

Thermonuclear supernovae

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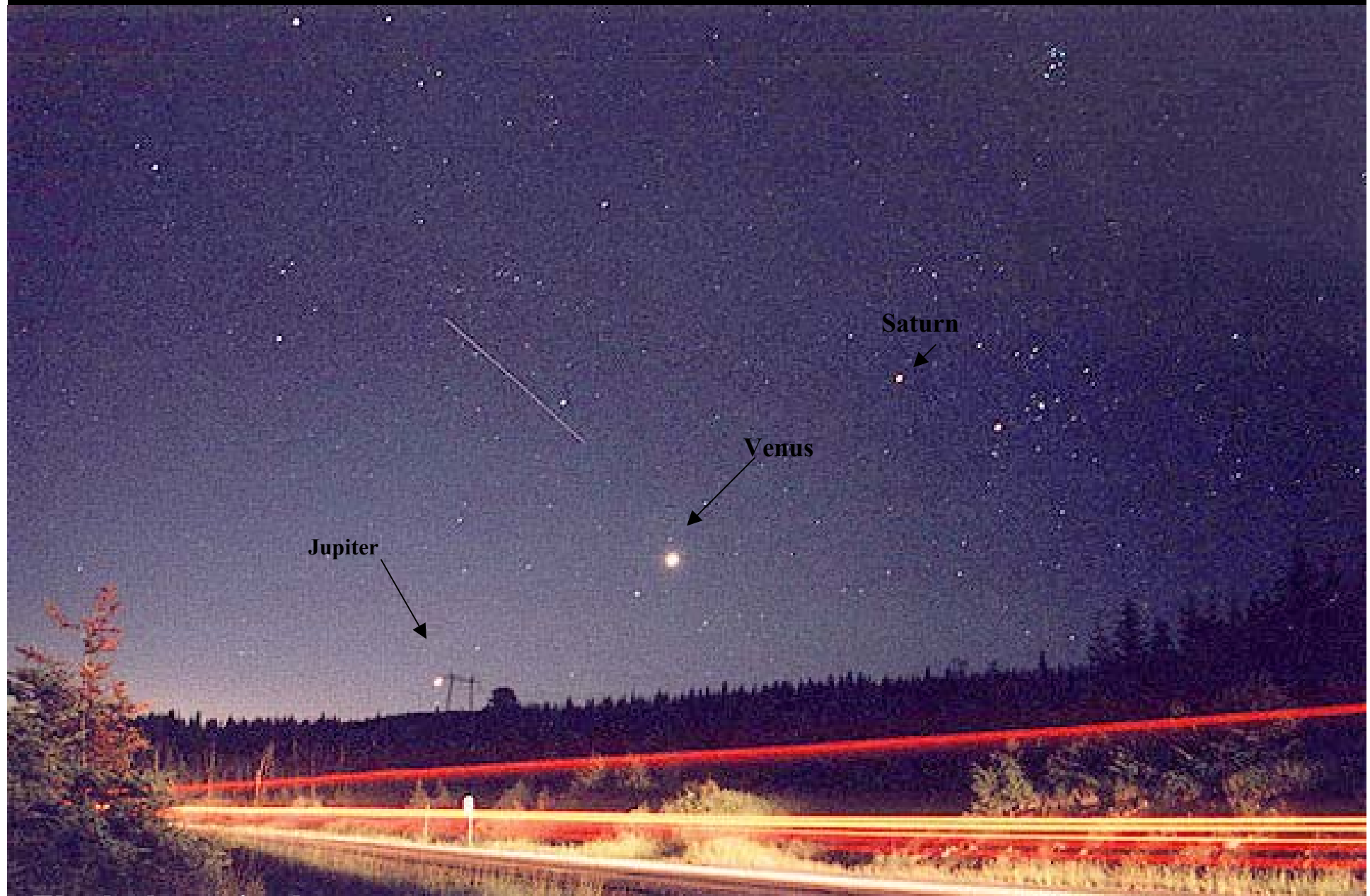
Institut de Ciències de l'Espai (CSIC)

1a Jornada de Recerca

DFEN - UPC

Barcelona, 1 febrer 2005

És el cel inmutable?



