

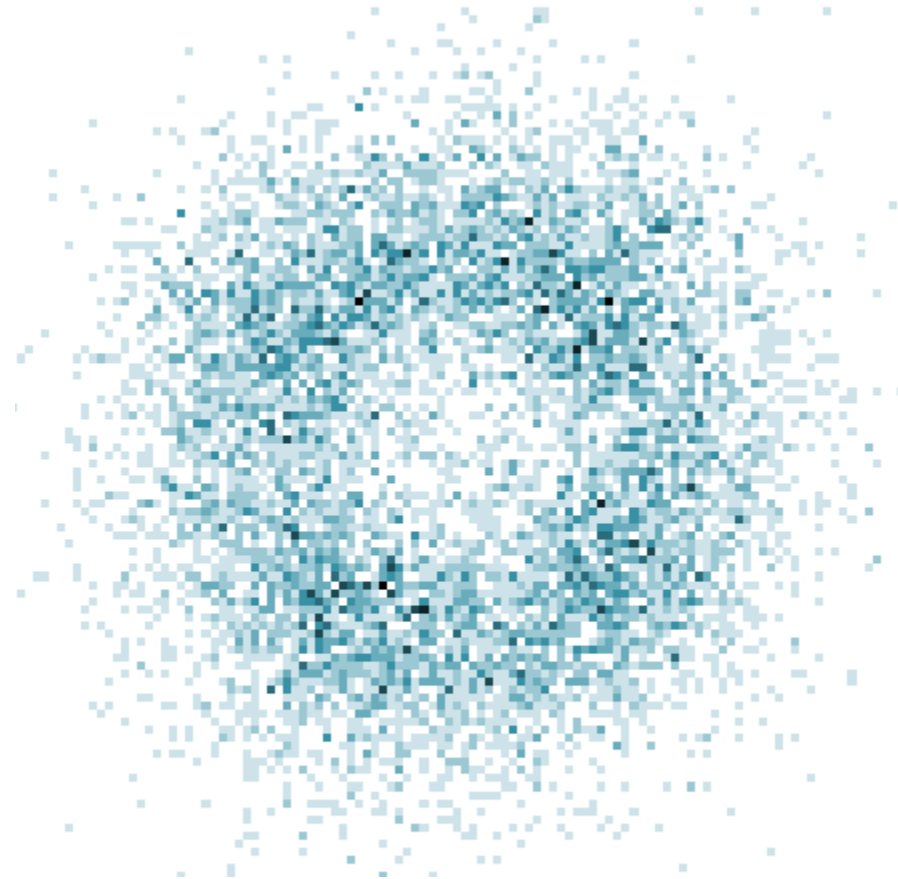
Rotating traps, a Laughlin wave function, and the emergence of fluid behavior.



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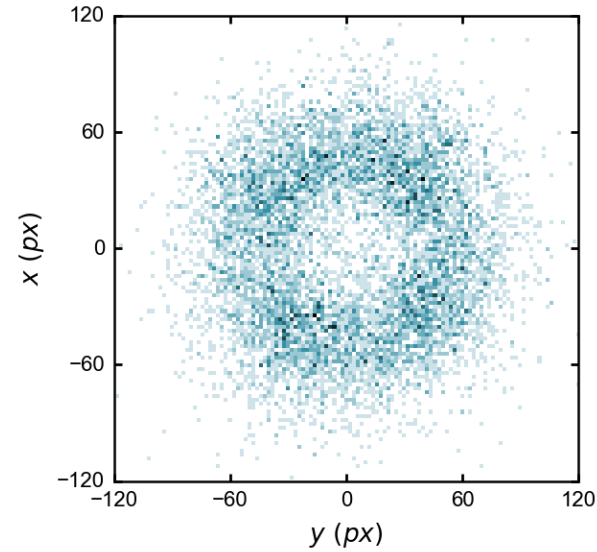
Barcelona, September 2023

Selim Jochim, Heidelberg University

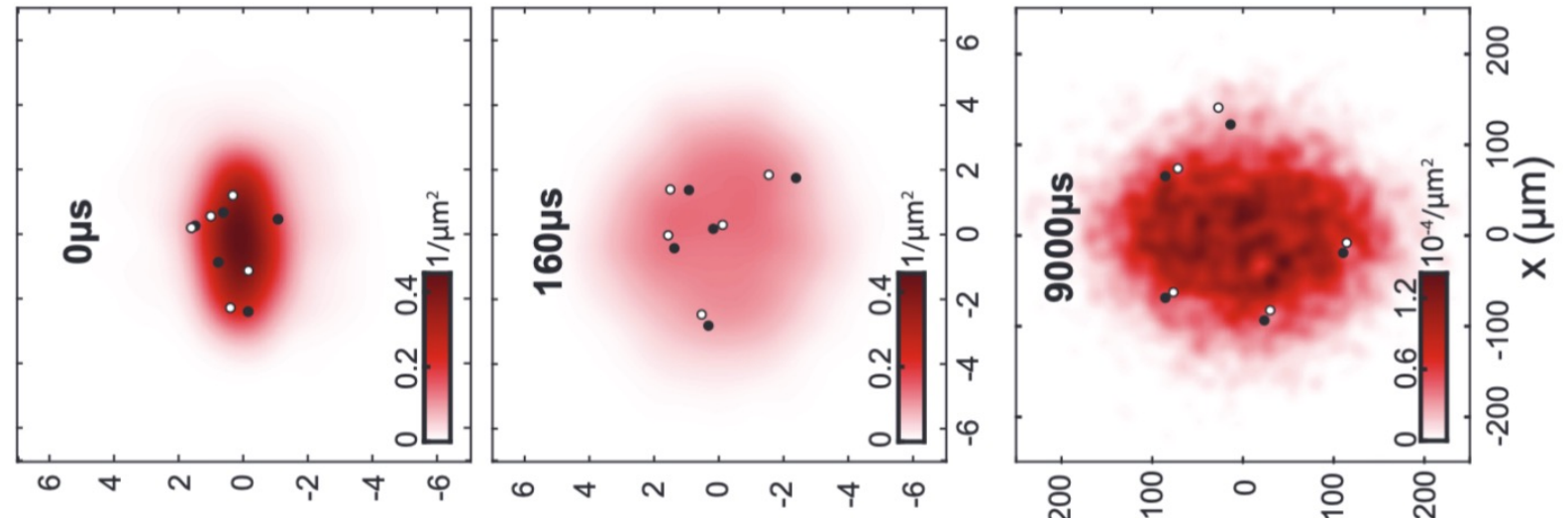


Outline

- Single atoms in discrete angular momentum states
- Two atoms turning around each other – a Laughlin state



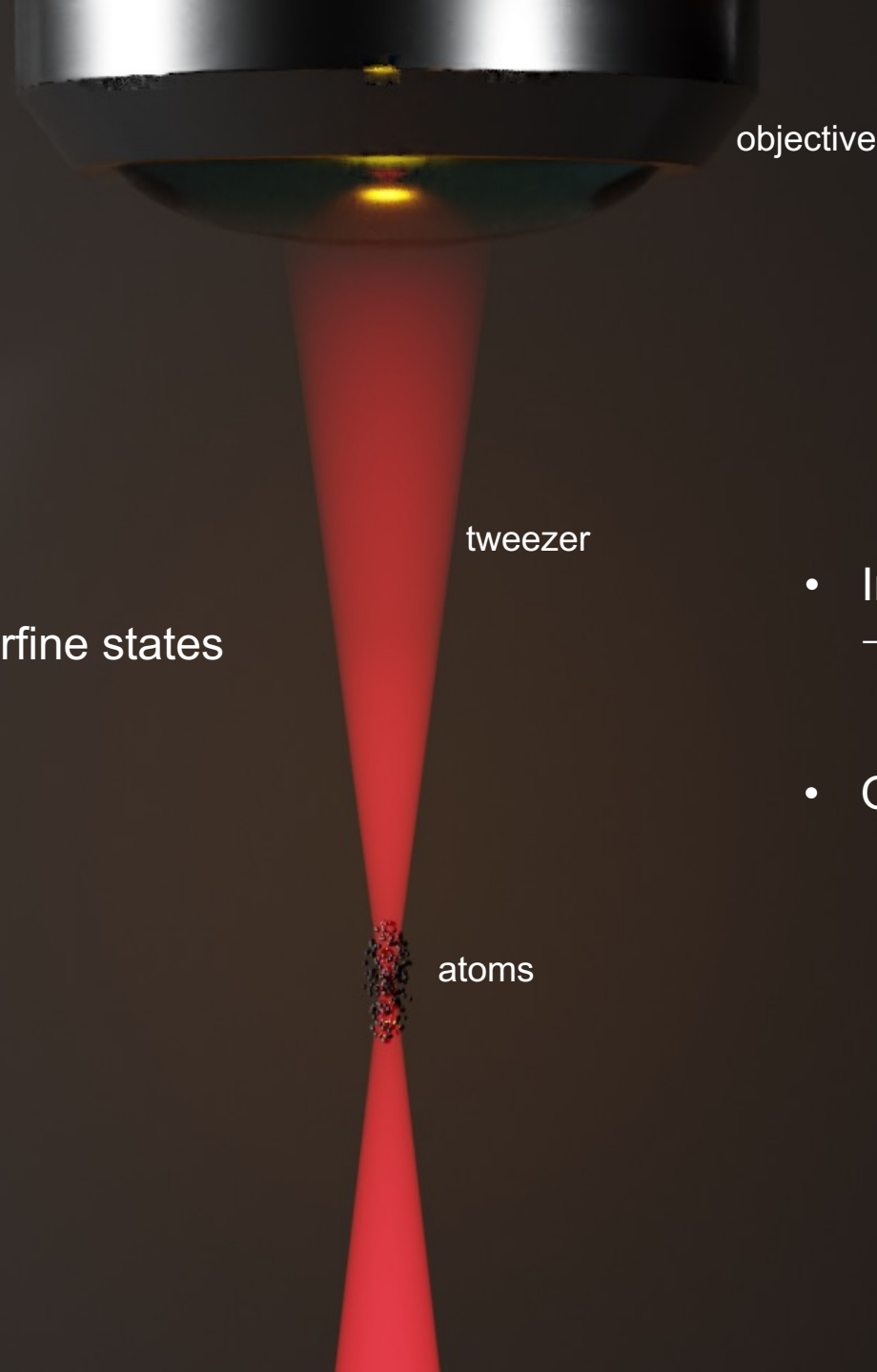
- 10 atoms acting like a fluid



Rotating two fermions



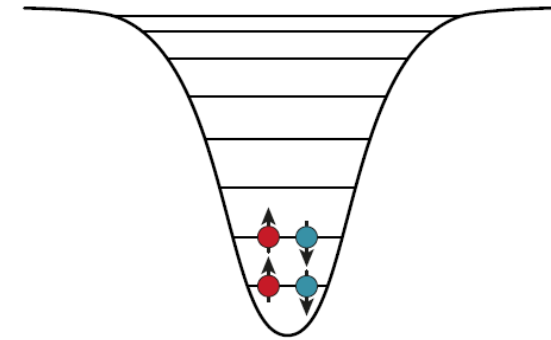
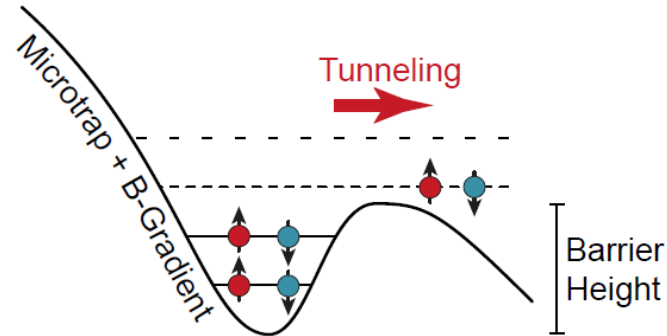
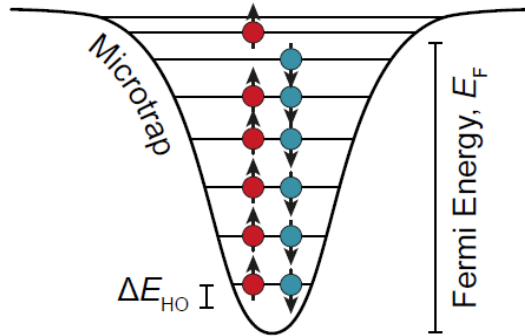
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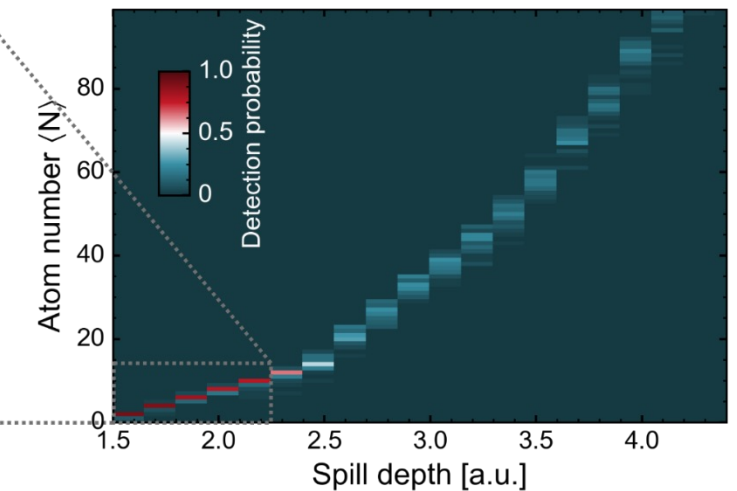
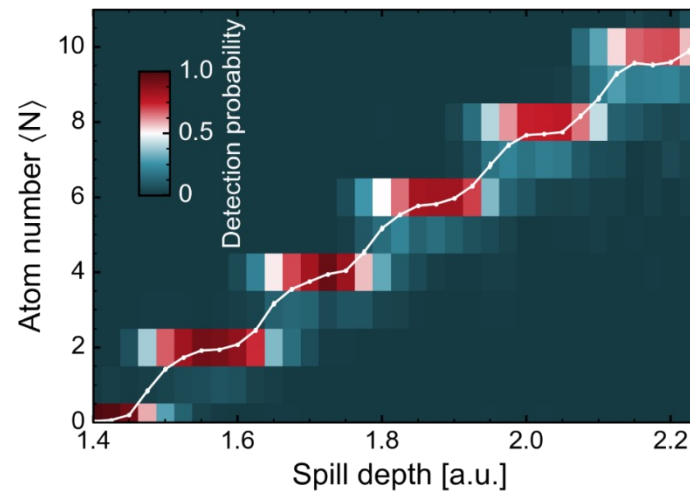
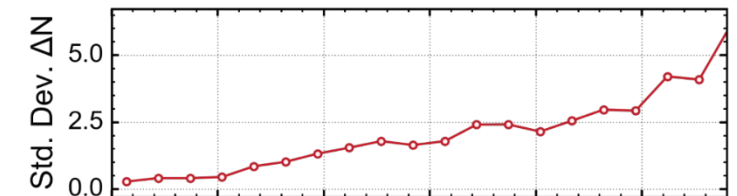
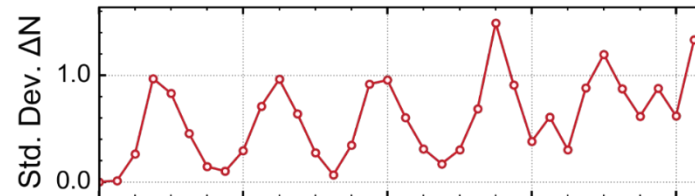
- Fermionic ${}^6\text{Li}$ atoms
→ balanced mixture of two hyperfine states
- Cigar-shaped trap
 $\omega_r \sim 52\text{kHz}$
 $\omega_r/\omega_z \sim 7$

- Interaction control
→ Feshbach resonance
- Observables:
 - Single-atom spin-resolved momentum space image
 - Spectroscopy

