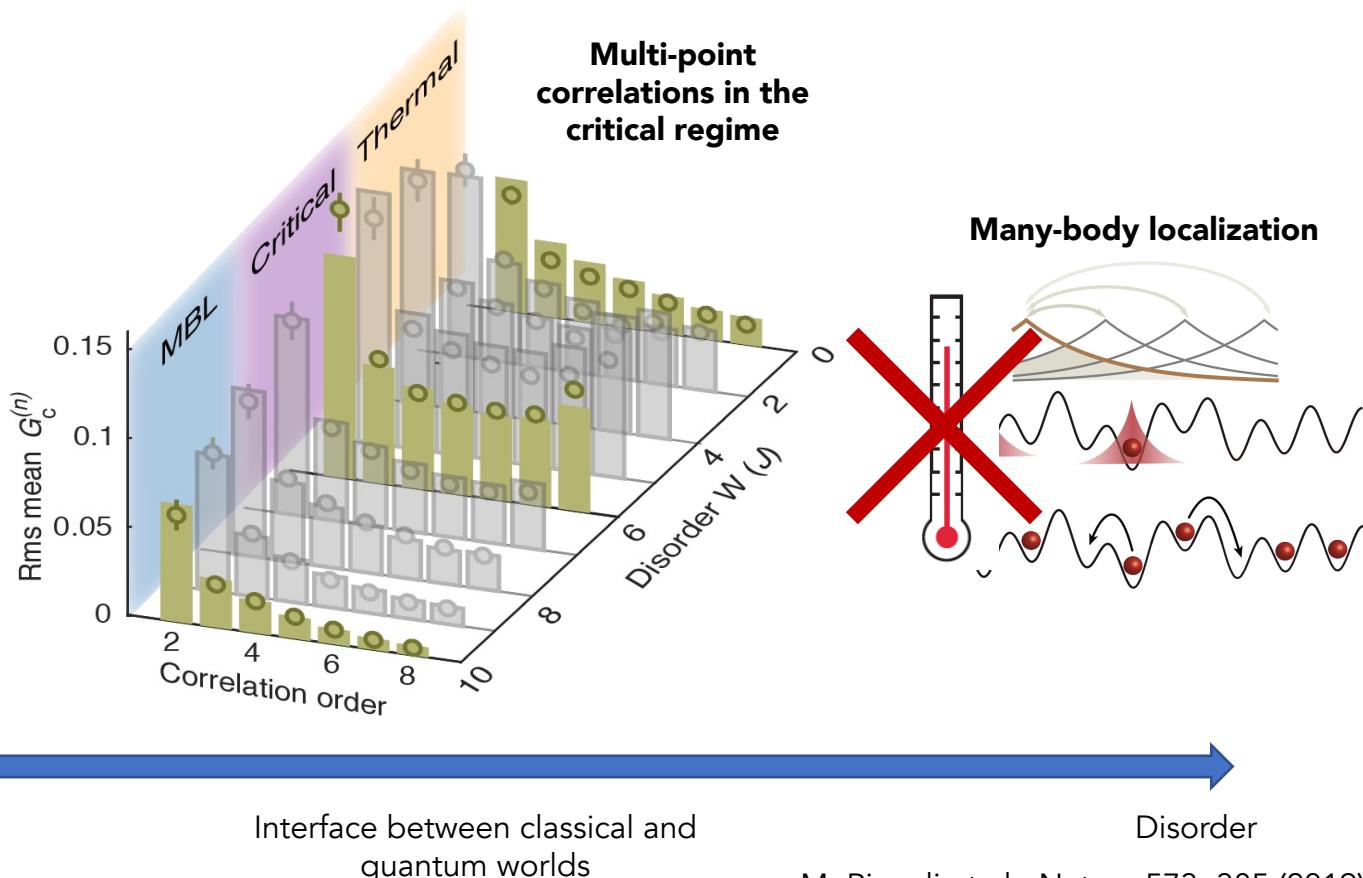
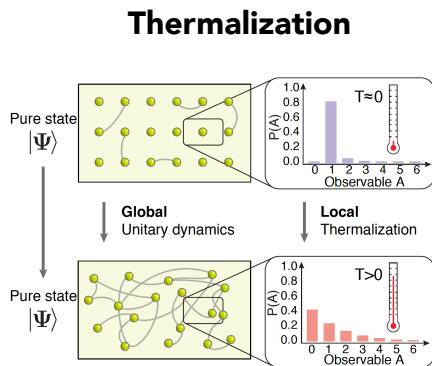


## Many-body localization



Interface between classical and quantum worlds      Disorder

# THERMALIZATION VS LOCALIZATION



# IS MANY-BODY LOCALIZATION STABLE?

## CONTRA

Quantum chaos challenges many-body localization  
Jan Suntajs et al.

Evidence for unbounded growth of the number entropy in many-body localized phases  
Maximilian Kiefer-Emmanouilidis et al.

Ergodicity breaking transition in finite disordered spin chains  
Jan Suntajs et al.

Dynamical obstruction to localization in a disordered spin chain  
Dries Sels et al.

Slow delocalization of particles in many-body localized phases  
Maximilian Kiefer-Emmanouilidis et al.

Unlimited growth of particle fluctuations in many-body localized phases  
Maximilian Kiefer-Emmanouilidis et al.

Markovian baths and quantum avalanches  
Dries Sels

Particle fluctuations and the failure of simple effective models for the many-body localized phases  
Maximilian Kiefer-Emmanouilidis et al.

...

## PRO

Distinguishing localization from chaos: challenges in finite-size systems  
Dmitry Abanin et al.

Can we study the many-body localization transition  
Rajat K. Panda et al.

Thouless time analysis of Anderson and many-body localization transitions  
Piotr Sierant et al.

Polynomially filtered exact diagonalization approach to many-body localization  
Piotr Sierant et al.

Is there slow particle transport in the MBL phase  
David J. Luitz et al.

Avalanches and many-body resonances in many-body localized systems  
Alan Morningstar et al.

Can we observe the many-body localization transition?  
Piotr Sierant et al.

Resonance-induced growth of the number entropy in strongly disordered systems  
Roopayan Ghosh et al.

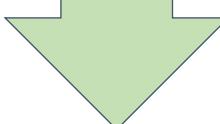
...