El cel a la matinada

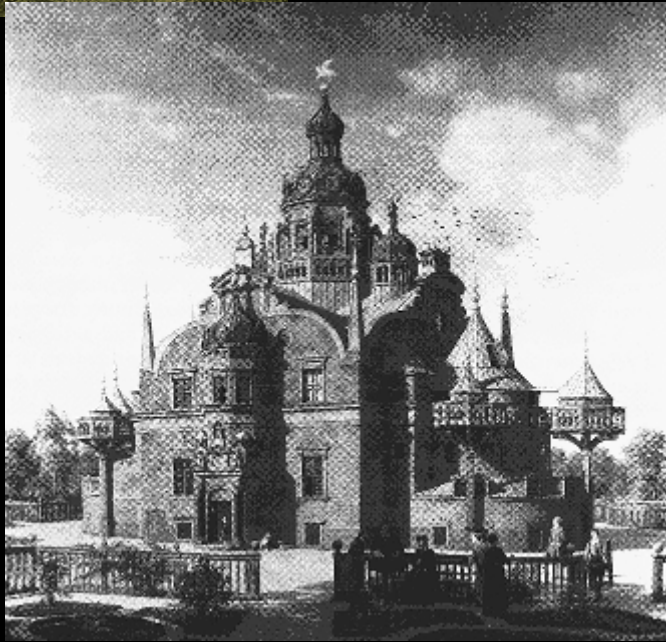


Figure 1: Artist concept of SN1006. Credit and Copyright:Tunç Tezel.