Deterministic preparation



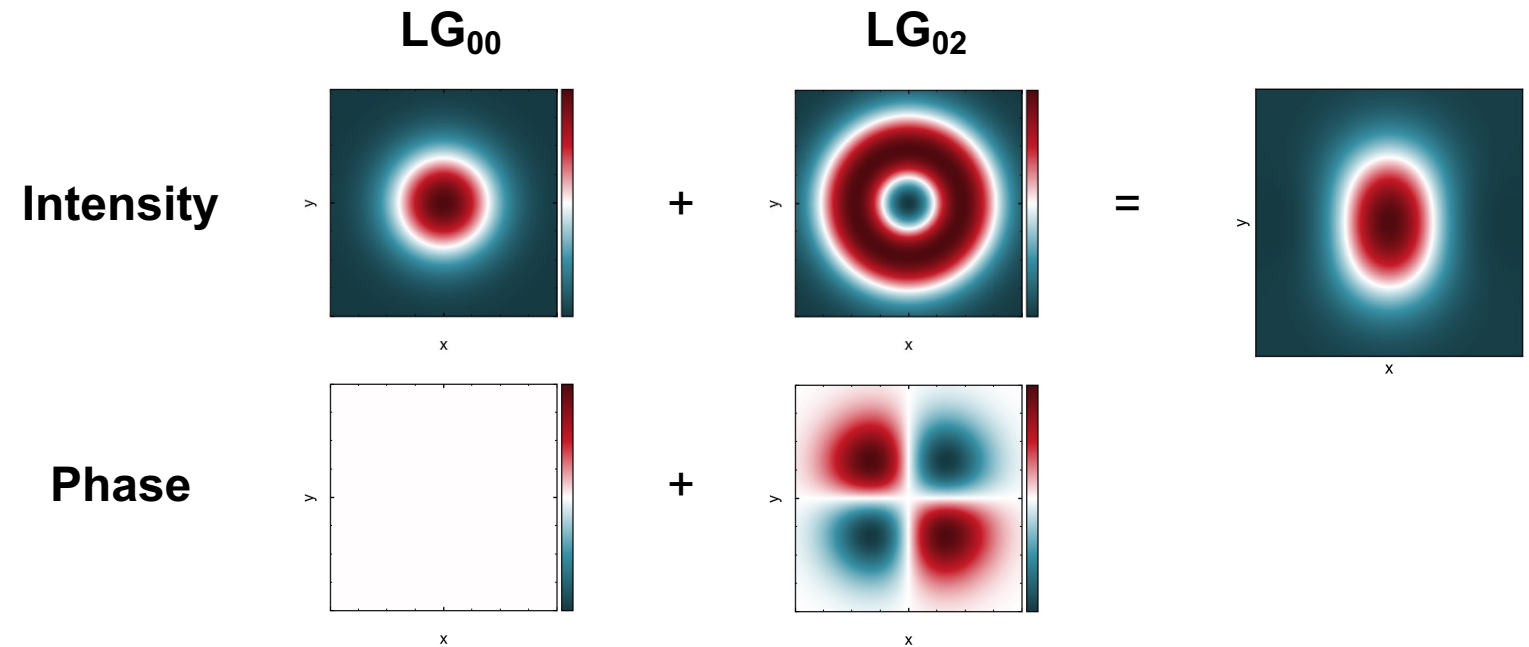
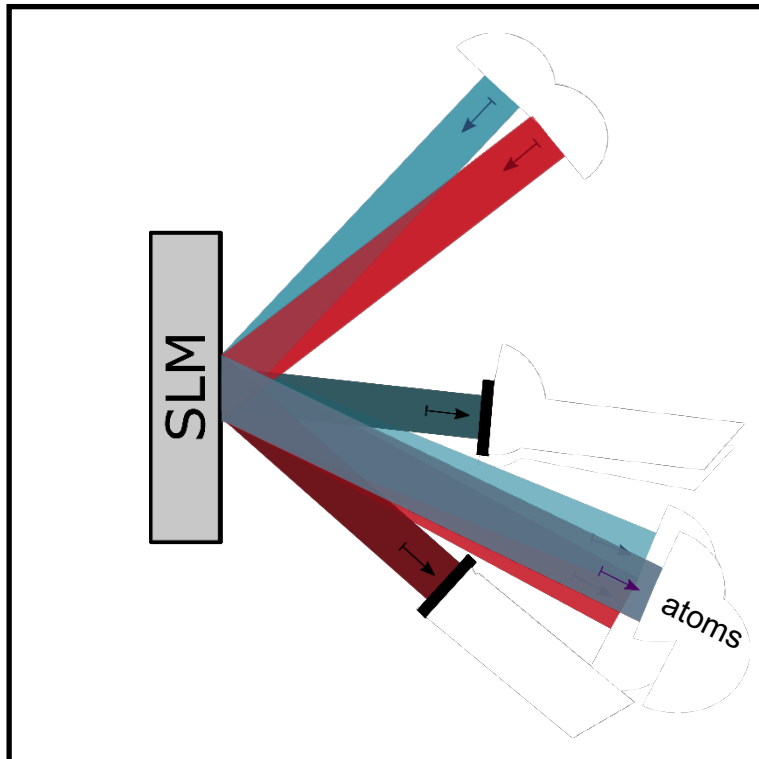
- Axial closed shell configurations for even atom numbers
- 1+1 ground state fidelity: 98%



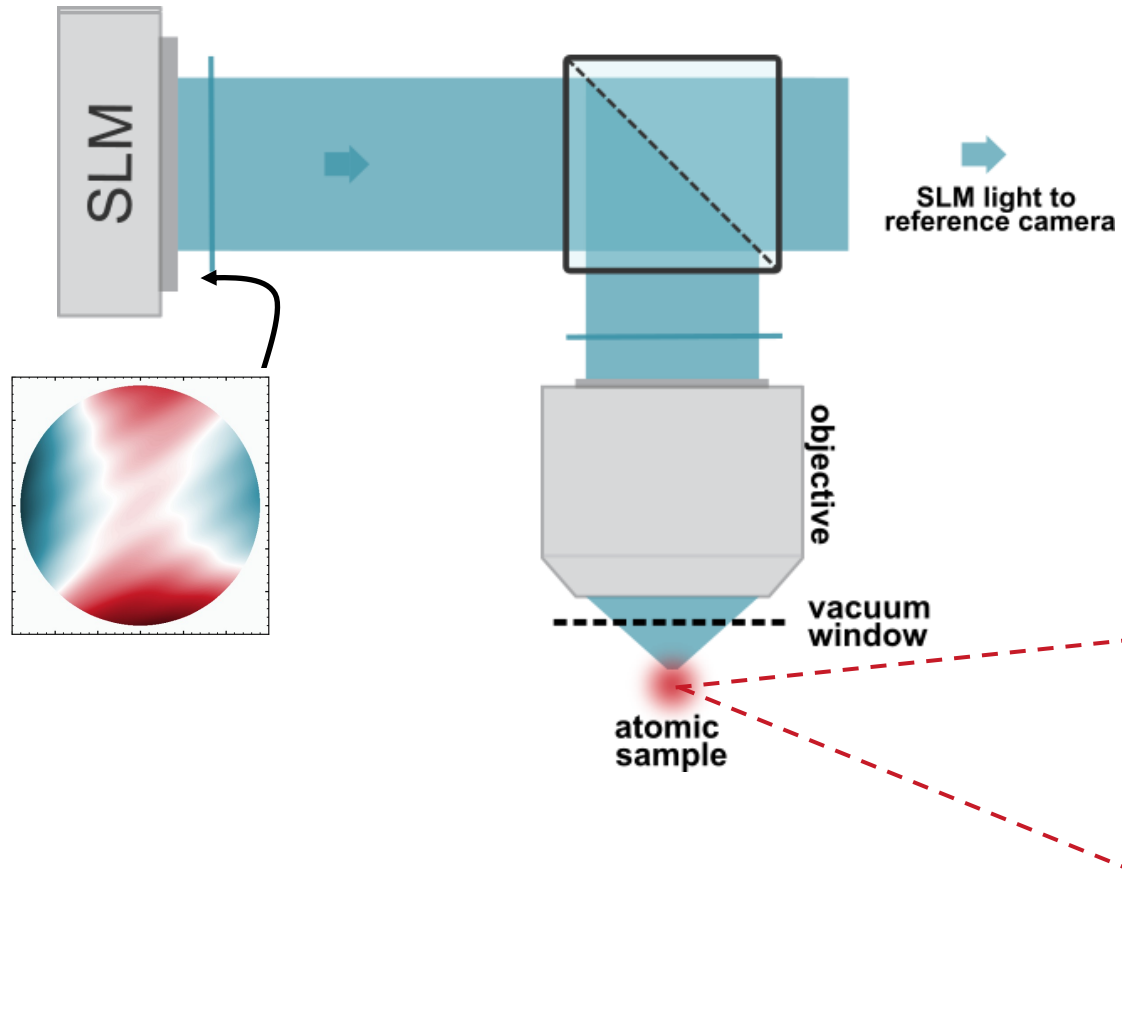
Creating a high-fidelity rotating potential: Interference of Laguerre-Gaussian beams



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Aberrations in optical Setups



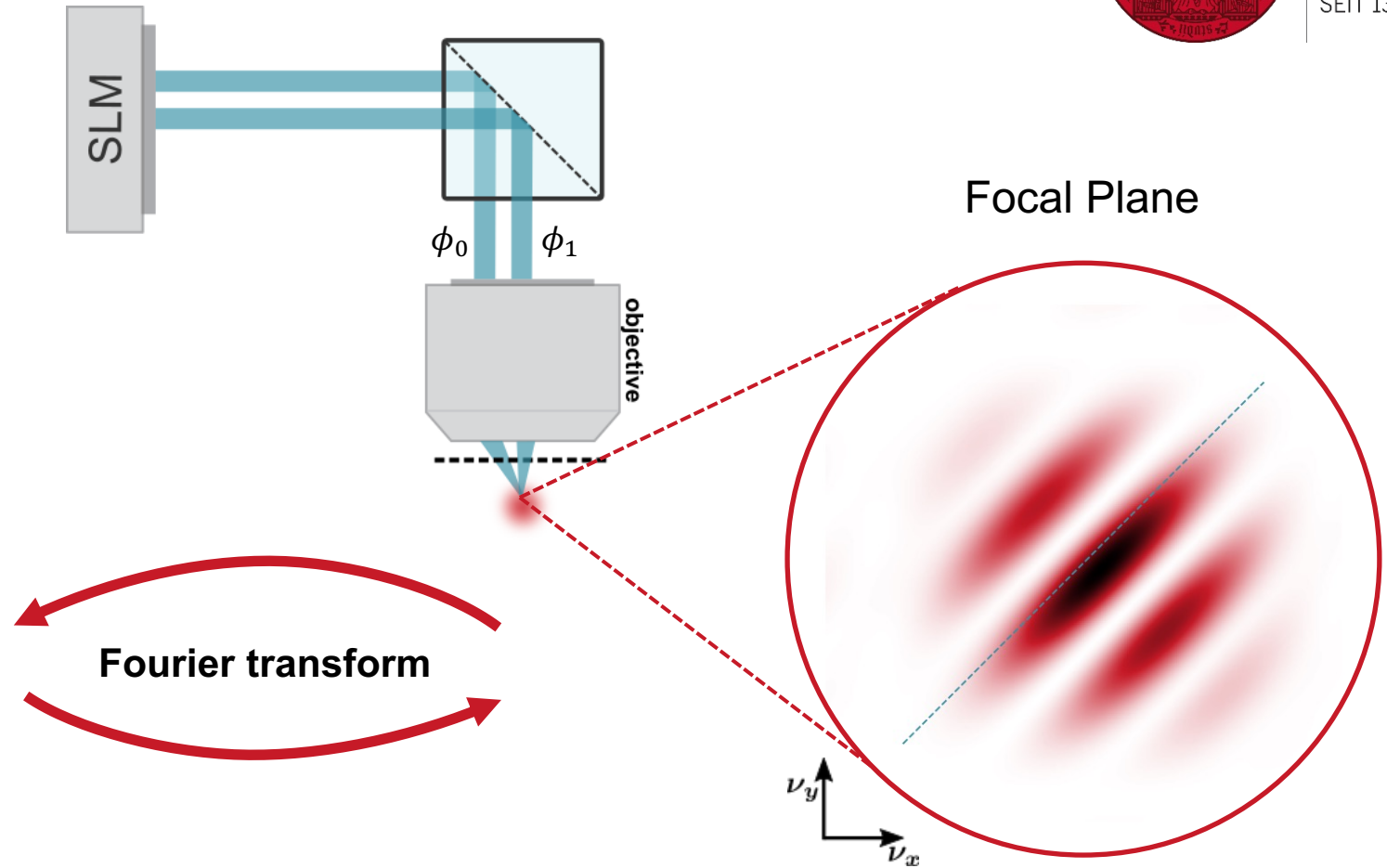
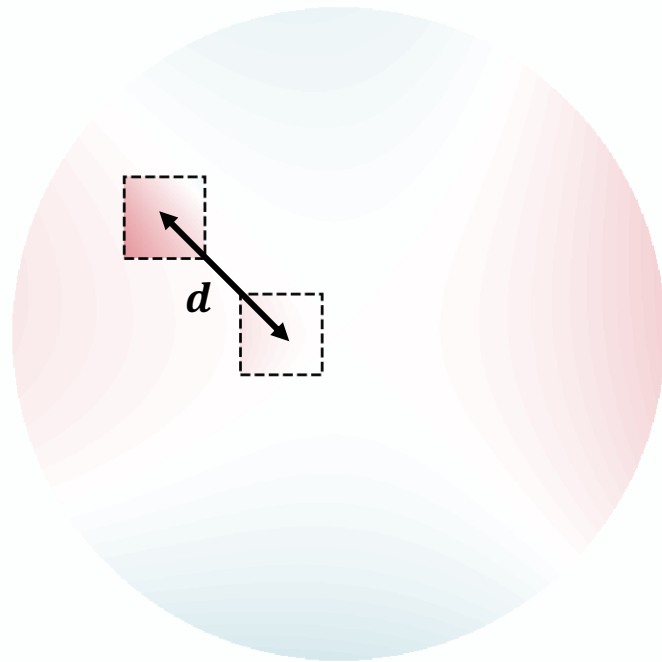
directly use atoms as
atomic wavefront-sensor

- ➔ measure aberrations where they matter
- ➔ map out inaccessible components

Measuring Aberrations



Wavefront (SLM + aberrations)

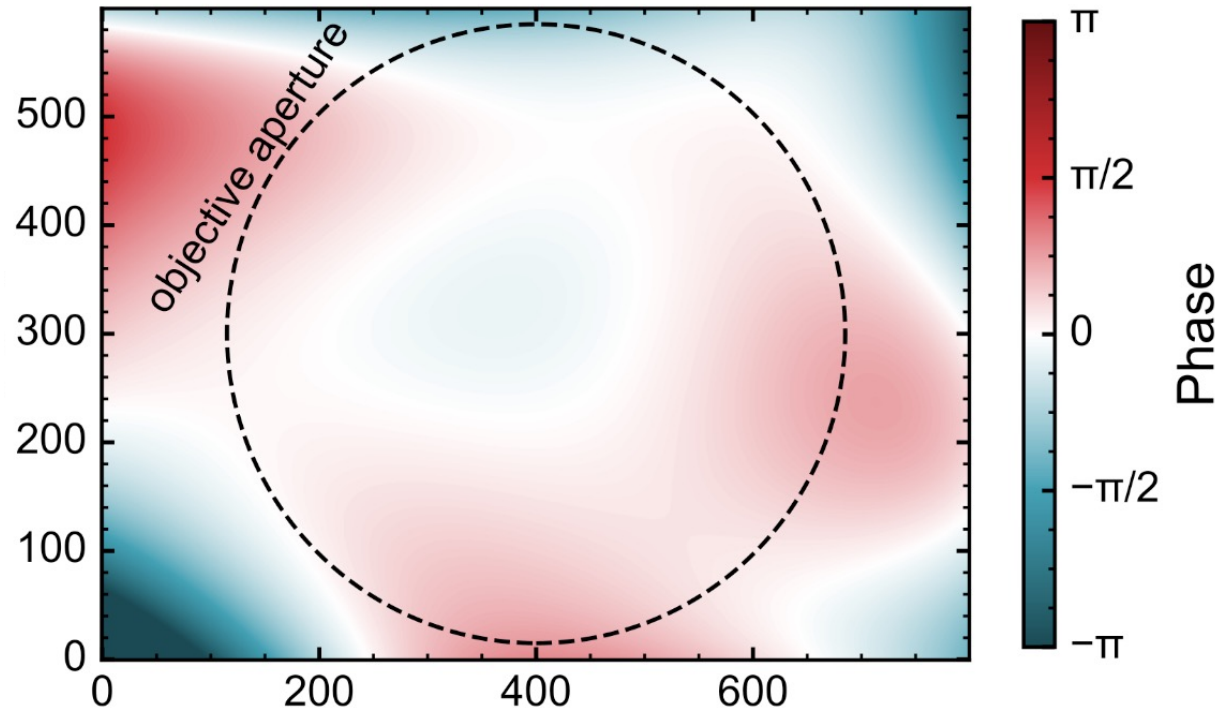


$$\sim 1 + \cos(2\pi \mathbf{d} \cdot \mathbf{v} + \Delta\phi)$$

Results (preliminary)