2019

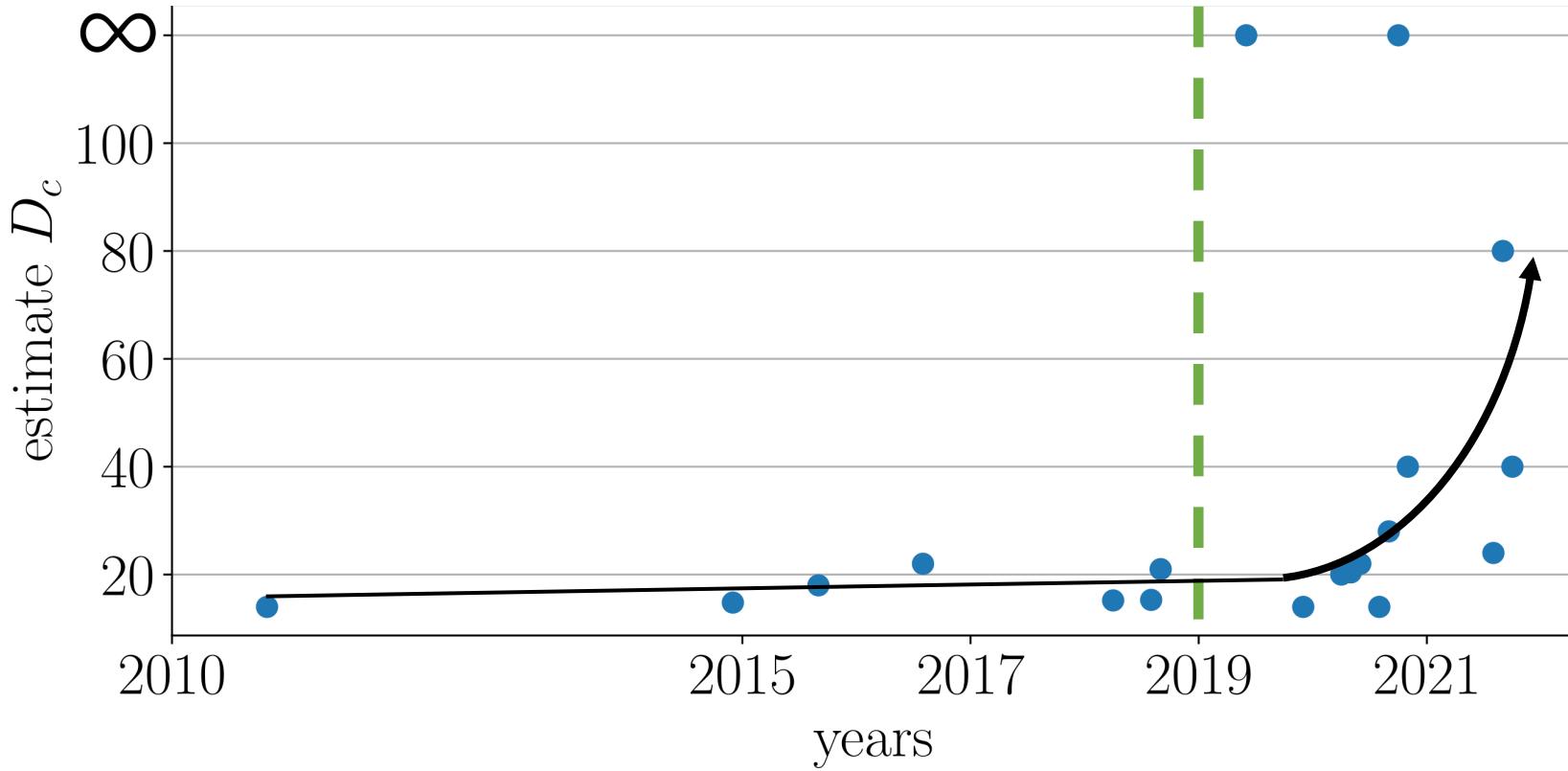
2020

2021

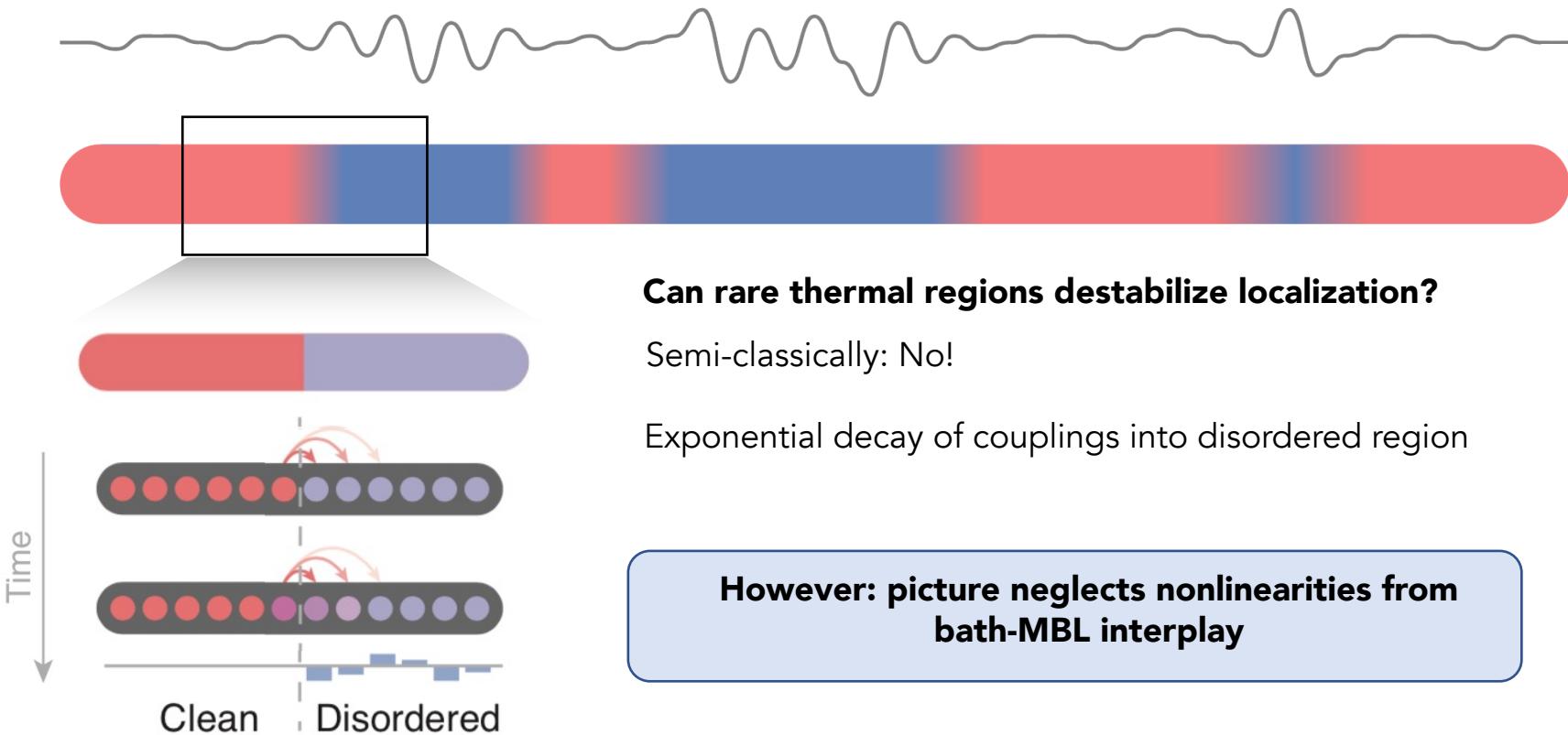
2022



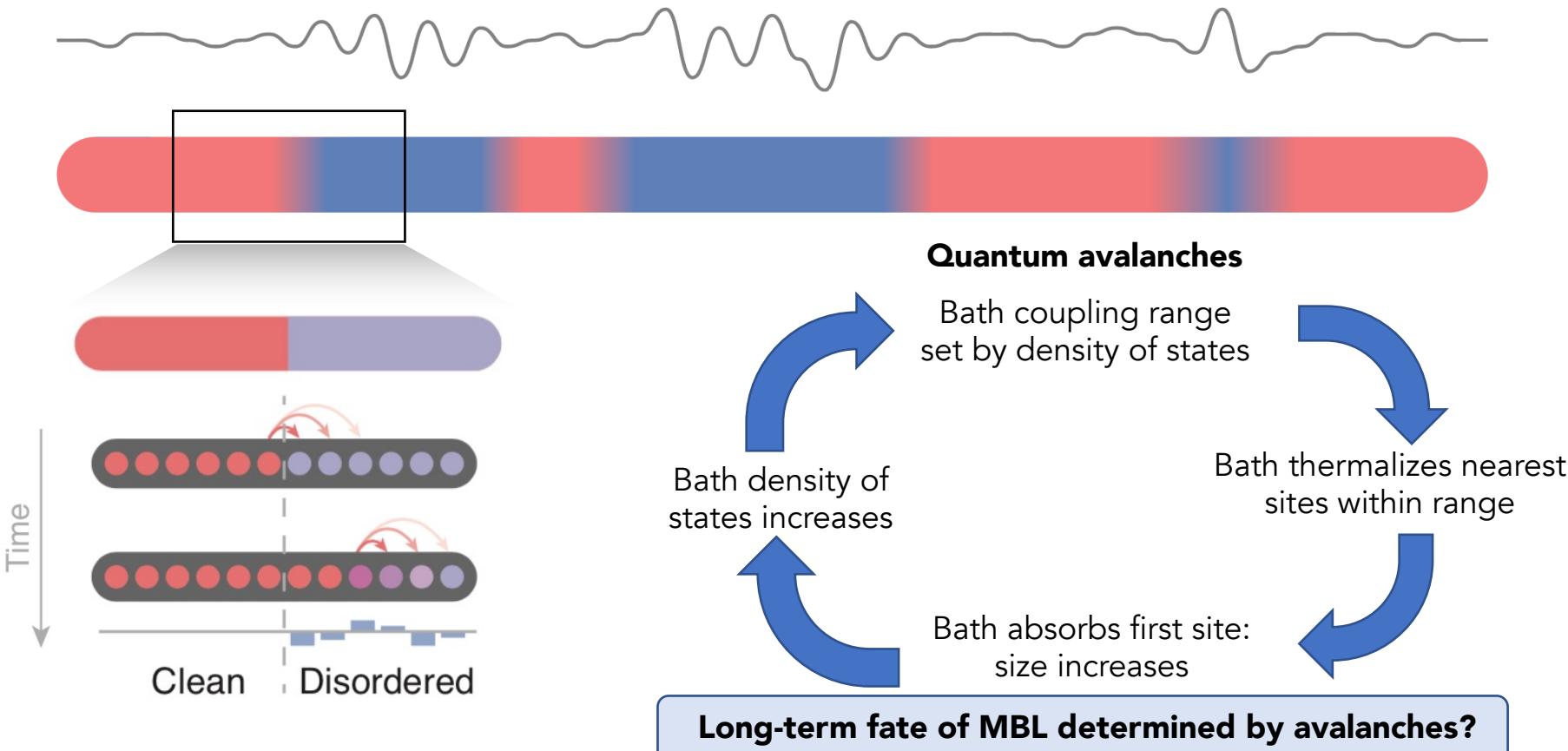
## IS MANY-BODY LOCALIZATION STABLE?