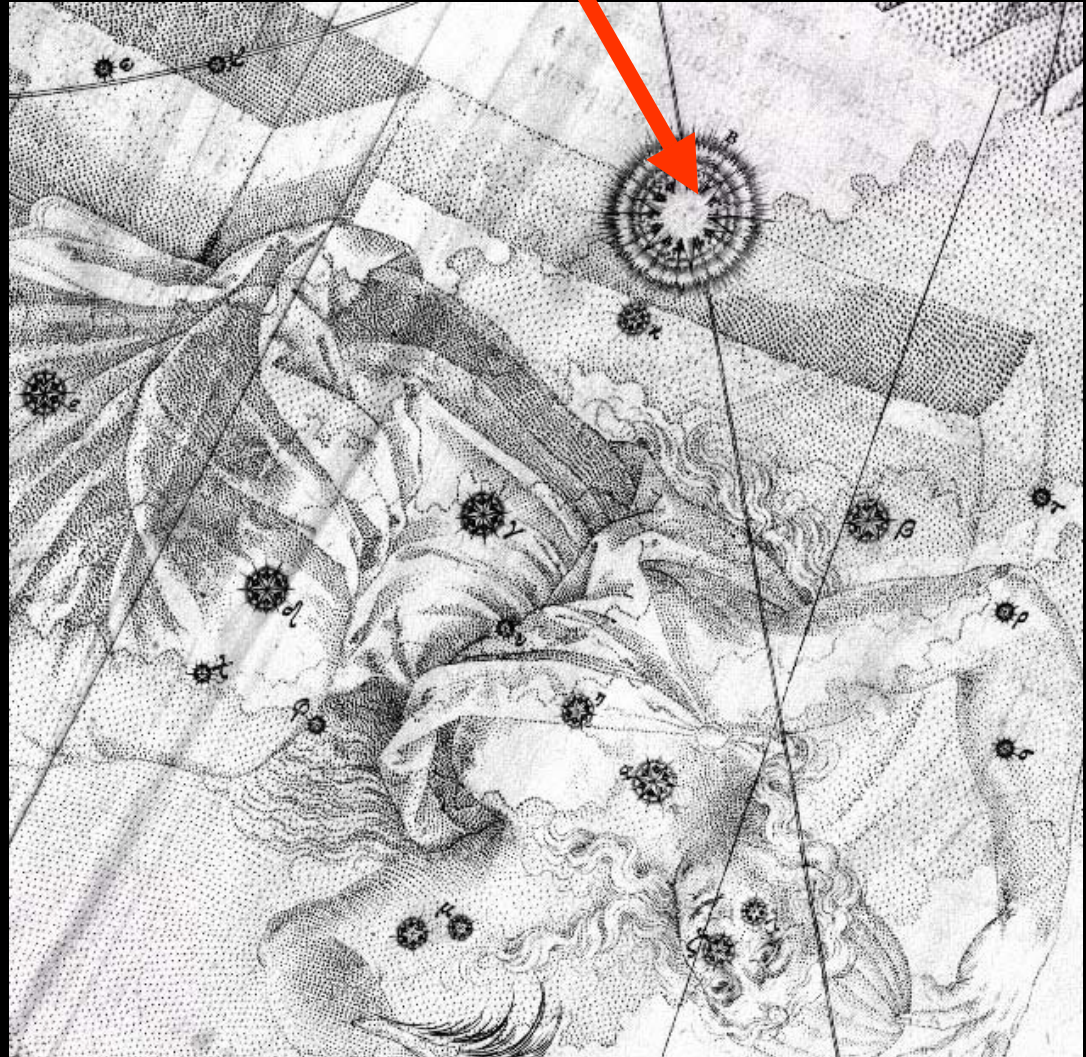


Tycho Brahe

**SN1572
Cassiopeia**

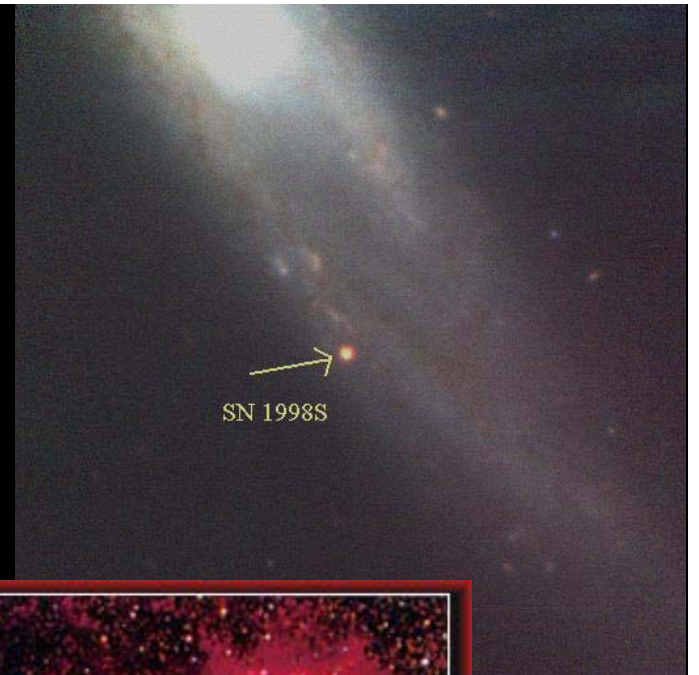


Uraniborg





SN 1998bu



SN 1998S

SN1987A



Supernoves

Evidències de la mort de les estrelles

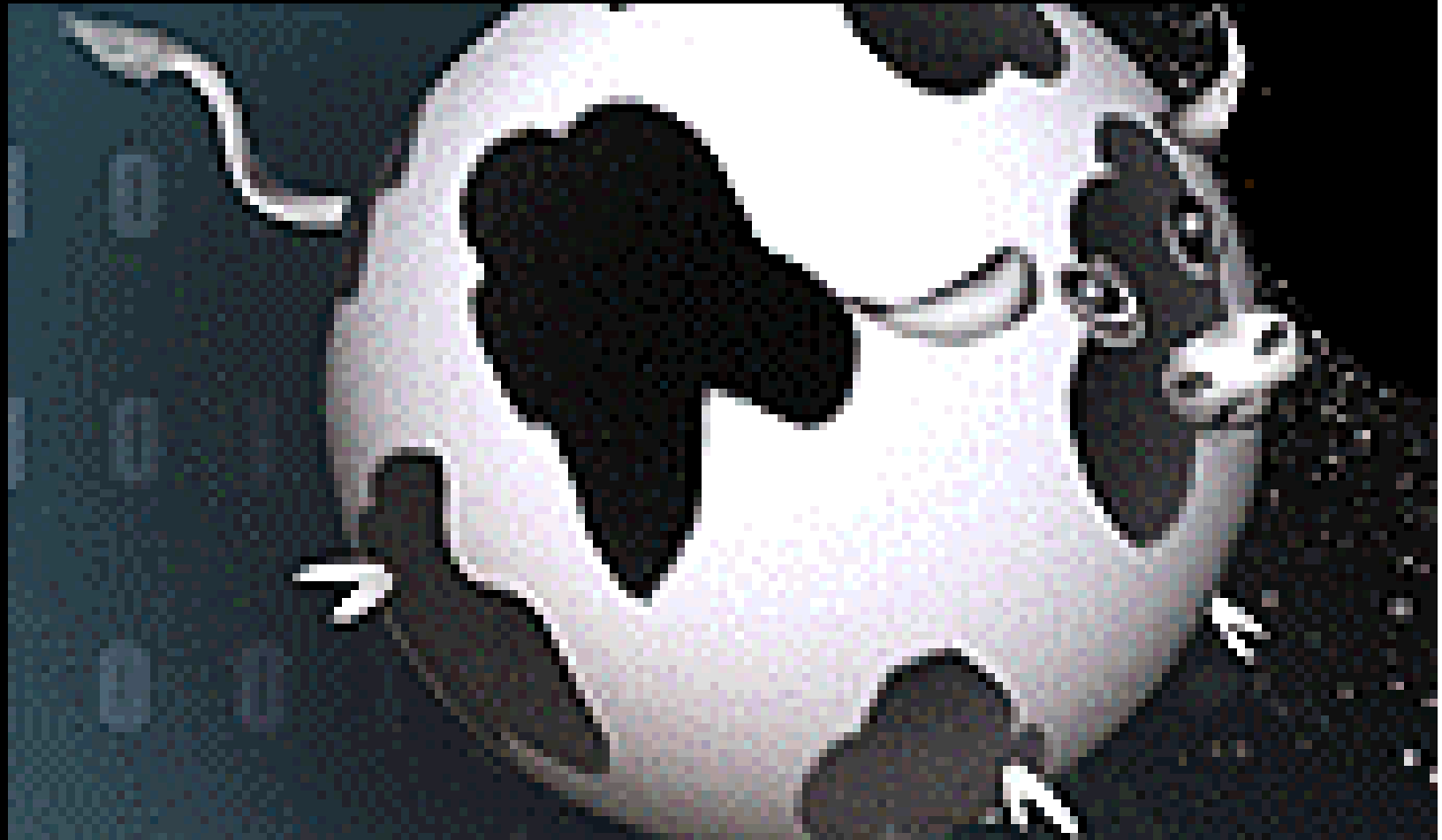


10^{51} erg d'energia cinètica!
Tota l'estrella està implicada a l'explosió

Exploding stars

- They play a fundamental role in shaping the galaxy
 - They inject 10^{51} ergs/explosion in the form of kinetic energy per event
 - They trigger the formation of new stars
 - They accelerate cosmic rays
 - They power intense galactic winds that can even remove the galactic gas and kill the process of star formation
 - They inject several M_{\odot} of freshly synthesized chemical elements, both stable and radioactive.
 - They play a key role on the origin and evolution of life
 - They synthesize the elements necessary to build rocky planets
 - They synthesize the biogenic elements
 - They can sterilize large regions of the Galaxy