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benchmarking

- rms deviation $\sim \lambda/13$
- peak-to-valley $\sim \lambda/5$

Limitations

- patch size: sensitivity to spatial frequencies
- grid spacing: strength of shears limited to $(-\pi, \pi)$

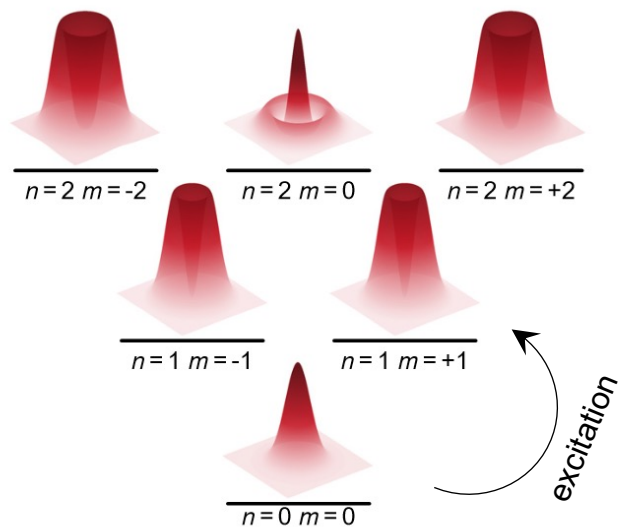
Rotation of a single Fermion



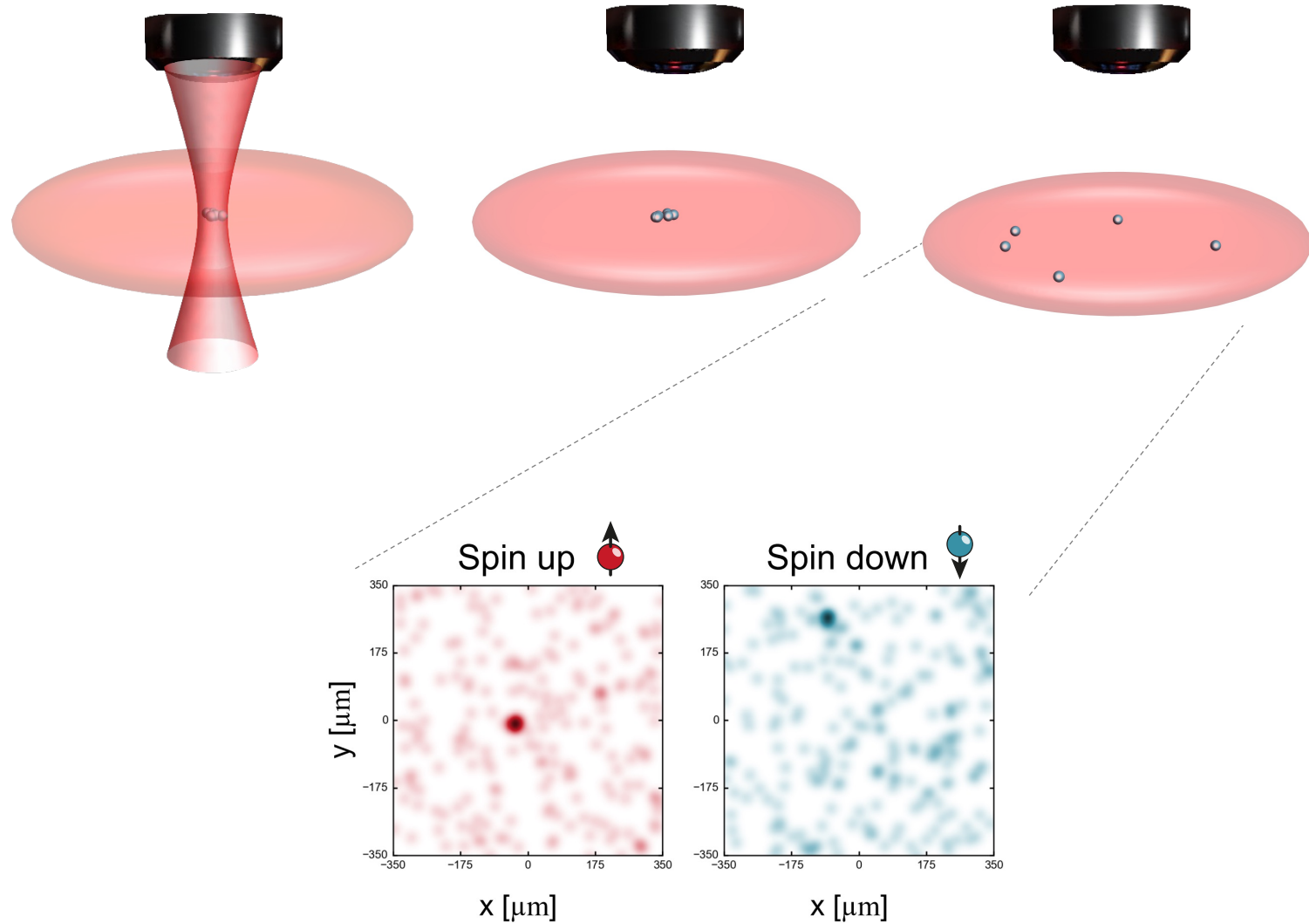
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Preparation

2D Harmonic oscillator levels



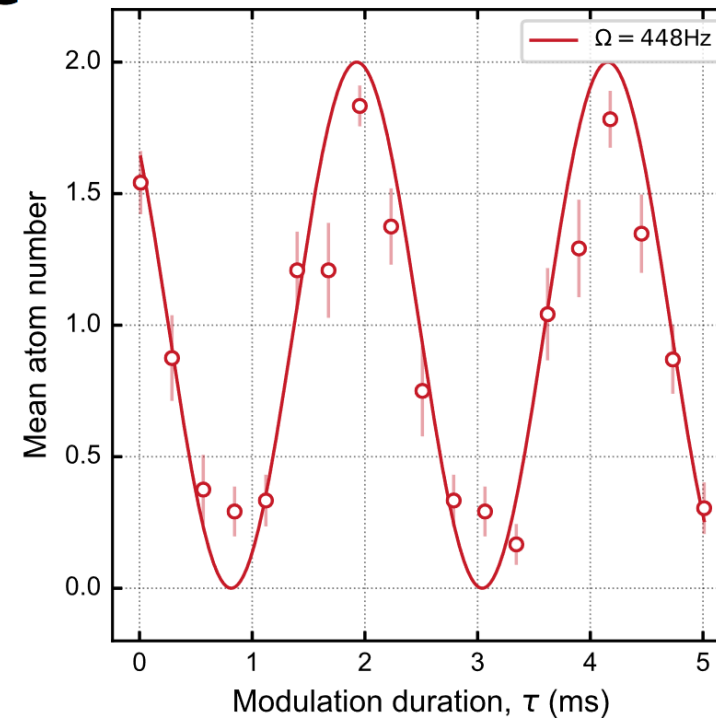
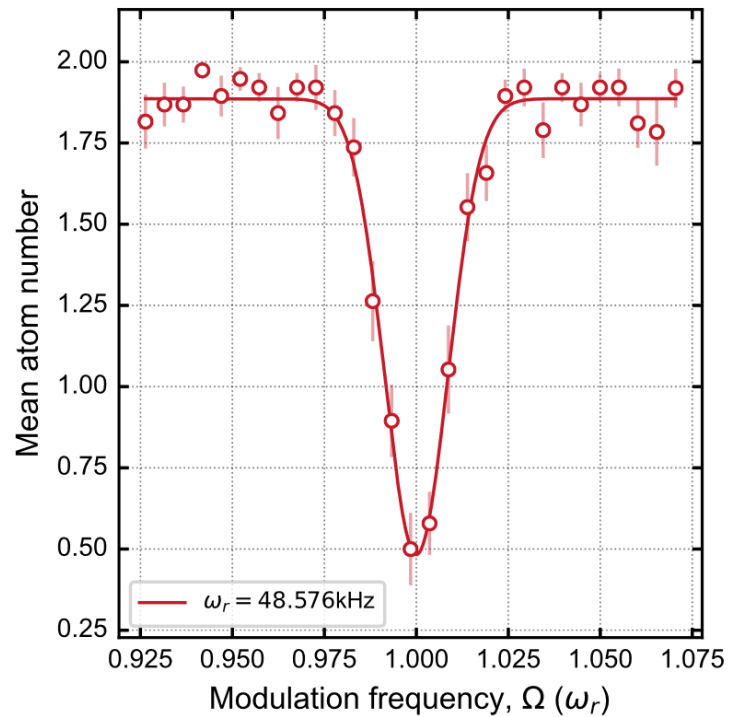
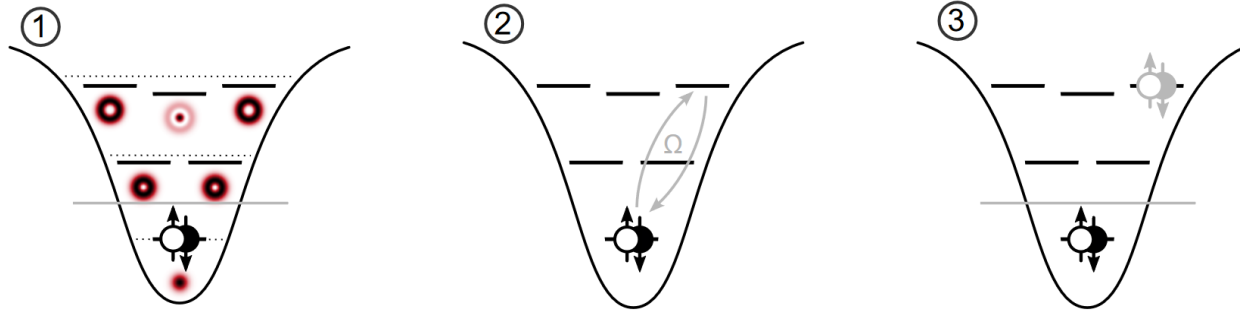
Detection



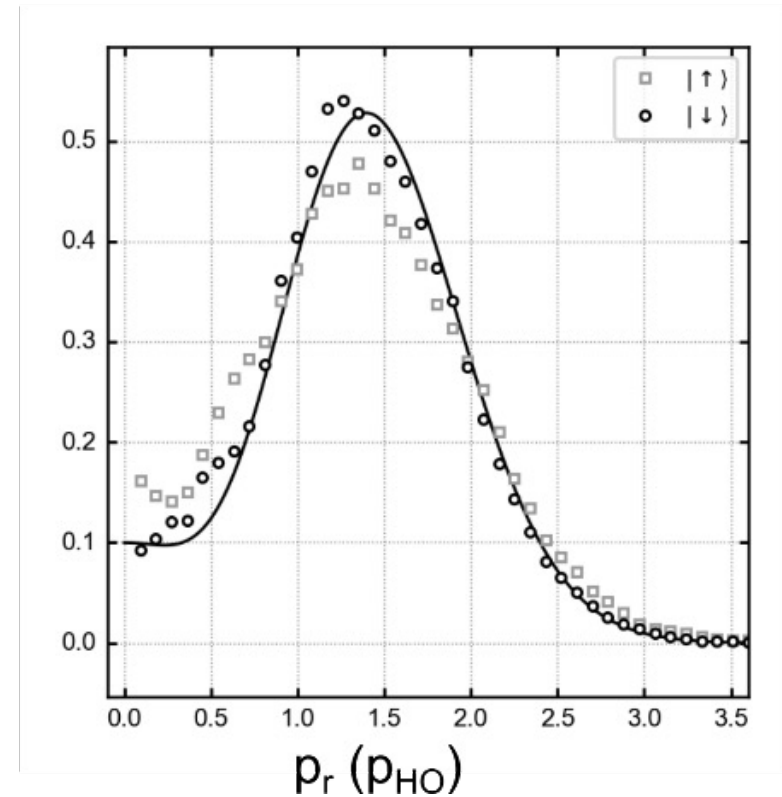
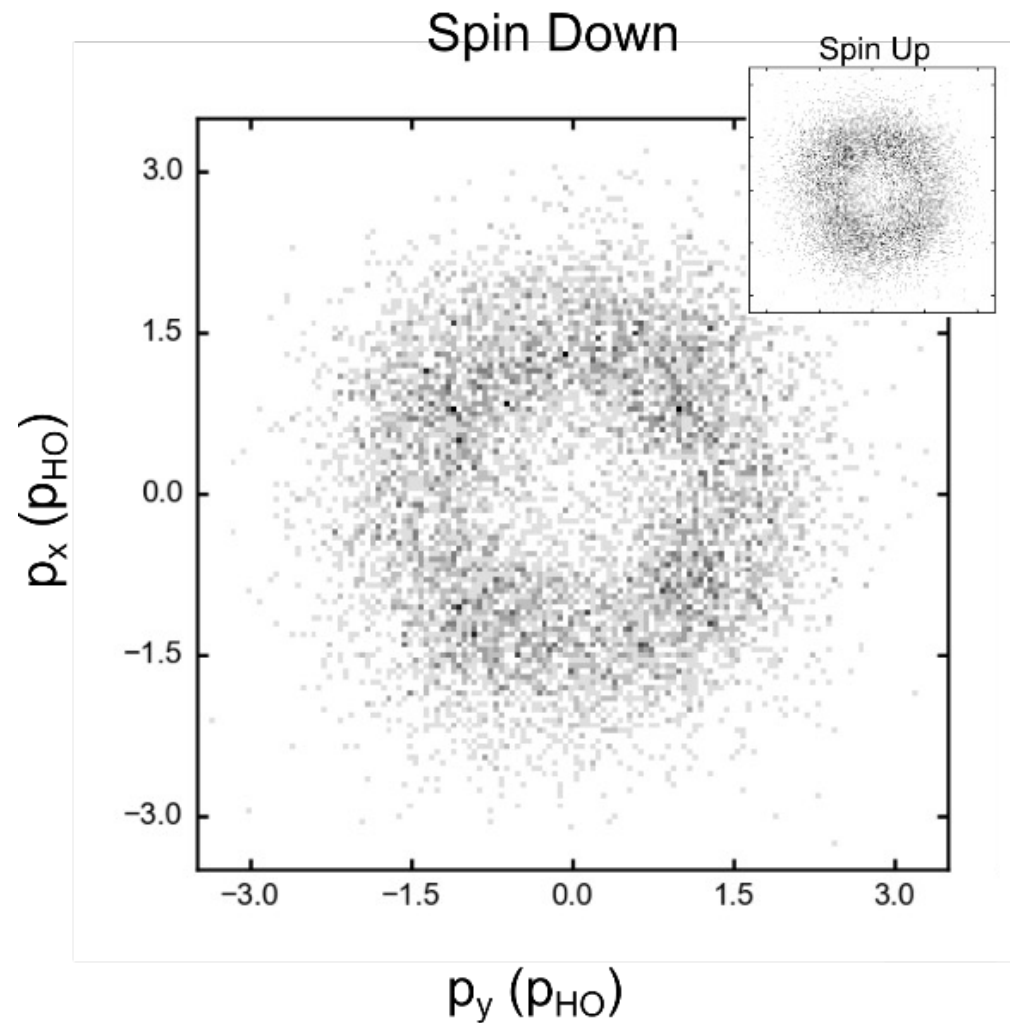
Atom loss spectroscopy