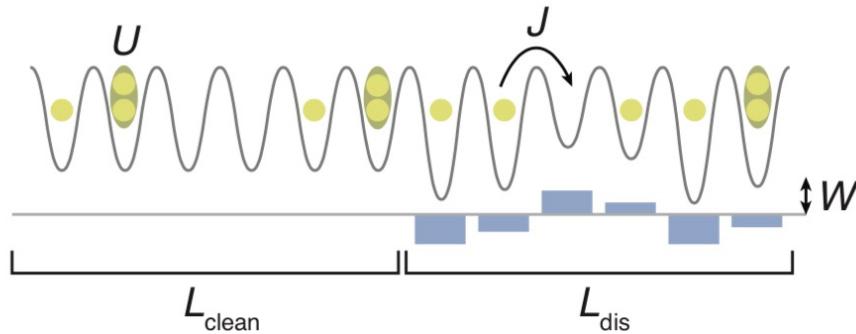
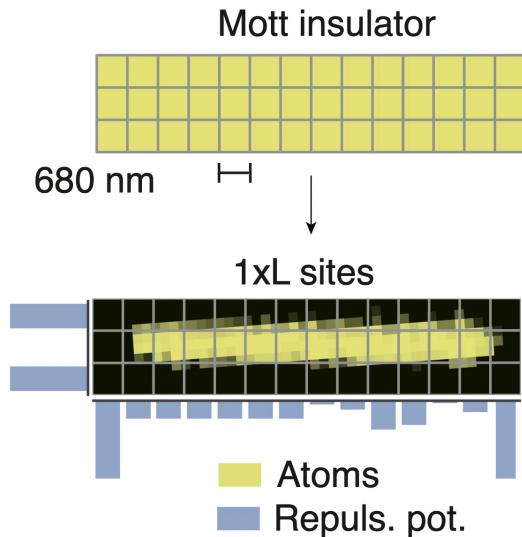
# THERMAL INCLUSIONS



# THERMAL INCLUSIONS



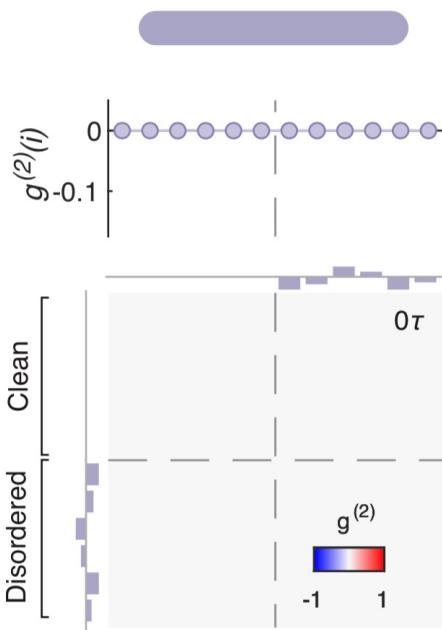
# CLEAN-DISORDER INTERFACE



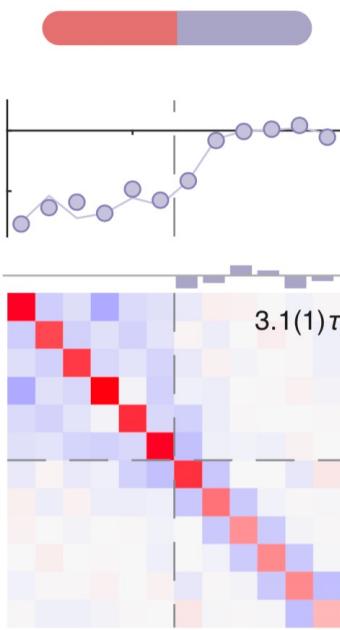
- $L_{\text{clean}}$  sites without disorder
- $L_{\text{dis}}$  sites with disorder (quasi-periodic)