Usually, spherical symmetry is assumed: only radial gradients are allowed. But ...



Hydrostatic Equilibrium

Characteristic times

Hydrodynamic time: $\tau_{\text{HD}} \approx 440 \rho^{-1/2}$
Thermal time: 10^7 yr
Nuclear time: 10^9 yr

$$\rho \approx \frac{M}{R^3}$$

$$\frac{dp}{dr} \approx \frac{P}{R}$$

$$\frac{dP}{dr} = -\rho \frac{Gm}{r^2}$$

$$P \approx M^2 R^{-4}$$

Electron degeneracy

At high densities e^- are dominant

$$P \cong P_{e,0}(\rho) + P_{e,1}(\rho, T) + P_{i,1}(\rho, T)$$

If

$$T \rightarrow 0$$

$$P_{e,1}(\rho, T) \rightarrow 0$$

$$P_{i,1}(\rho, T) \rightarrow 0$$

$$P_{e,0} = K_{NR} \rho^{5/3}$$

Even at $T=0$ electrons (and other fermions) are able to exert pressure!

$$P_{e,0} = K_{ER} \rho^{4/3}$$

Zero temperature structures can exist

The virial theorem

$$E_G = -3 \int_* P dV$$

Non Relativistic
Particles

$$P = 2/3 \epsilon$$

$$E_i = -1/2 E_G$$

During a gravitational transition from an equilibrium configuration to another one, half of the energy is radiated away and half is invested in internal energy.