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Rotation of two non-interacting fermions

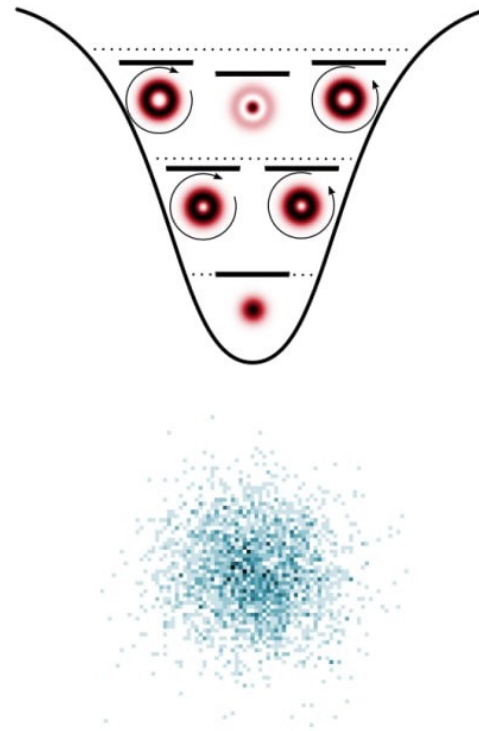


$$|\psi|^2 = 0.05 |\psi_{00}|^2 + 0.95 |\psi_{22}|^2$$

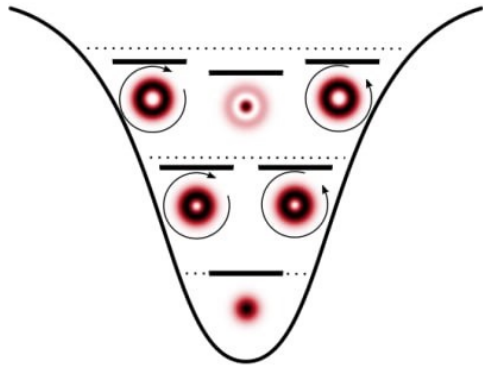
Control of the optical potential $\rightarrow$ control over motional states



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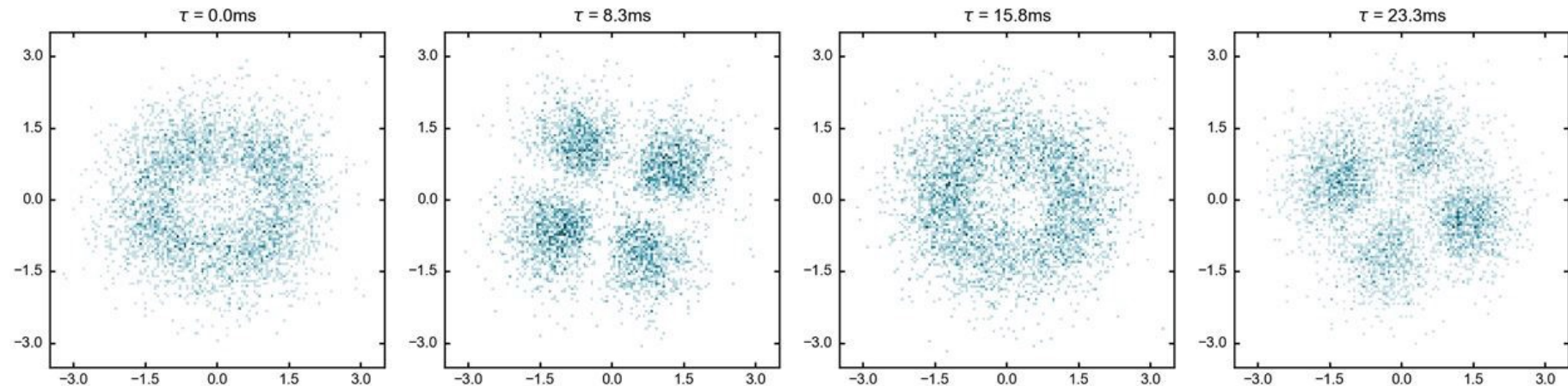
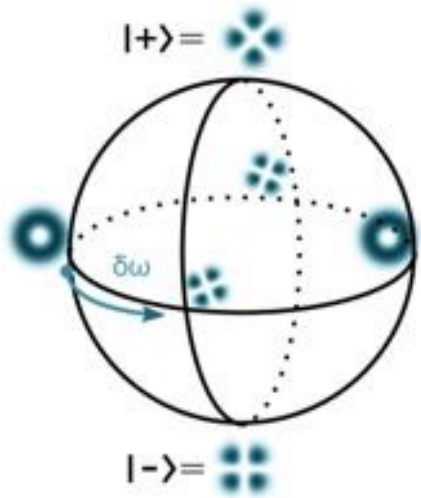
Do we know the sense of rotation?



A slight anisotropy lifts degeneracies:
Angular momentum states are no longer eigenstates!

$$\nu_r \sim 30\text{kHz}, \nu_x - \nu_y \sim 30\text{Hz}$$

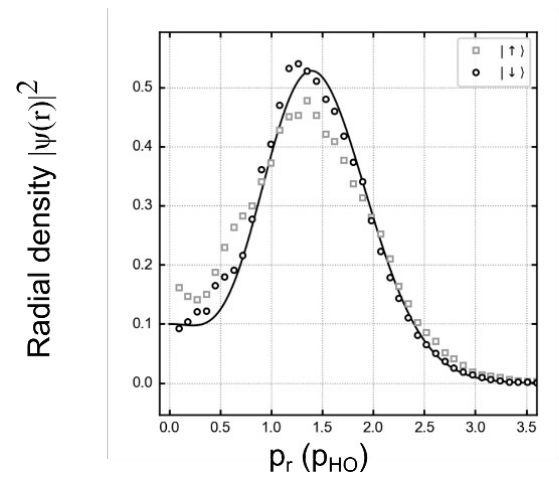
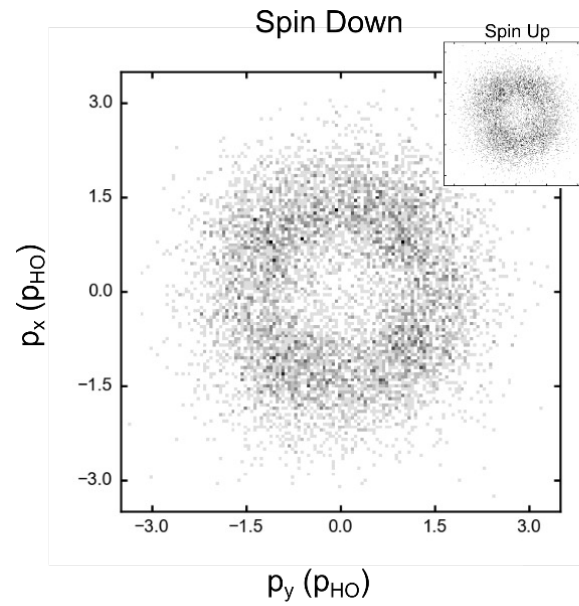
Time evolution of the rotational state:



Center of mass & relative motion



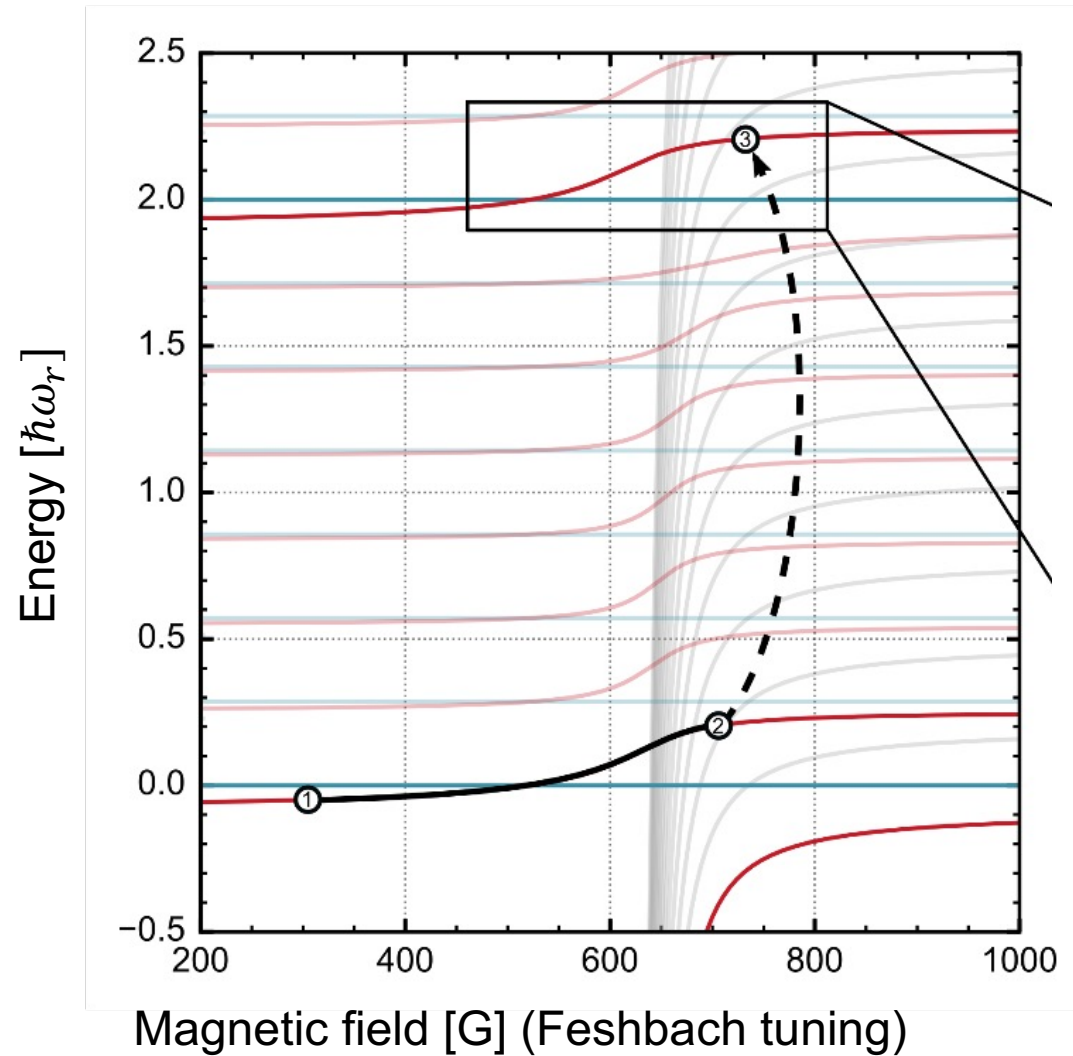
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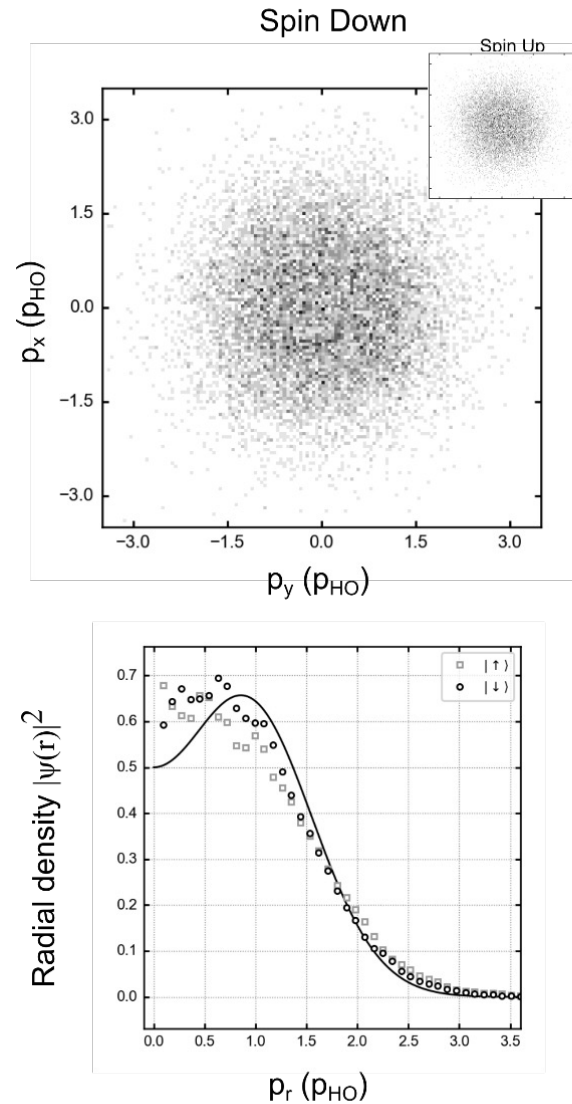
States with relative angular momentum: Laughlin states



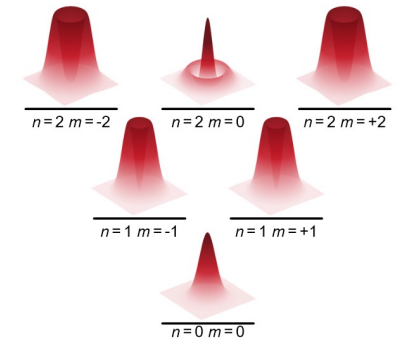
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Laughlin state