# AVALANCHE DYNAMICS

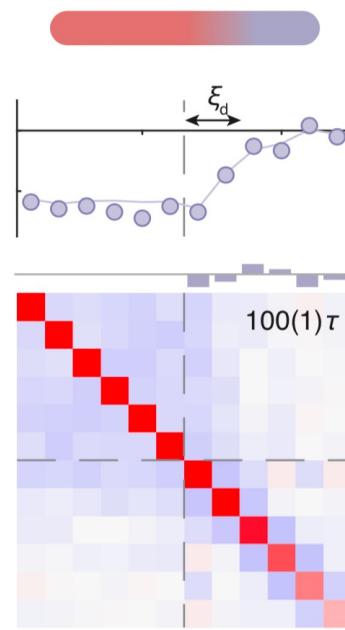
Quenched initial state



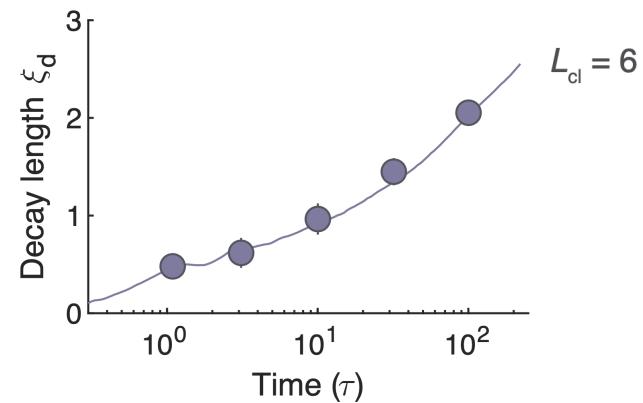
Separate dynamics



Transport across interface

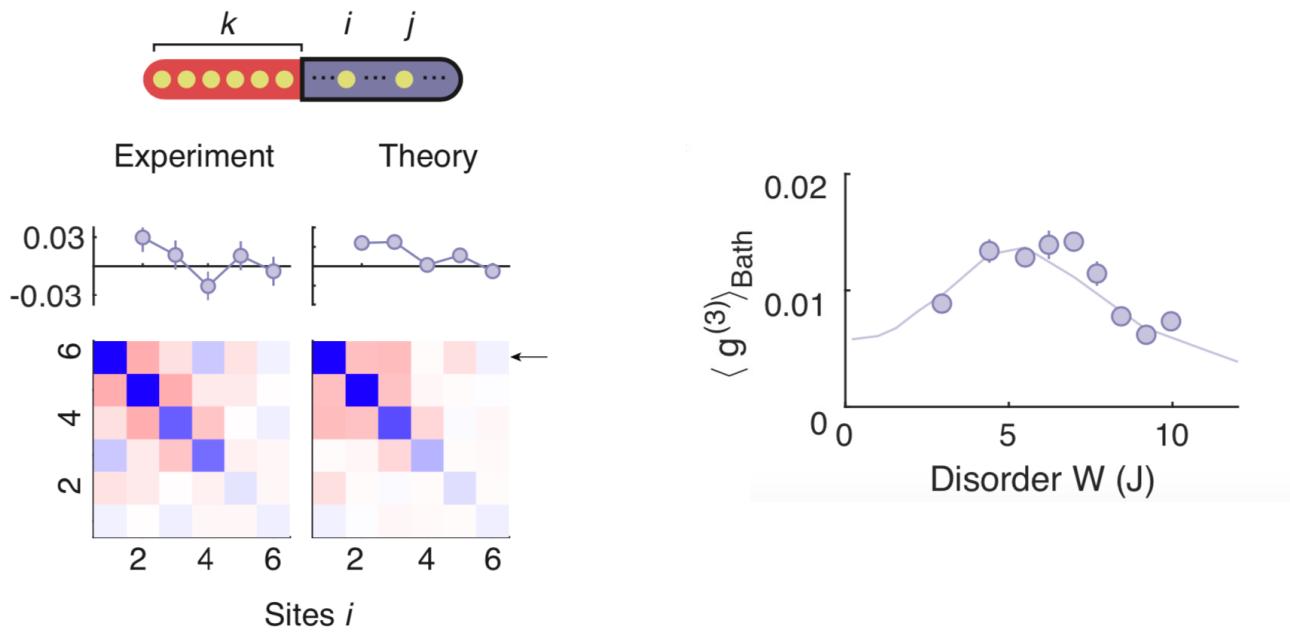


**Accelerated thermalization**



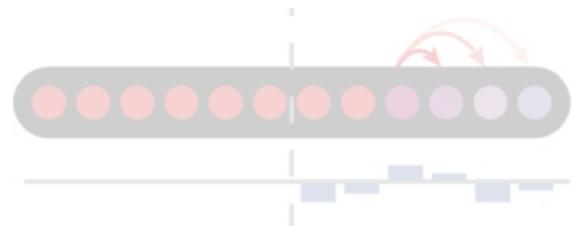
$$g^{(2)}(i, j) = \langle \hat{n}_i n_j \rangle - \langle \hat{n}_i \rangle \langle \hat{n}_j \rangle$$

# THREE-BODY CORRELATIONS

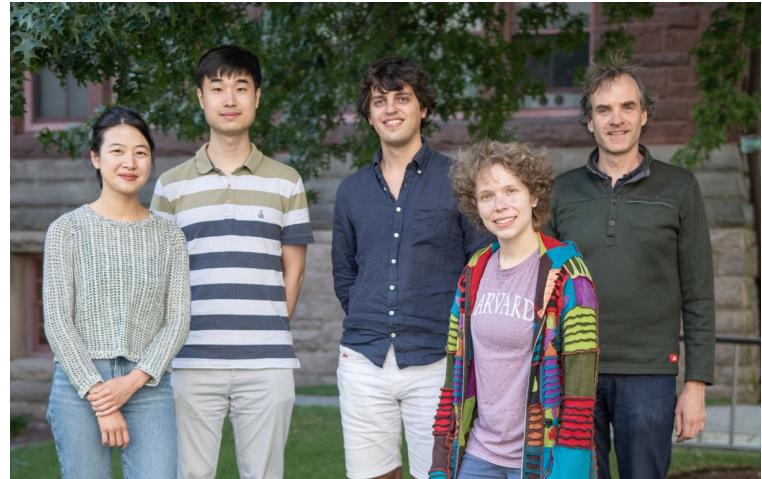
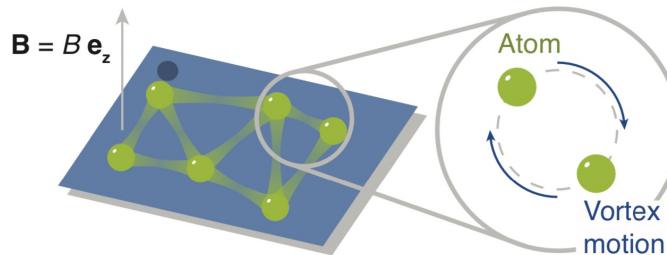


→ driven by many-body processes

## AVALANCHE THERMALIZATION



## FRACTIONAL QUANTUM HALL PHYSICS



Joyce  
Kwan

Sooshin  
Kim

J. L.  
Perrin  
Segura

Markus  
Greiner



Nathan Goldman  
ULB



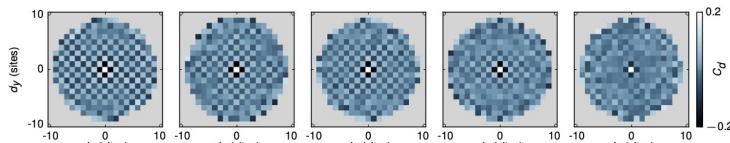
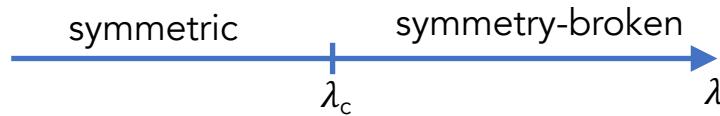
Fabian Grusdt  
LMU Munich



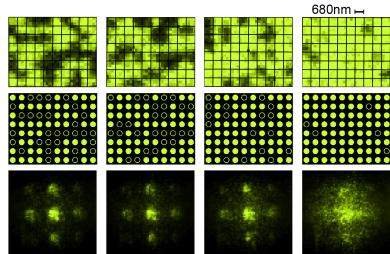
Cécile Repellin,  
Univ. Grenoble

# NOVEL STATES OF MATTER

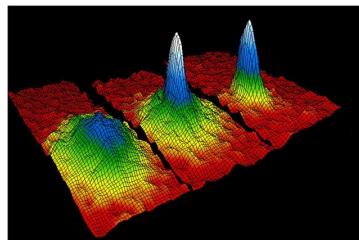
## Ginzburg Landau paradigm: order parameter



Mazurenko 2017

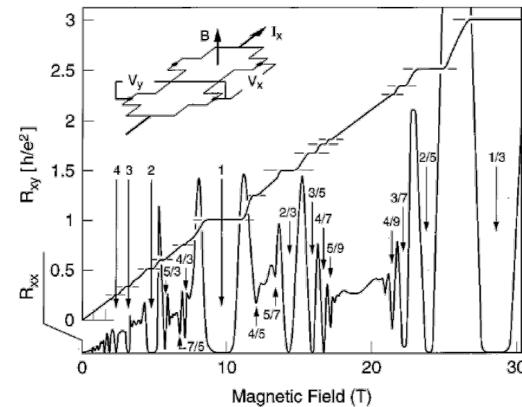
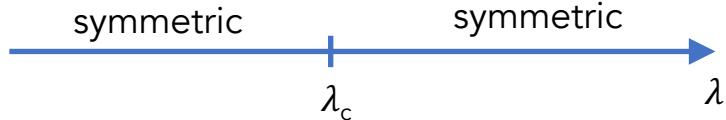


Bakr 2010

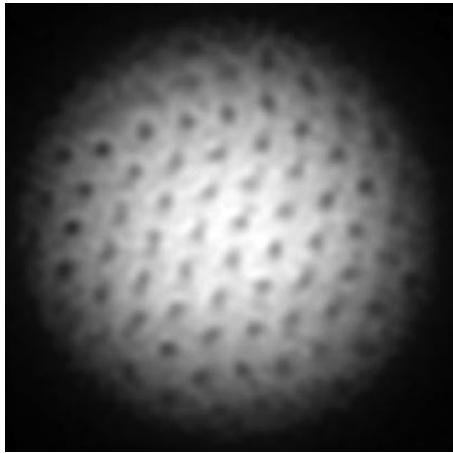


Anderson 1995

## Beyond Ginzburg-Landau: Topological order



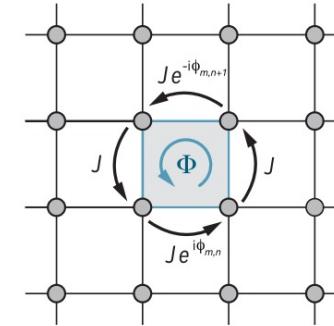
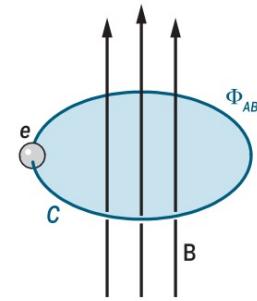
## TWO STRATEGIES FOR COLD-ATOM TOPOLOGY



### Rotating systems

Coriolis force emulates Lorenz force

Dalibard, Zwierlein, Spielman,  
Chu/Gemelke...



### Laser-assisted tunneling

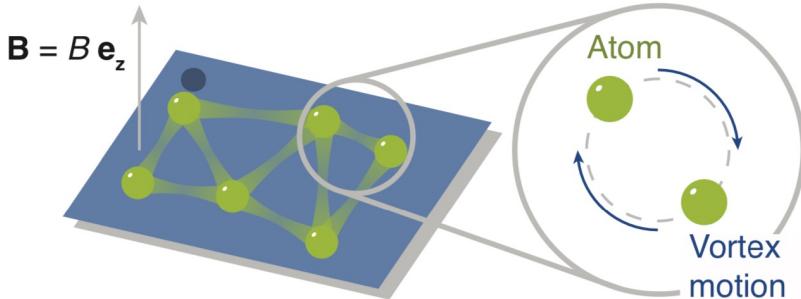
Engineer Peierls phase via lattice modulation

Esslinger, Bloch/Aidelsburger, Sengstock,  
Ketterle,...