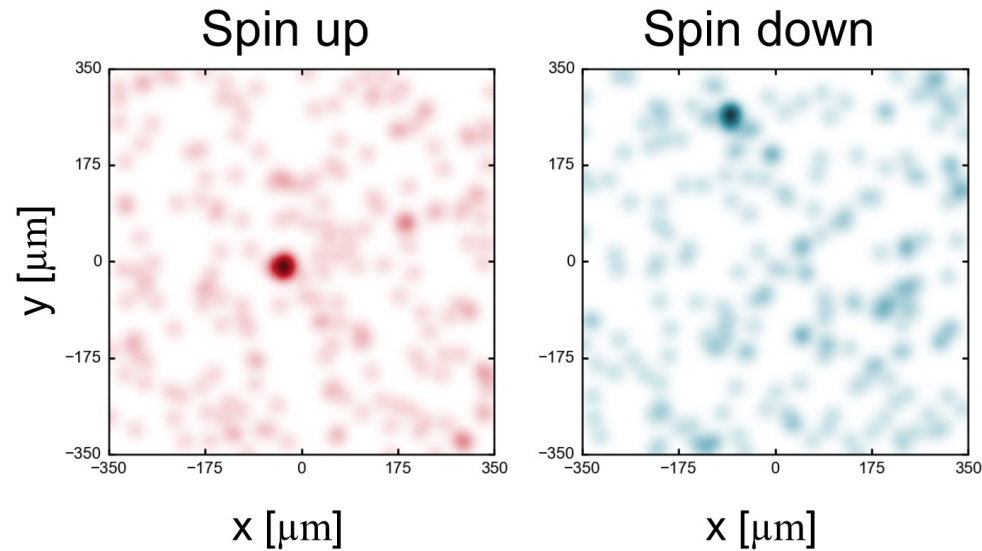


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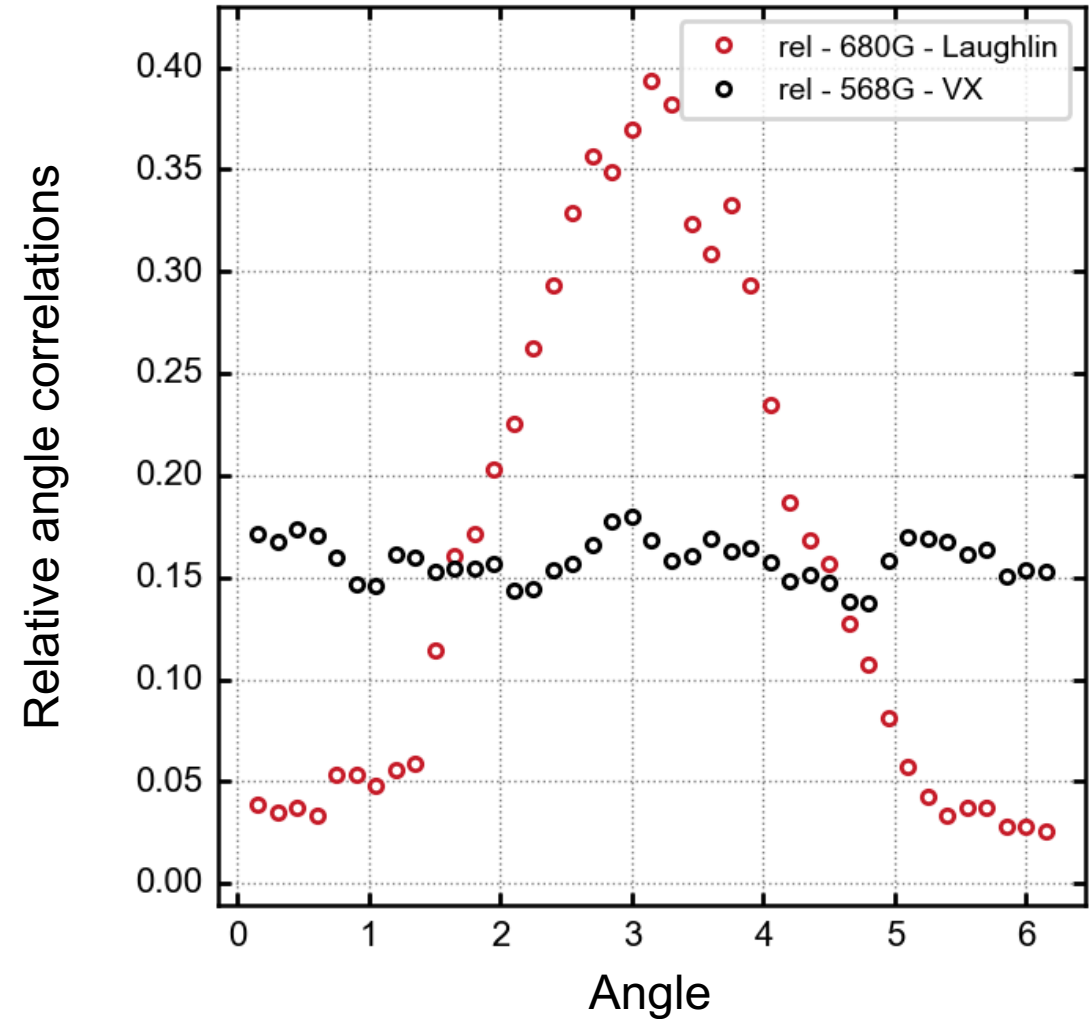


See also: Clark et al., Nature **582**, 45 (2020), Léonard et al., Nature **619**, 495 (2023)

Angular correlations

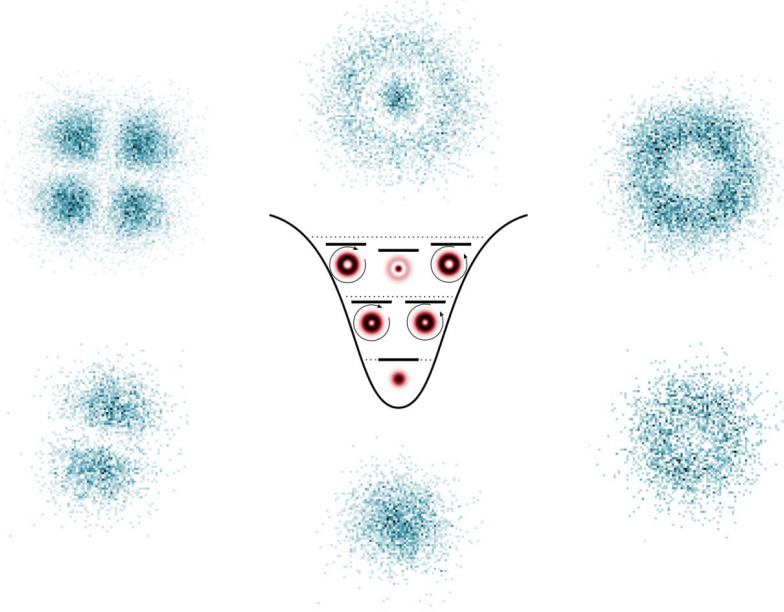


- Measure angle ϕ_1, ϕ_2
- Relative angle $\Phi = \phi_1 - \phi_2$
- $\text{Mod}(\Phi, 2\pi)$

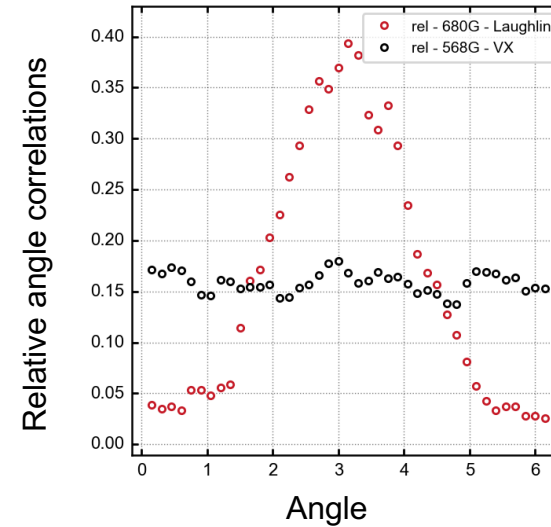
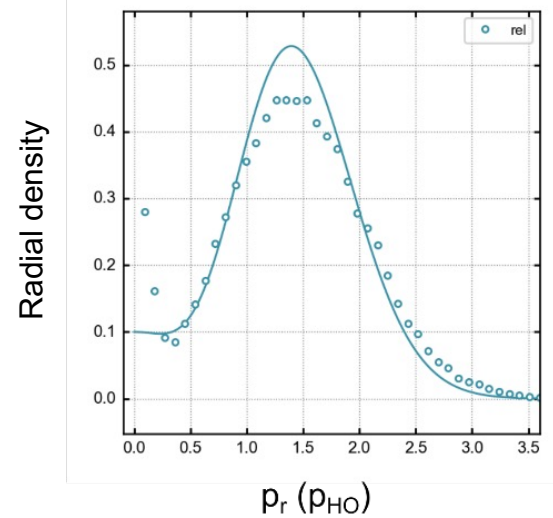
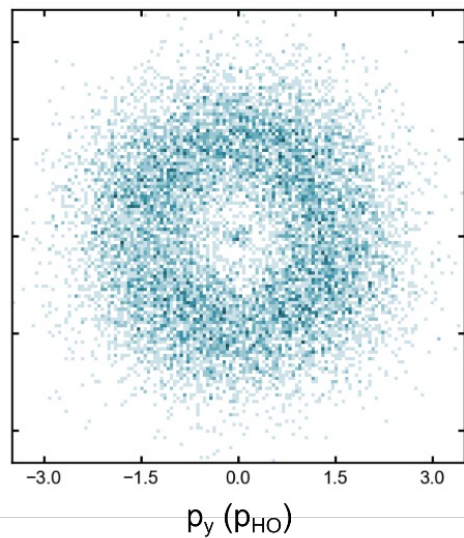


Summary rotating states

- Control of the optical potential



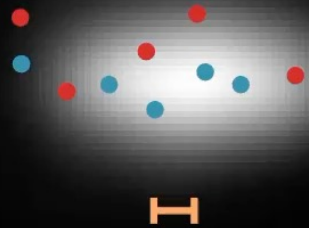
- Observation of Laughlin state



A fluid composed of 10 atoms



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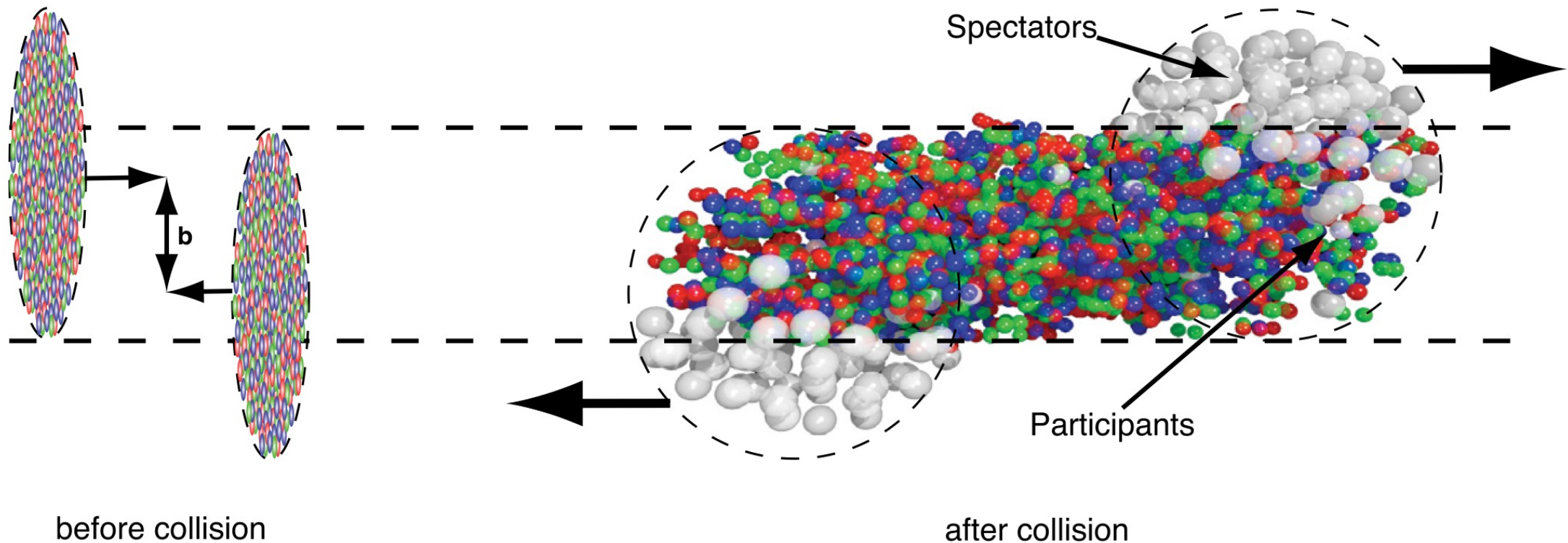
Let's look at some dynamics!



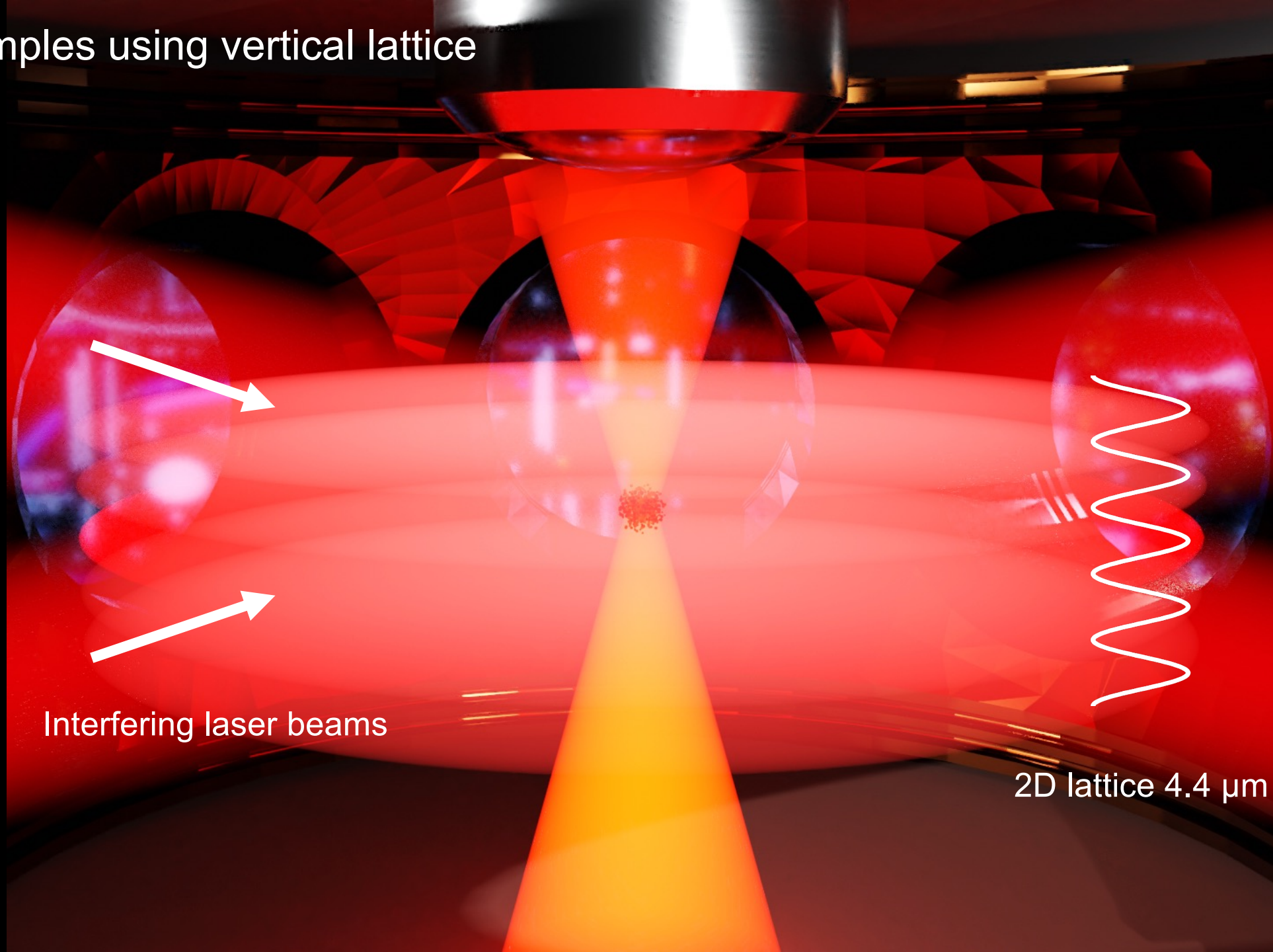
How many particles does one need to see hydrodynamics?

Inspired by nuclear physics:

Hydrodynamic „elliptic flow“ is observed in Pb-Pb collisions:



2D Samples using vertical lattice

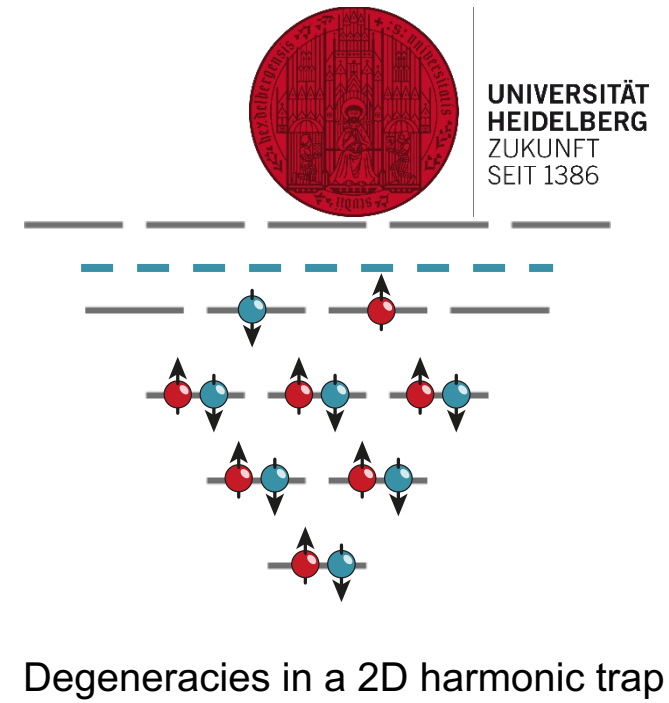
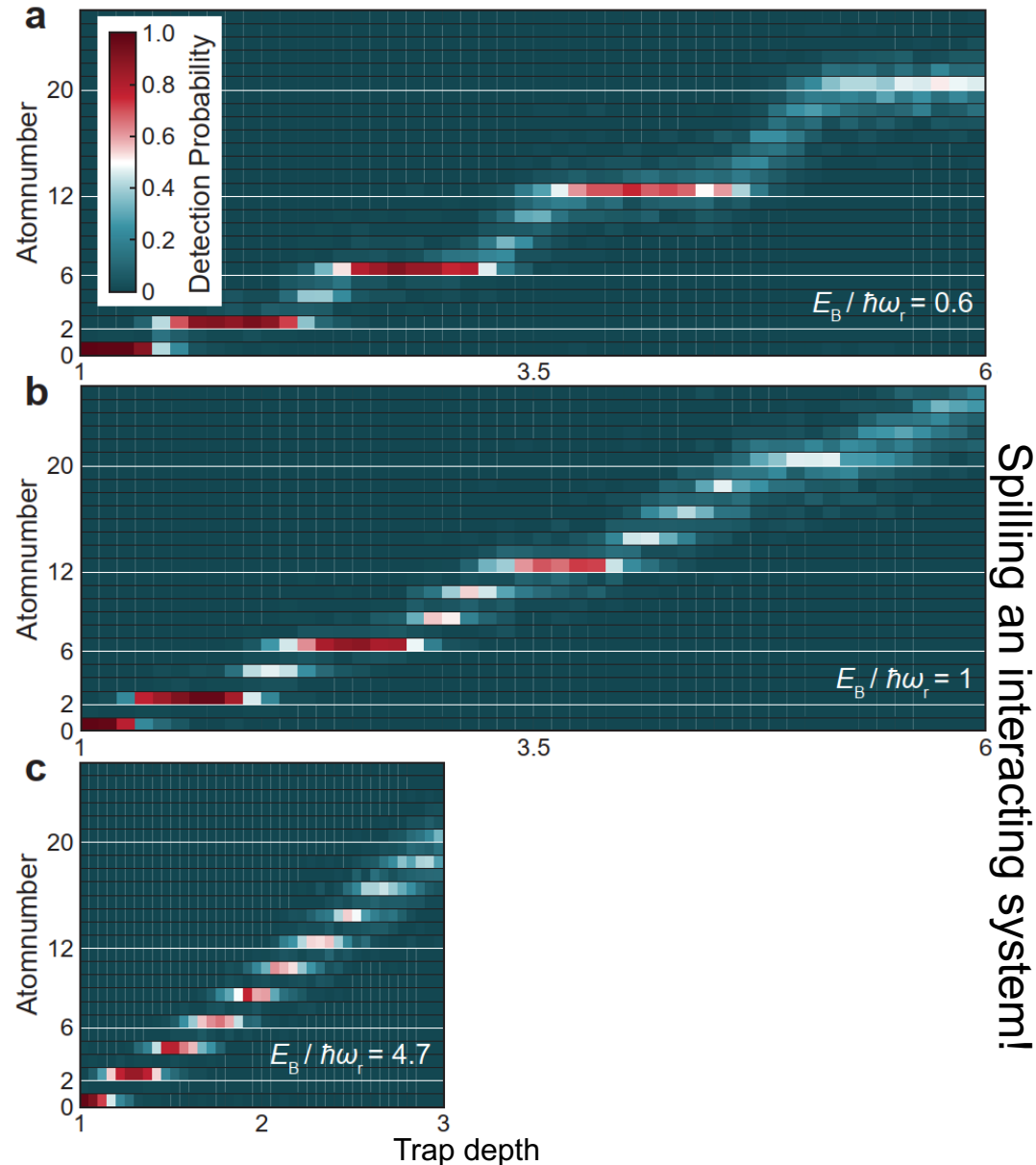
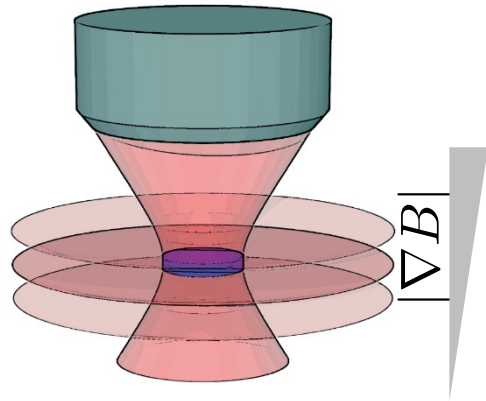


Interfering laser beams

2D lattice 4.4 μm

Controlling the particle number

Spilling particles from a 2D tra



Degeneracies in a 2D harmonic trap

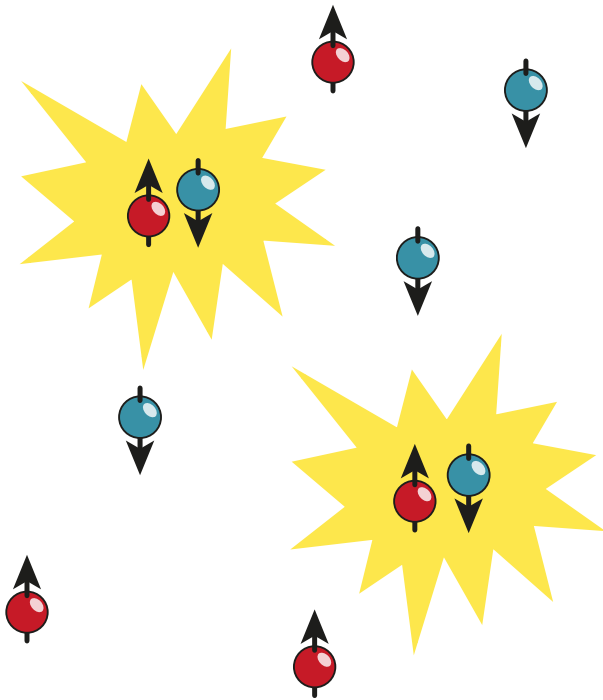


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Energy scales

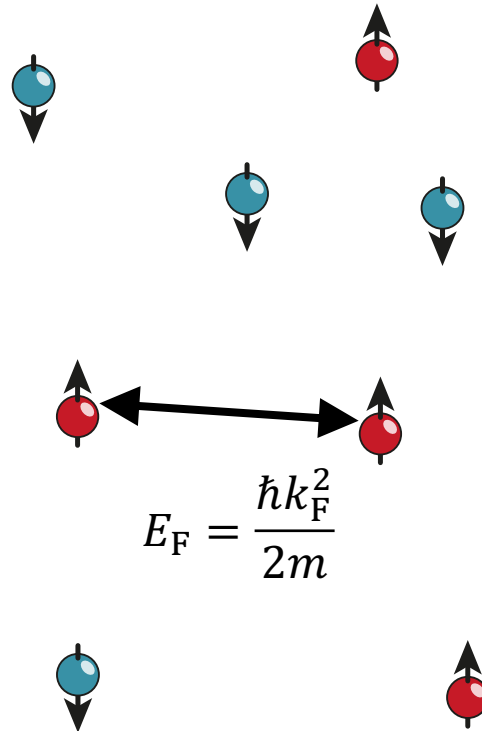


Binding Energy



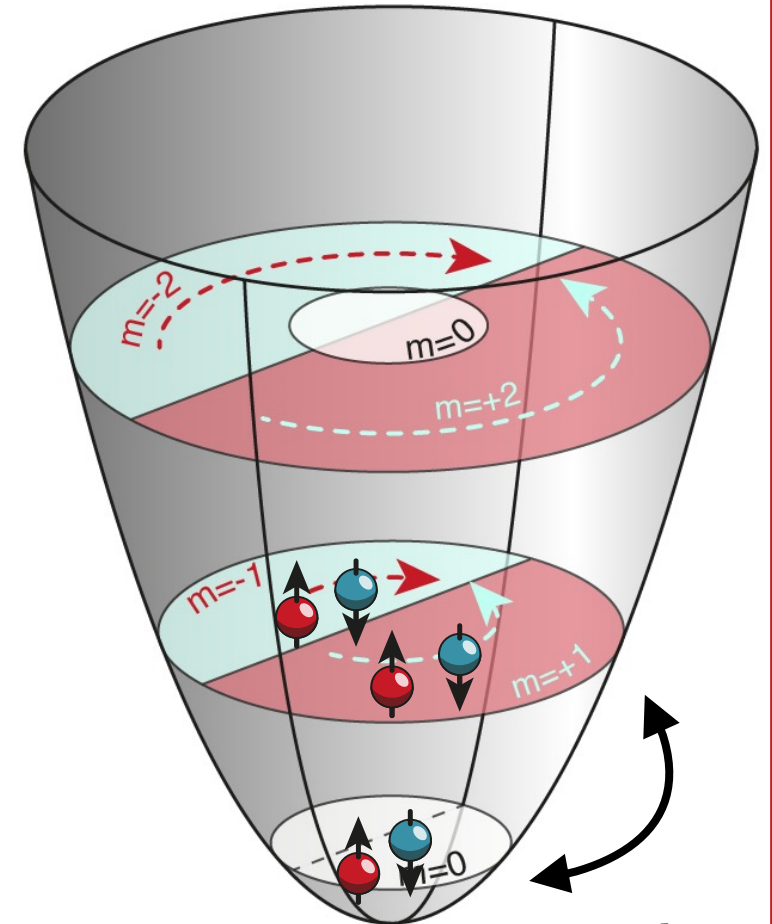
$$E_B = \frac{\hbar}{2ma_{2D}^2}$$

Fermi Energy



$$E_F = \frac{\hbar k_F^2}{2m}$$

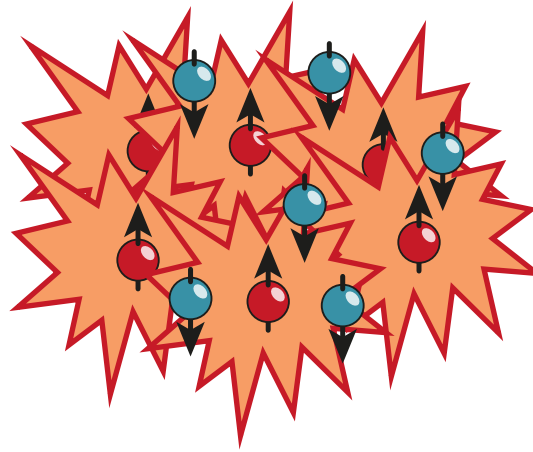
Trap Frequency



$$\Delta E = \hbar\omega_R$$

Tuning interactions

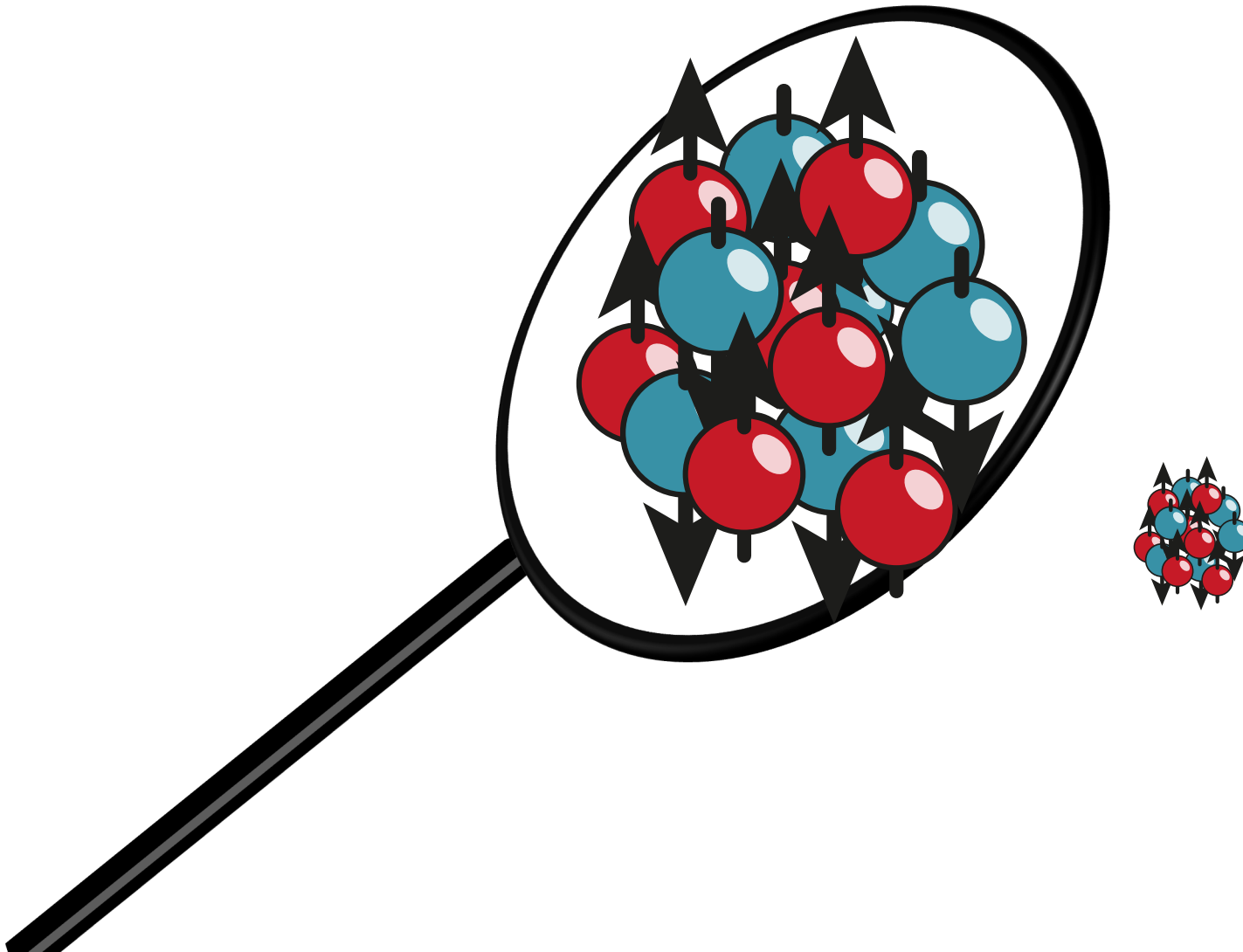
- Interactions can be tuned at will using Feshbach resonances!
- Goal: Measure their in-situ momenta
- Essential ingredient: Fast switch-off of interactions using Raman induced spin flip



Our new tool: A matterwave microscope



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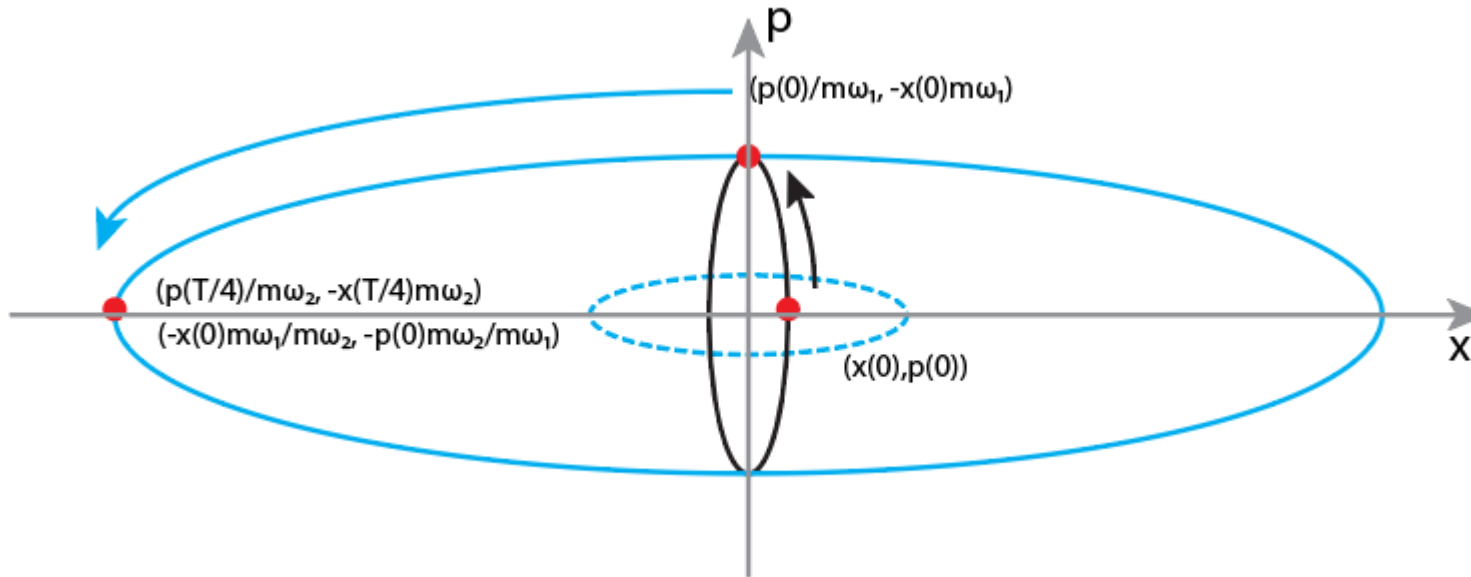
Scheme