**No FQH states yet!**

Main challenge: Floquet heating, particularly  
in interacting systems

# KEY PROPERTIES OF FQH STATES



## Laughlin states

Paradigmatic class of FQH states

Many-body wavefunction:

$$\psi \sim \prod_{i < j} |z_i - z_j|^m e^{-\sum_i |z_i|^2}$$

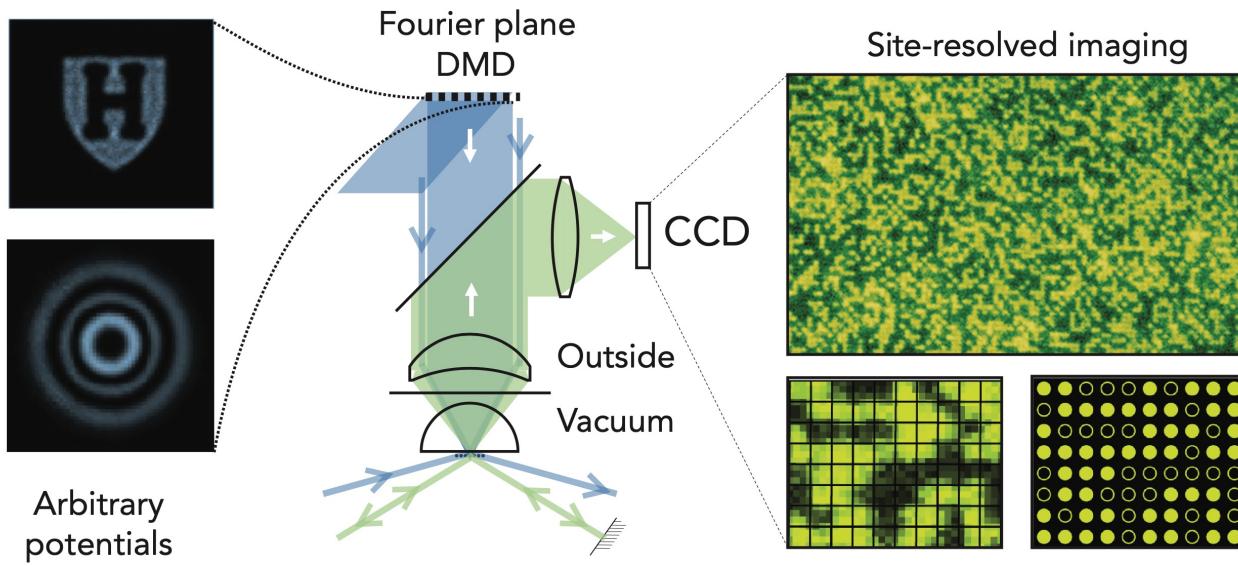
$m$  even: bosons

$m$  odd: fermions

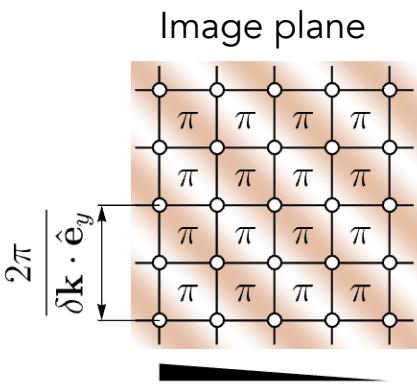
## Properties

- Shielded interactions: no two particles at the same position
- Vortex motion protects topology
- Fractional Hall conductivity
- crucial information in  $g^{(2)}$  correlations  
→ minimal system:  $N = 2$