- A $T/4$ – propagation in a harmonic trap corresponds to a Fourier transform:

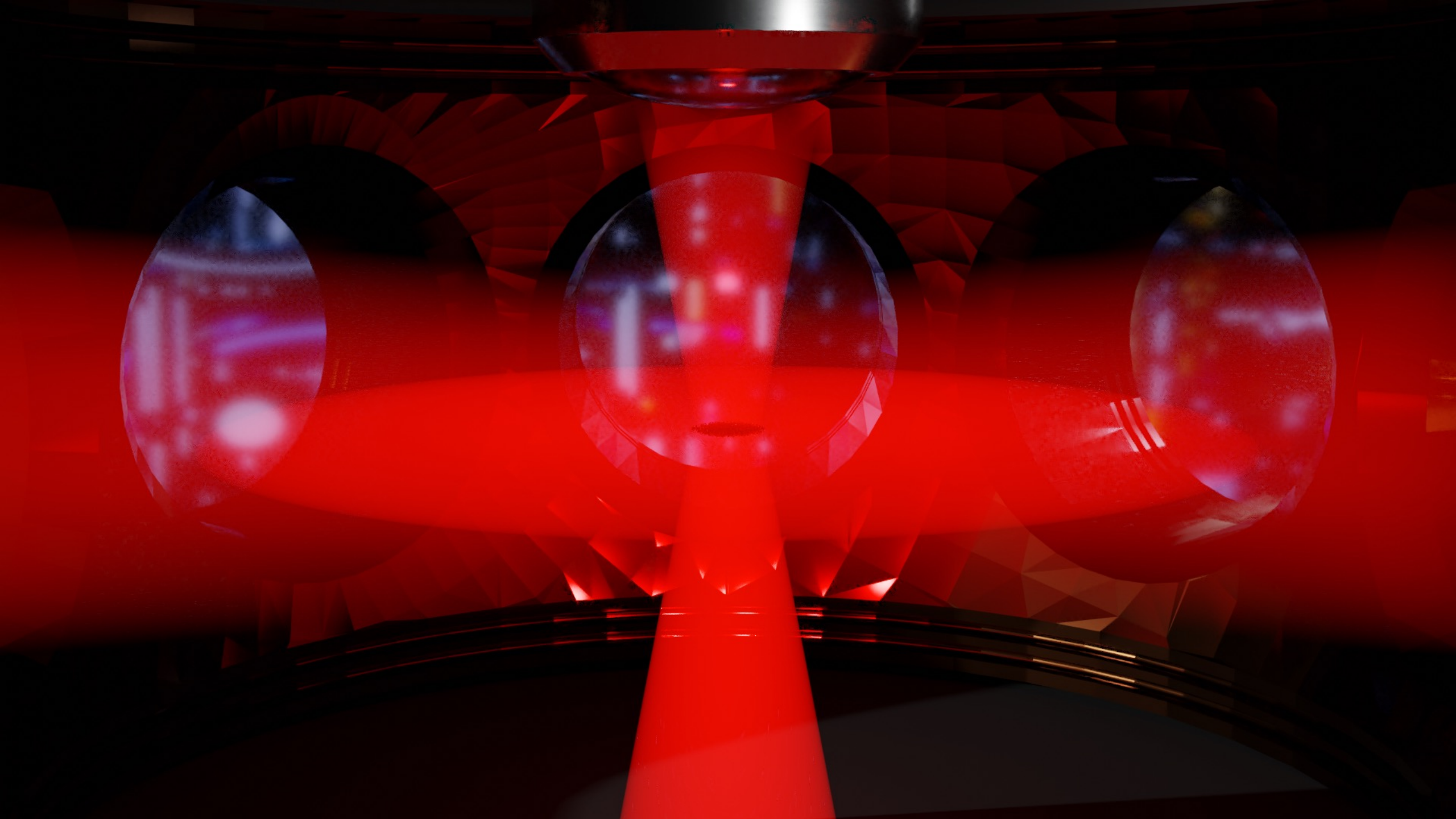
$$\begin{bmatrix} x(t) \\ p(t) \end{bmatrix} = \begin{bmatrix} \cos \omega t & \frac{1}{m\omega} \sin \omega t \\ -m\omega \sin \omega t & \cos \omega t \end{bmatrix} \begin{bmatrix} x(0) \\ p(0) \end{bmatrix}$$

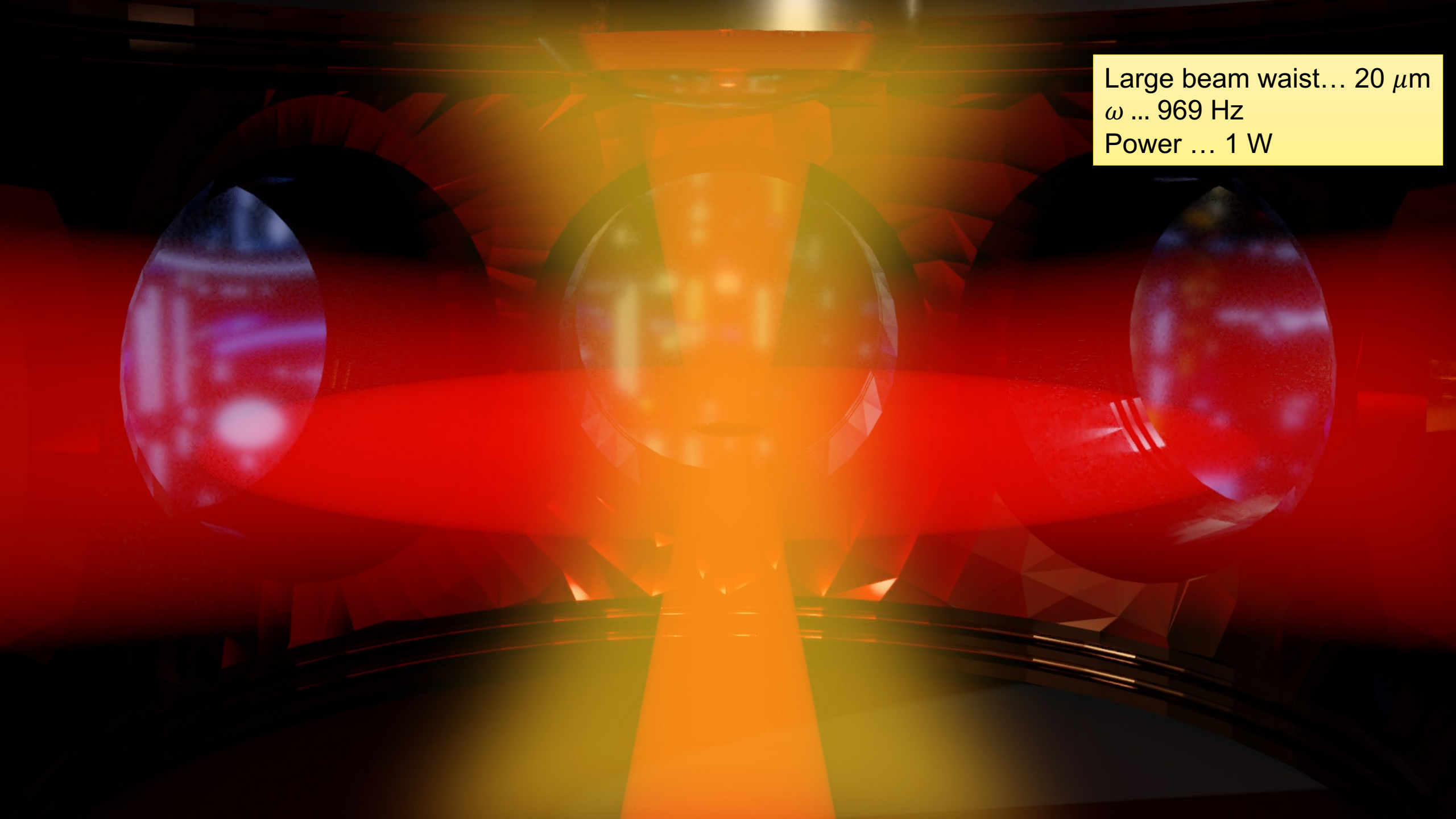
- Use two Fourier transforms with different magnification



Asteria *et al.*, *Nature* **599**, 571 (2021)
Murthy *et al.*, arXiv:1911.10824
Murthy *et al.*, *Phys. Rev. A* **90** (2014), 043611

I Svarchuk *et al.*, PRL **89**, 270404 (2002)
A. H. van Amerongen *et al.*, PRL **100**, 09040 (2008)
S. Tung *et al.*, PRL **105**, 230408 (2010)
T. Jacqmin *et al.*, PRA **86**, 043626 (2012)





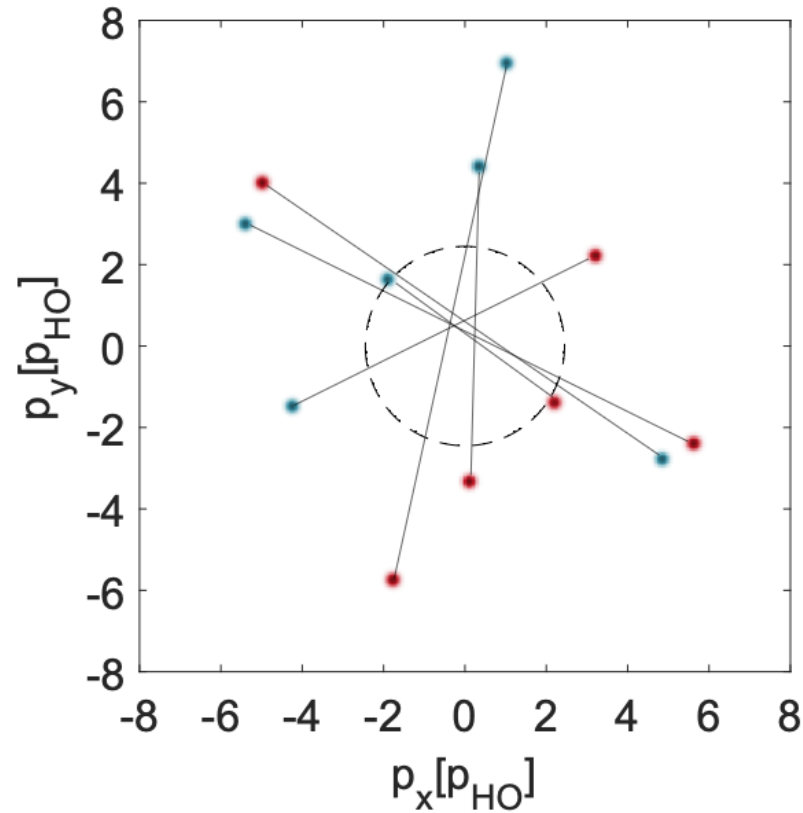
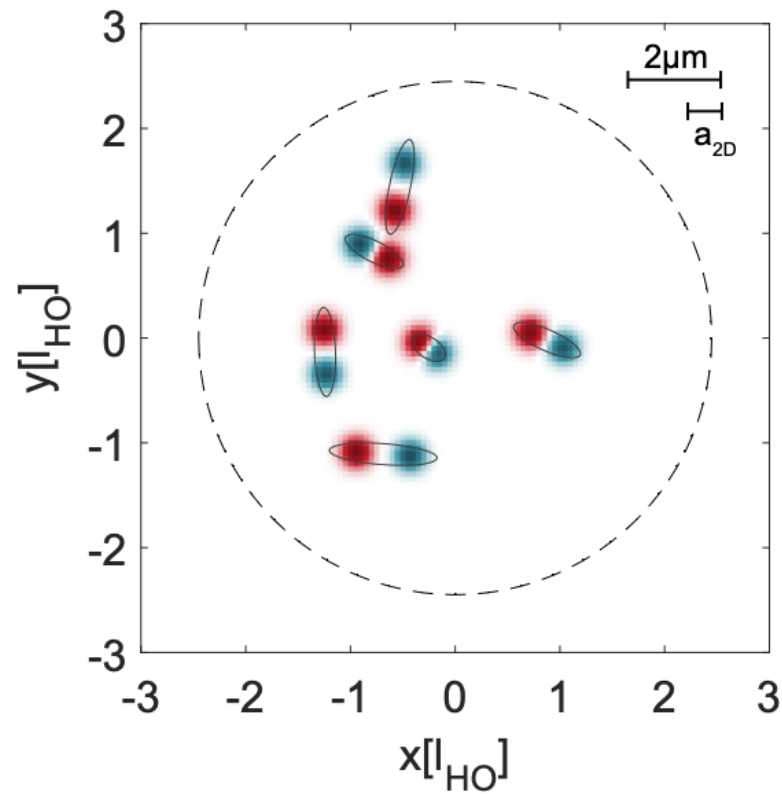
Large beam waist... 20 μm
 ω ... 969 Hz
Power ... 1 W

We now have a matterwave microscope!



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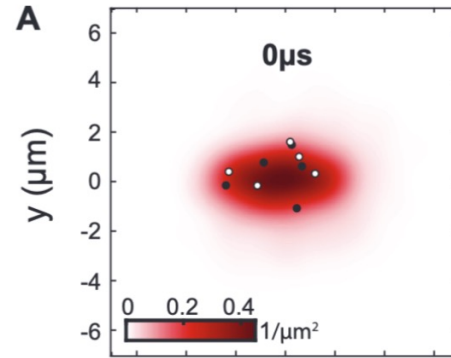
Imaging of molecules in real space



- Magnification about 50x
- Sufficient to resolve all relevant length scales for our systems

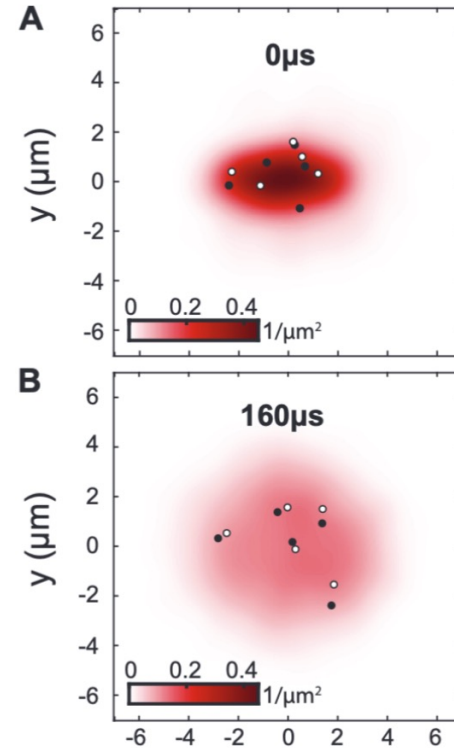
Creating a model system for elliptic flow:

- prepare an elliptic system,
- release it from the trap
- and wait ...



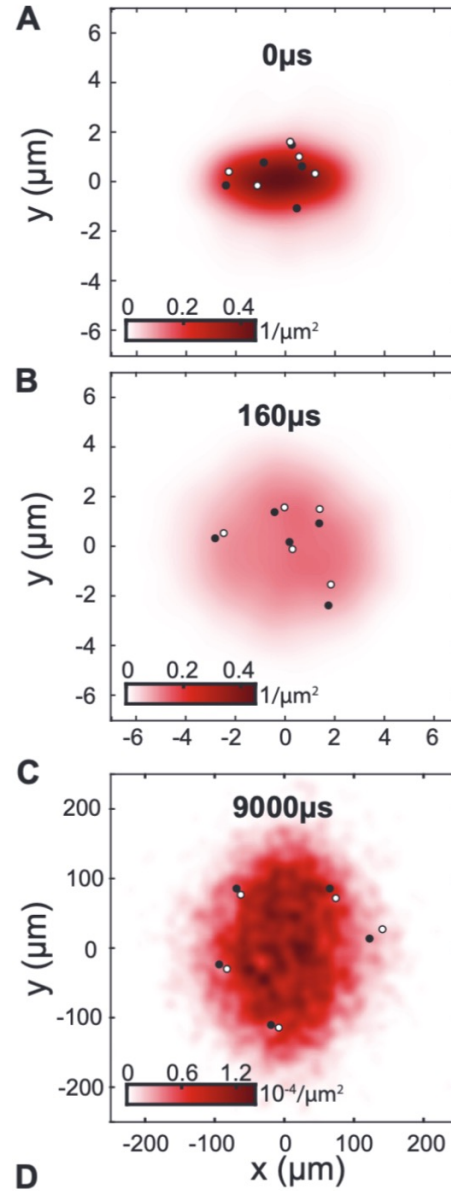
Creating a model system for elliptic flow:

- prepare an elliptic system,
- release it from the trap
- and wait ...
- The cloud becomes round



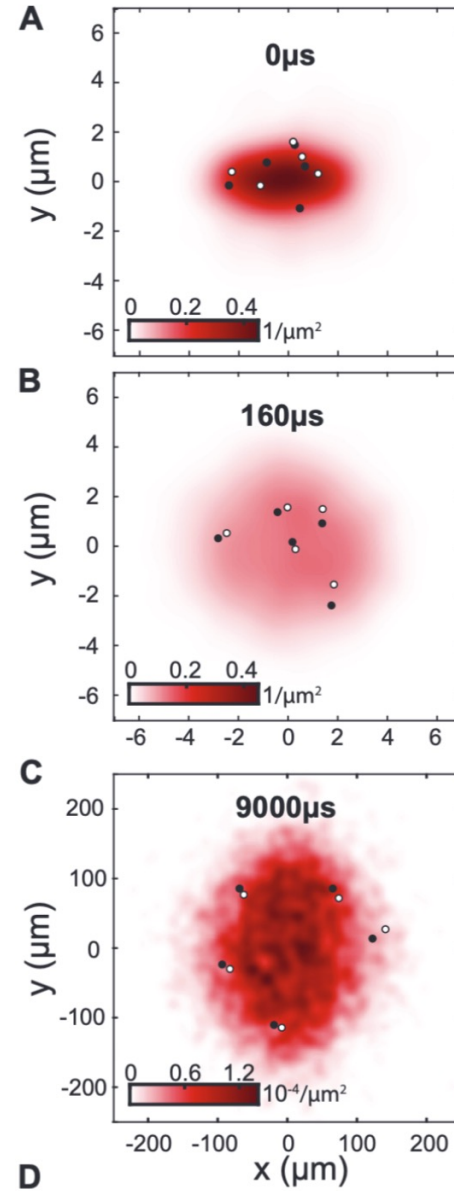
Creating a model system for elliptic flow:

- prepare an elliptic system,
- release it from the trap
- and wait ...
- The cloud becomes round ...
- ... and inverts!



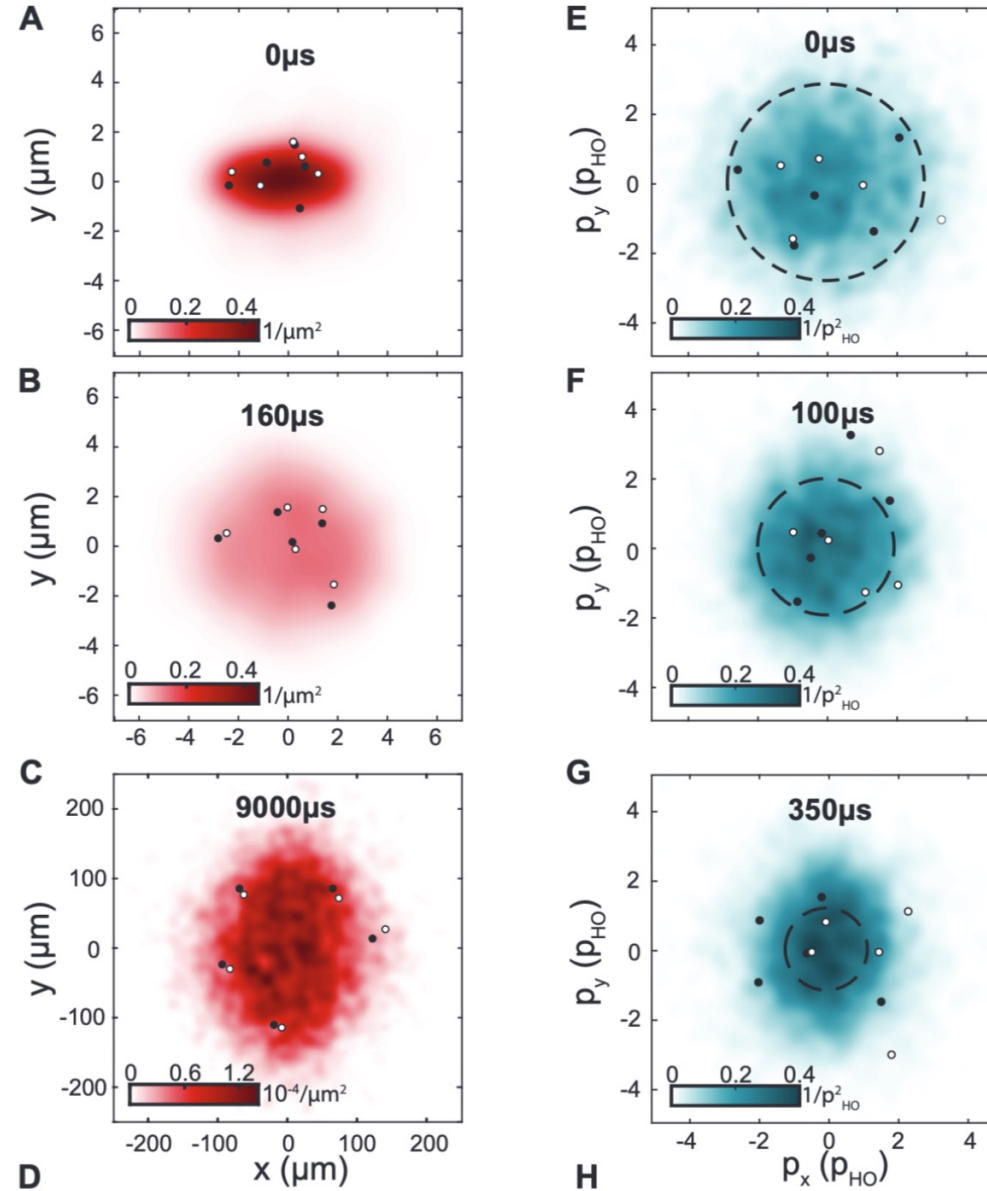
Creating a model system for elliptic flow:

- prepare an elliptic system,
- release it from the trap
- and wait ...
- The cloud becomes round ...
- ... and inverts!
- At the same time: Molecules are formed!

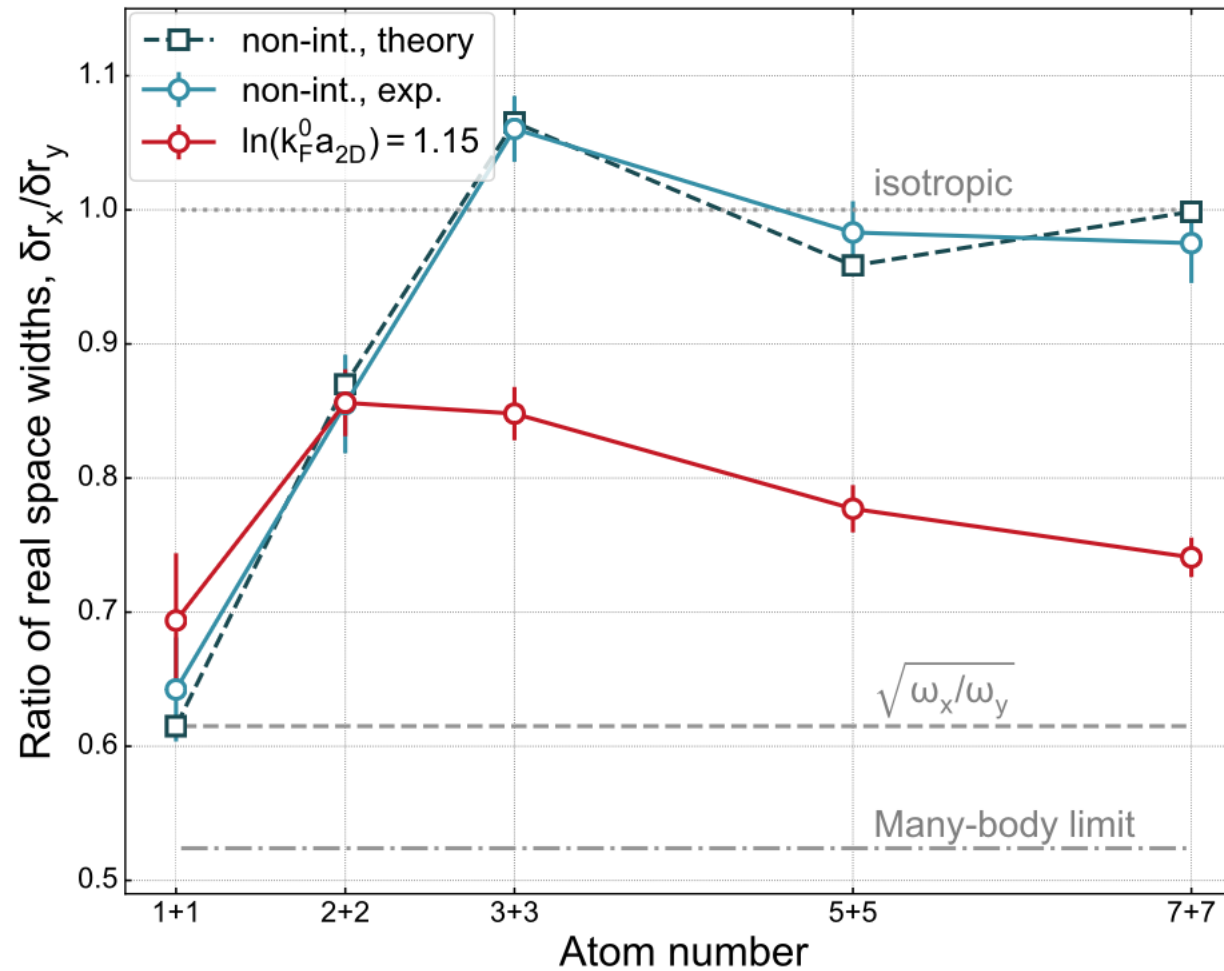


We can also observe the evolution of momenta

- prepare an elliptic system,
- release it from the trap
- and wait ...
- The cloud becomes round ...
- ... and inverts!
- at the same time:
molecules are formed!



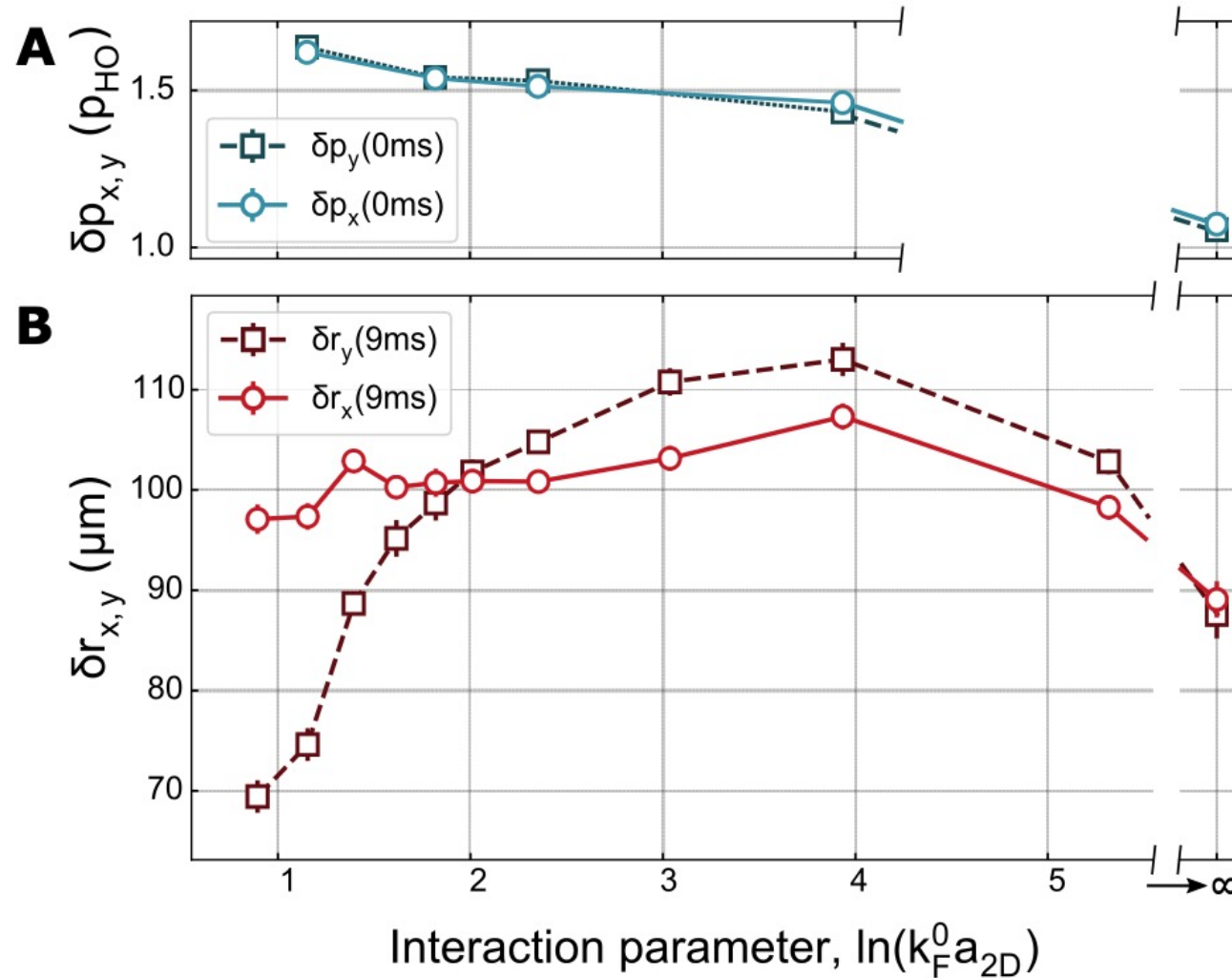
Emergence of hydrodynamic behavior



Dependence on interaction strength



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We have a lot of questions



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What do we associate with hydrodynamics?

A system described by

- equation of state: Density determined by (local) density, temperature
- Velocity field: define (local) velocity

What we observe:

Redistribution of momenta leading to deformation of the system consistent with „elliptic flow“

Can we sort out a contribution from nonlocal entanglement in the system?

→ The formation of pairs during expansion is a very strong indicator

Thank you for your attention!



Want to join?
jochim@uni-heidelberg.de



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CLUSTER OF
EXCELLENCE

Center for
Quantum
Dynamics