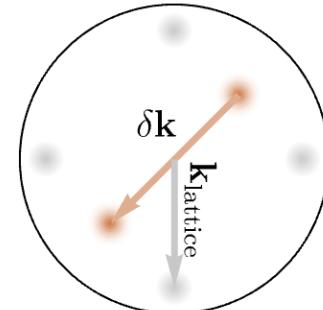
# QUANTUM GAS MICROSCOPE



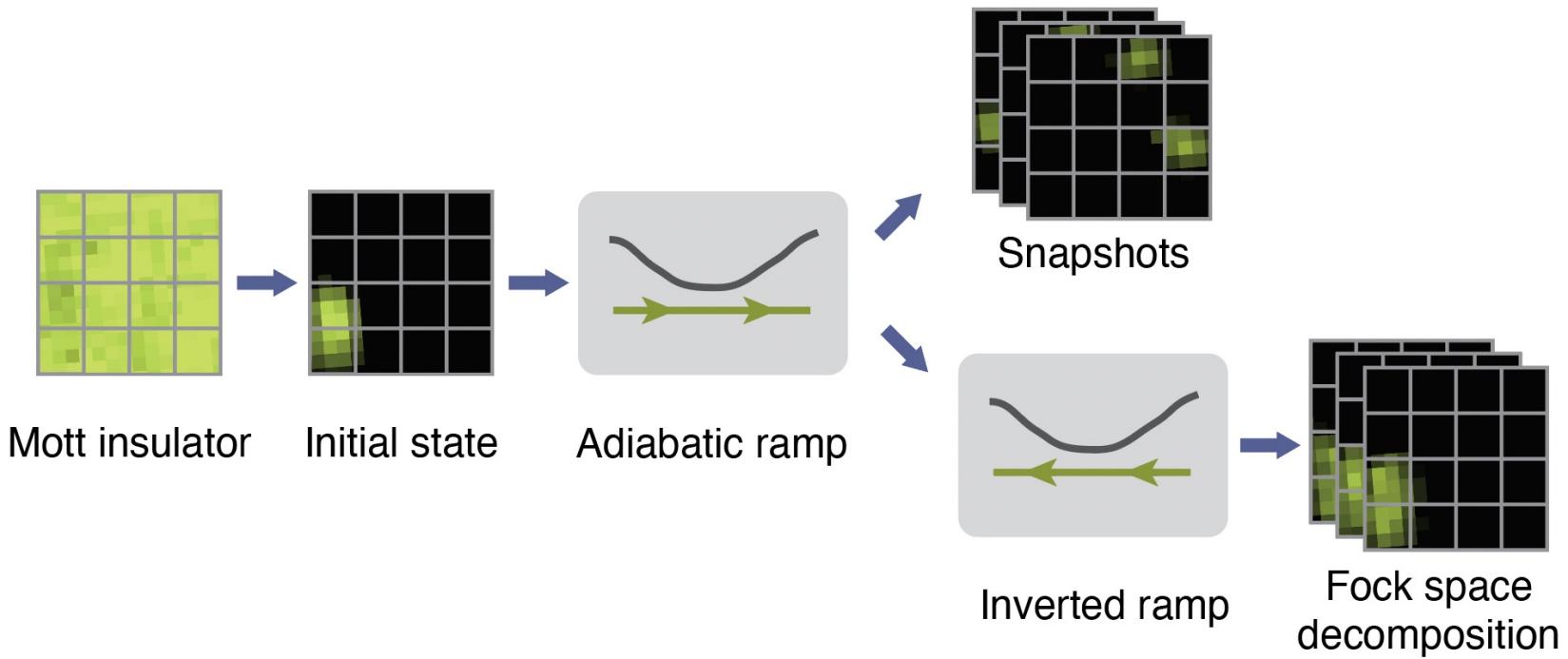
Tunable flux



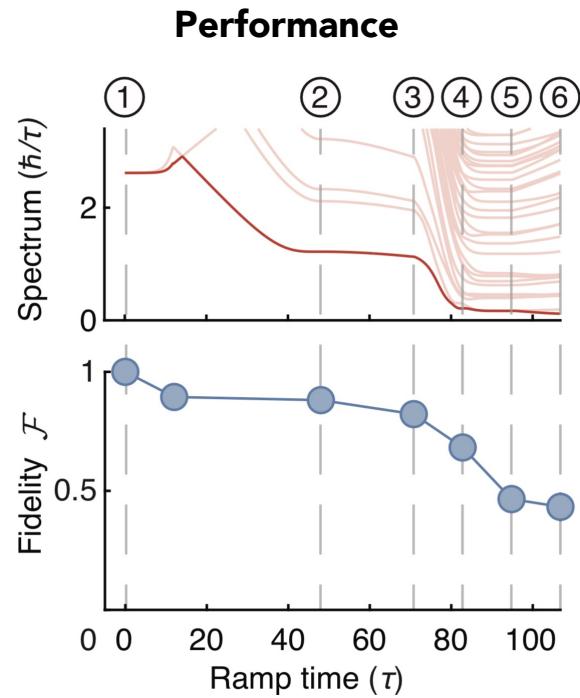
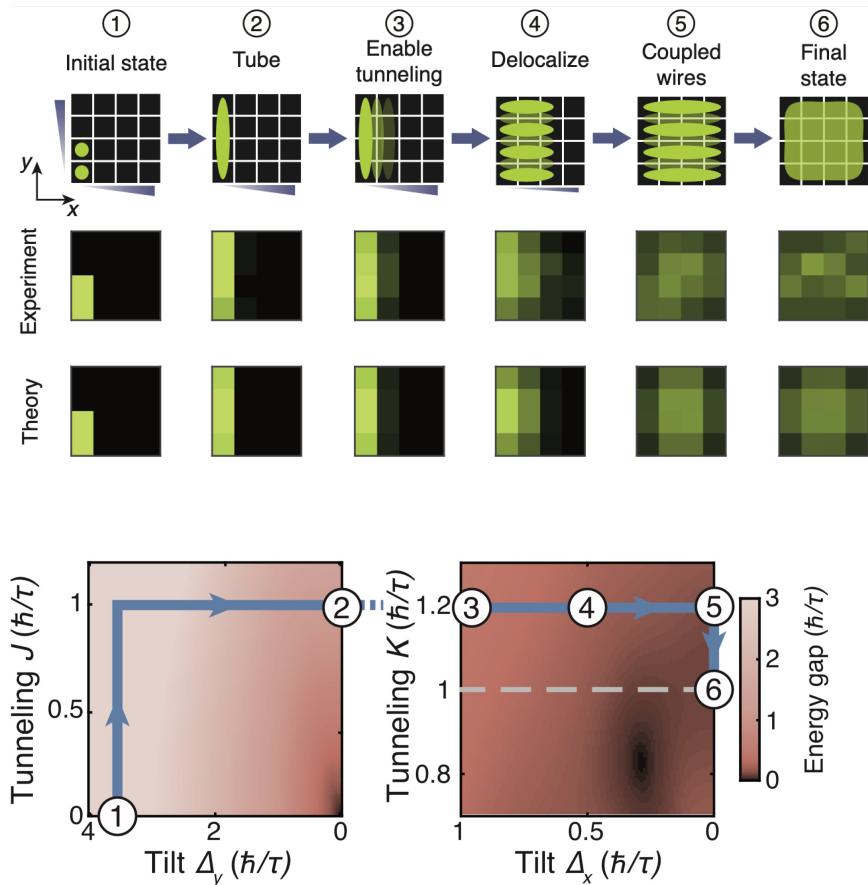
Fourier plane



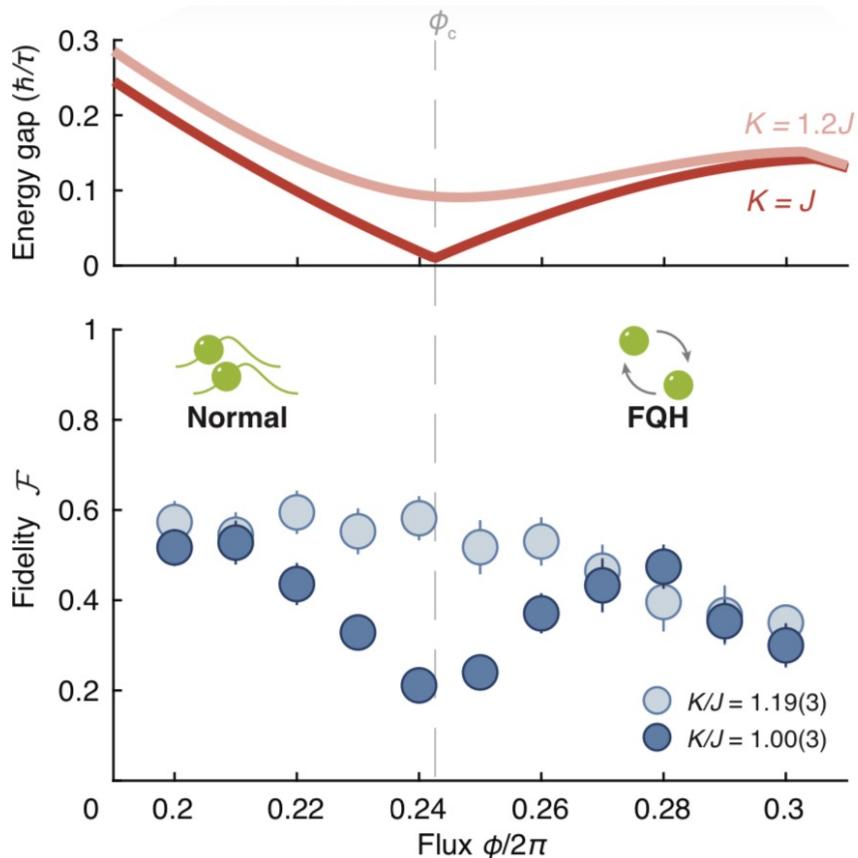
# PROTOCOL



# STATE PREPARATION



# MAPPING OUT THE PHASE DIAGRAM

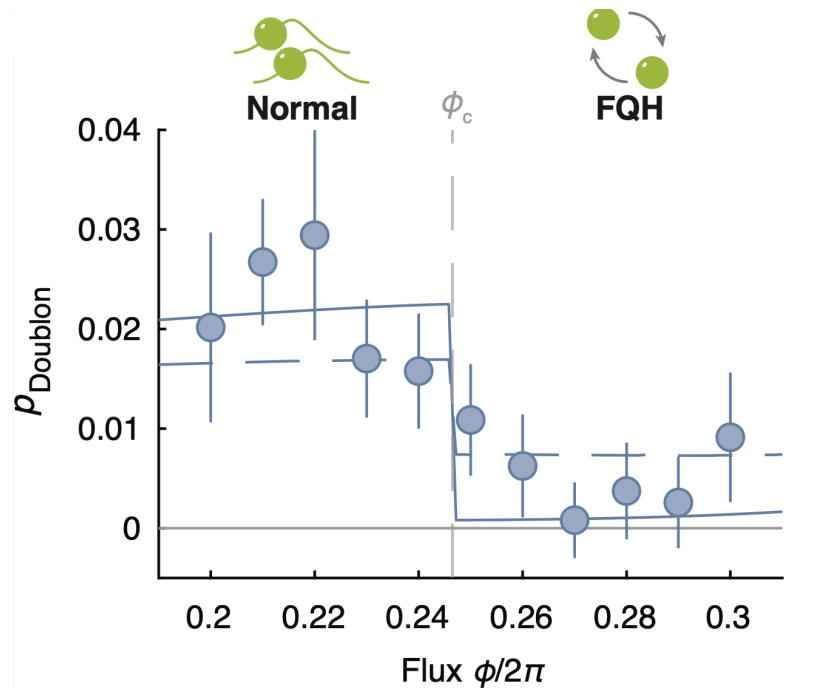


Idea:

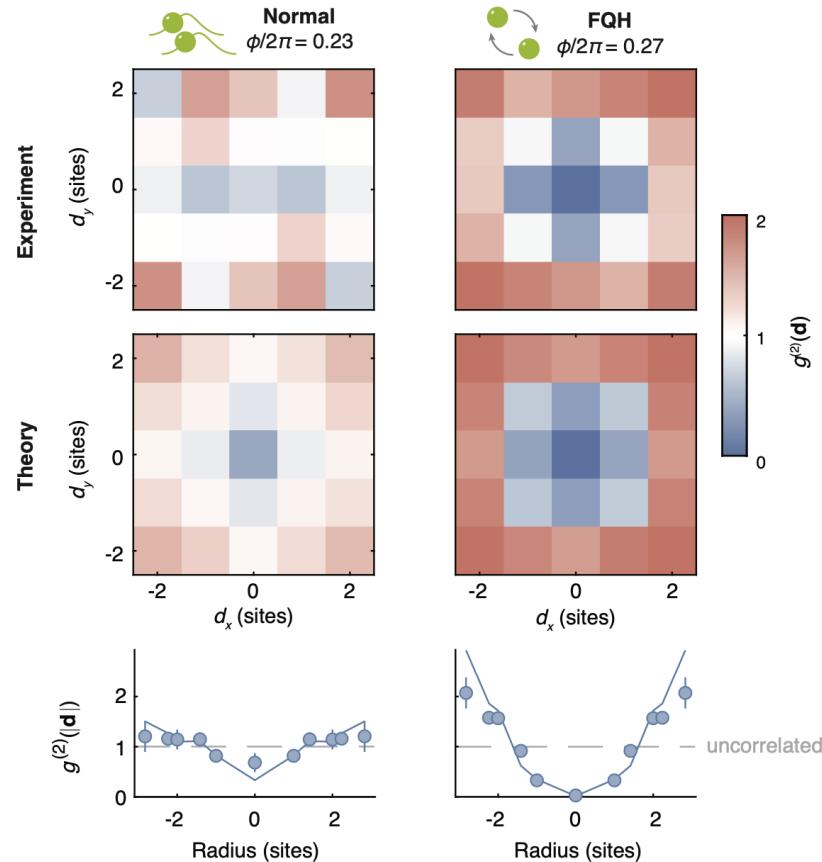
Use fidelity as spectroscopic probe  
for many-body gap

Many-body gap closing  
reveals topological transition

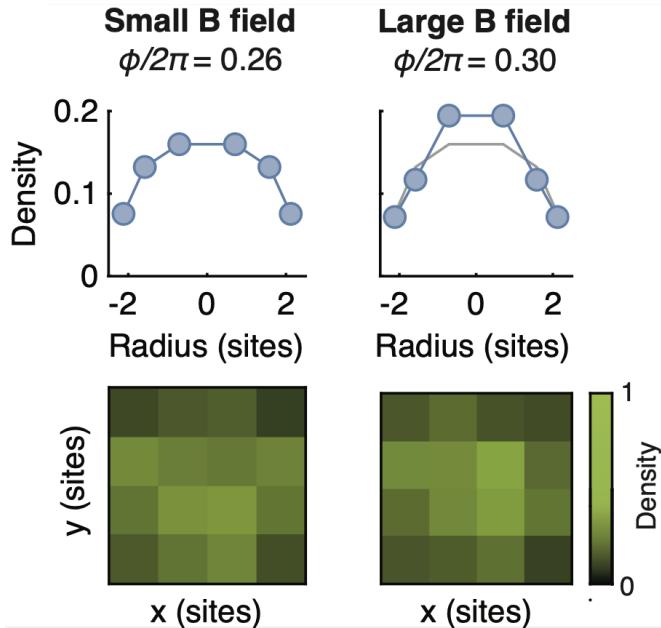
# MICROSCOPIC STRUCTURE



**Vortex motion suppresses correlations at short-distance**

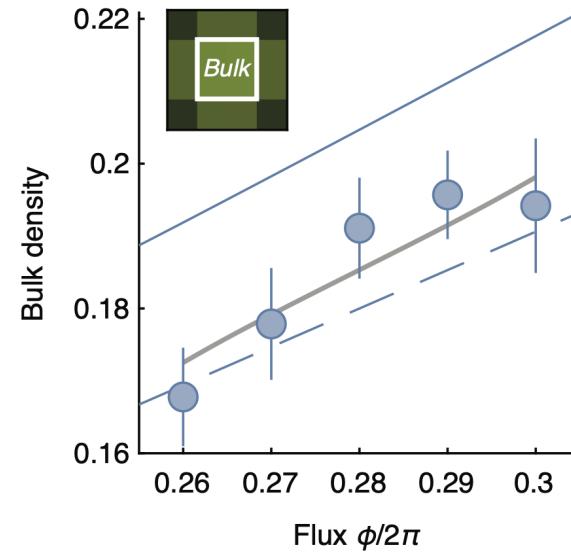


# FRACTIONAL HALL CONDUCTIVITY



**Streda's formula:**

$$\frac{\sigma_H}{\sigma_0} = \frac{\partial \rho_{\text{Bulk}}}{\partial \alpha}$$



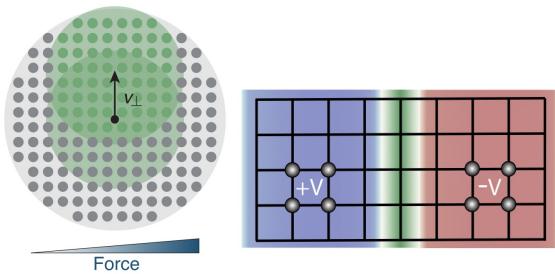
**Fractional Hall conductivity:**

$$\sigma_H/\sigma_0 = 0.6(2)$$

Thermodynamic limit:  $\nu_{\text{MB}} = 0.5$

# OUTLOOK

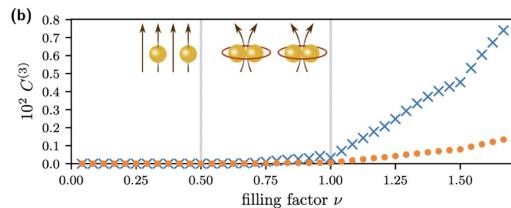
## Further topological signatures



Repellin et al., PRA 102, 063317 (2020)

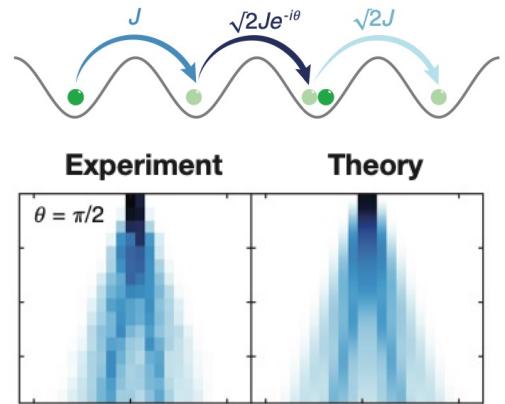
Raciunas et al., PRA 98, 063621 (2018)

## Pfaffian states, non-abelian anyons



Palm et al., PRB 103, L161101 (2021)

## 1D anyons



J. Kwan et al., arXiv:2306.01737



# VIENNA LAB



**VCQ**

**FWF**

Der Wissenschaftsfonds.



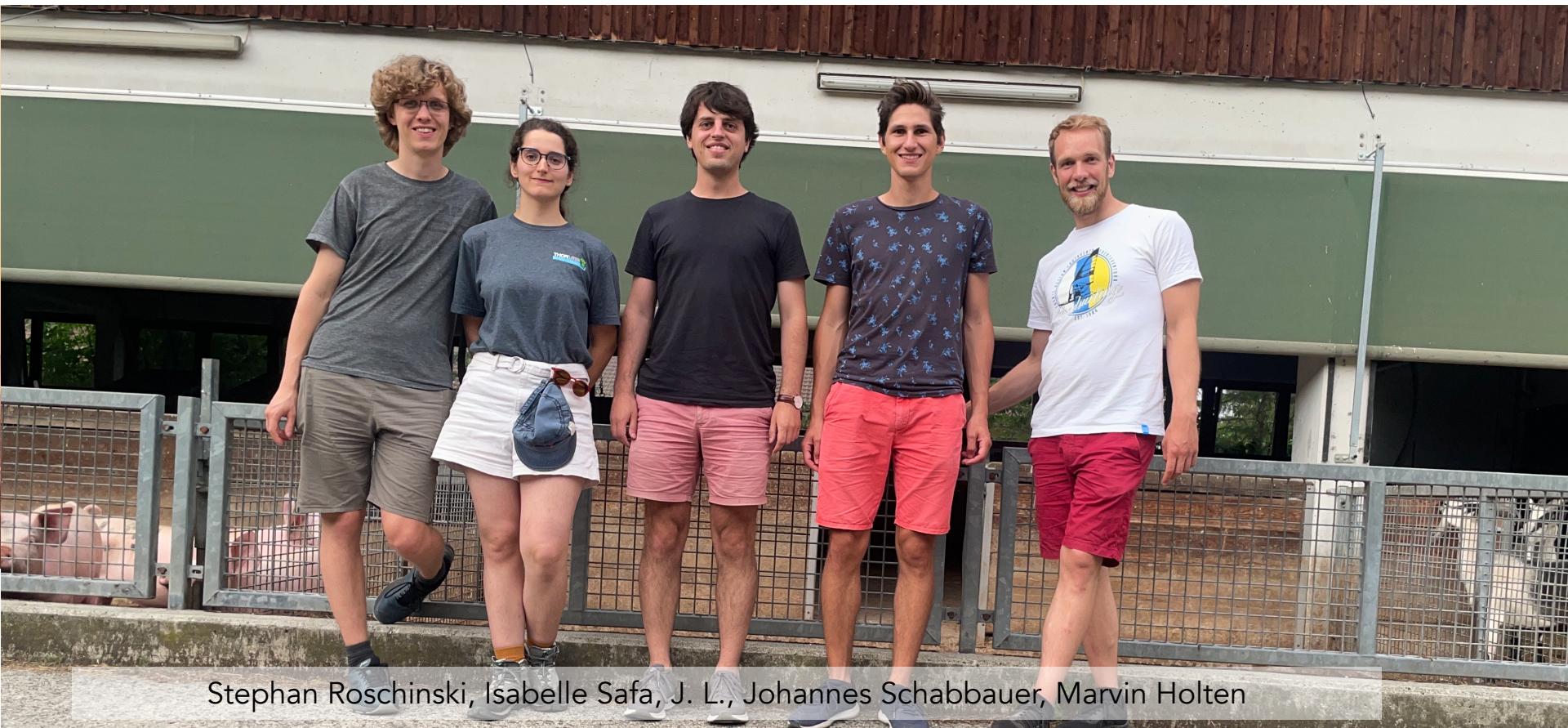
**FFG**

Promoting Innovation.



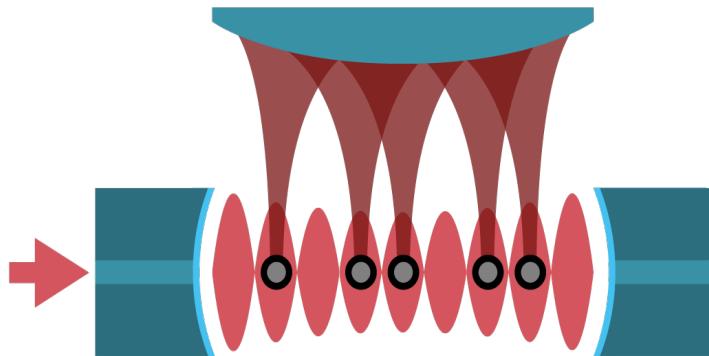
TECHNISCHE  
UNIVERSITÄT  
WIEN

# VIENNA LAB



Stephan Roschinski, Isabelle Safa, J. L., Johannes Schabbauer, Marvin Holten

# TWEEZER ARRAY IN A CAVITY

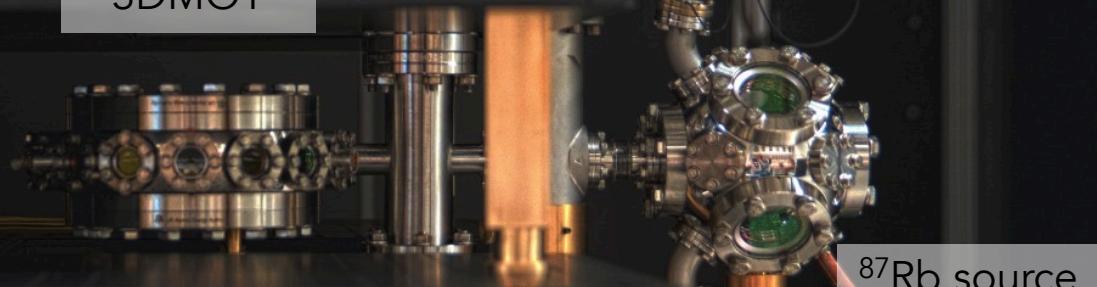
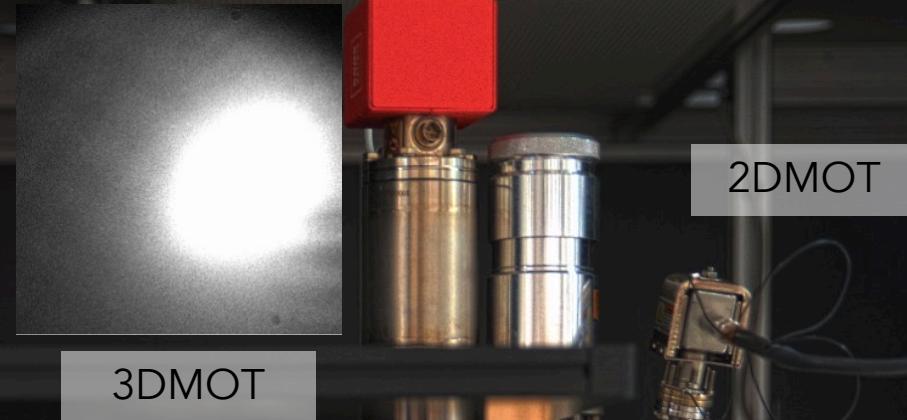
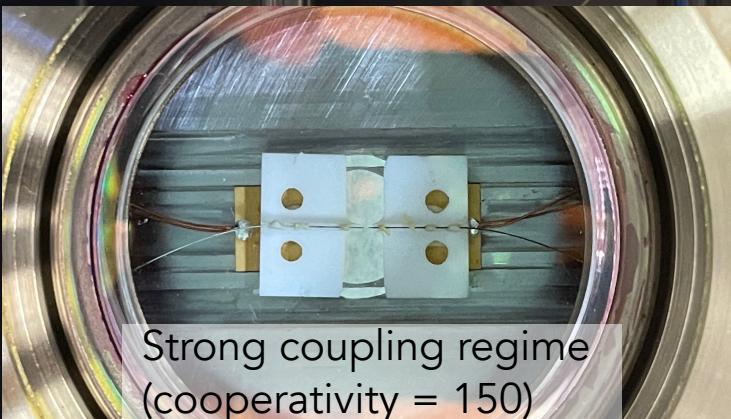


Non-local entanglement

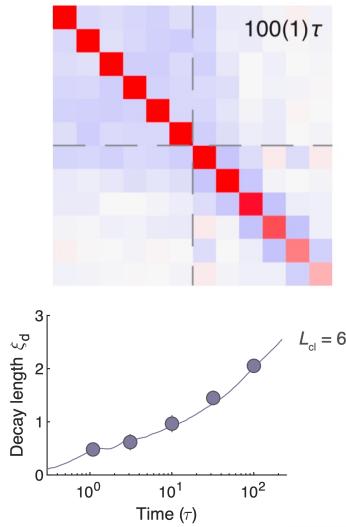
Long-range spin models

Non-demolition readout

Quantum networks



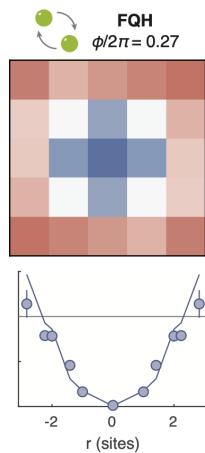
# SUMMARY



## Non-equilibrium quantum systems

Many-body localization  
Avalanche instability

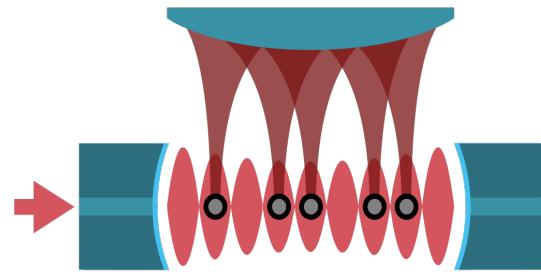
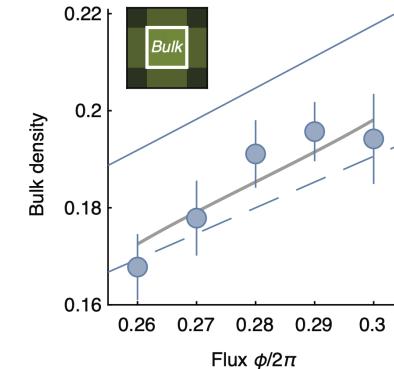
J. Léonard et al., Nat.  
Phys. 19, 481 (2023)



## Topological quantum matter

Fractional quantum Hall state  
Microscopy of correlations

J. Léonard et al.,  
Nature 619, 495 (2023)



## A photon-coupled neutral atom array

Cavity setup with high aperture  
Engineering entanglement

THANK YOU