$$P = 1/3 \epsilon$$

Extremely Relativistic
Particles

$$E_i = -E_G$$

Relativistic stars are not bounded

$$M_{Ch} = 1.44 \langle 2Y_e \rangle^2 M_o$$

Non relativistic electrons

If electrons are non relativistic

$$P \approx (MR^{-3})^{5/3} = M^{5/3} R^{-5}$$

Hydrostatic equilibrium:

$$P \approx M^2 R^{-4}$$



**It is always possible to find an equilibrium structure
The star only needs to contract**



R decreases when M increases

Nuclear reactions

Virial theorem $\Rightarrow E_i \cong E_G$

$$E_i \sim MT$$

$$E_G \sim M^2 R^{-1}$$

$$T \sim M/R$$

$$\rho \sim M R^{-3}$$

$$\rho \sim T^3 M^{-2}$$

Each burning phase occurs at a fixed temperature

$$\rho \sim M^{-2}$$

Light stars ignite nuclear reactions at high densities

Electron degeneracy can stop the nuclear burning process

$M < 0.08 \text{ Mo}$, H is never ignited

$M < 0.5 \text{ Mo}$, He is never ignited

$M < 8-9 \text{ Mo}$, C is never ignited

$M < 10-12 \text{ Mo}$, Ne is never ignited

$M > 10-12 \text{ Mo}$, Fe cores are formed



$M < 0.5 \text{ Mo}$, form He cores
 $M < 8-9 \text{ Mo}$, form C/O cores
 $M < 10-12 \text{ Mo}$, form O/Ne

These limits change in binary systems.
If close enough, stars
with 2.5 Mo can give He wd of $\sim 0.4 \text{ Mo}$

If $M \uparrow \quad R \downarrow \Rightarrow E_F \uparrow$

When $E_F \gg m_e c^2$ electrons become relativistic

Relativistic electrons

If electrons are relativistic

$$P \approx (MR^{-3})^{4/3} = M^{4/3} R^{-4}$$

Hydrostatic equilibrium:

$$P \approx M^2 R^{-4}$$



It is not possible to find an equilibrium structure



There is not a length scale

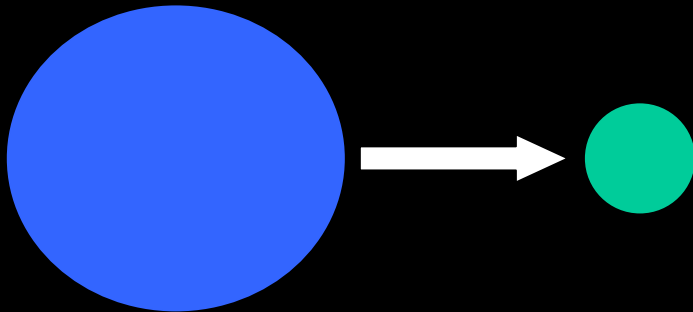
If $\delta E < 0$ $\delta R < 0$ The star contracts

If $\delta E > 0$ $\delta R > 0$ The star expands

The ideal scenario for catastrophic events !

Explosive sources of energy

Gravitational collapse



Electron degenerate core

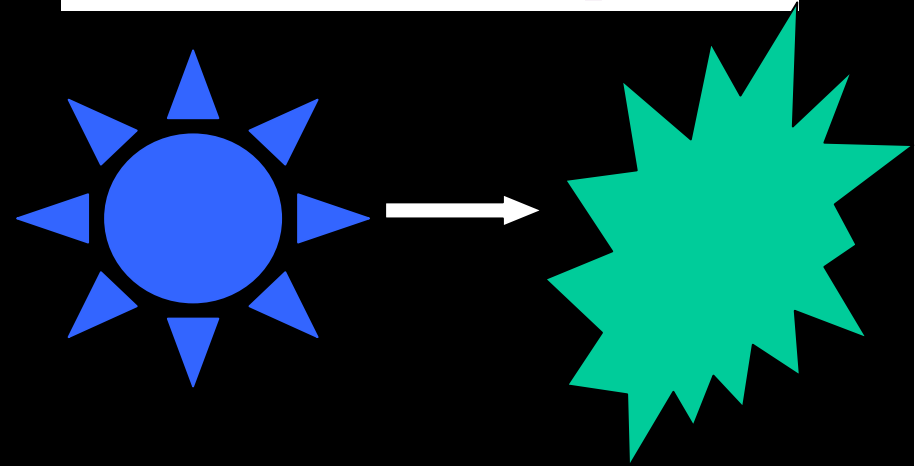
$M \sim 1.4 \text{ Mo}$
 $R \sim 10^8\text{-}10^9 \text{ cm}$

Neutron star

$M \sim 1.4 \text{ Mo}$
 $R \sim 10^6 \text{ cm}$

$\Delta E_G \sim 10^{53} \text{ erg}$
 $K \sim 10^{51} \text{ erg}$
 $E_{\text{em}} \sim 10^{49} \text{ erg}$

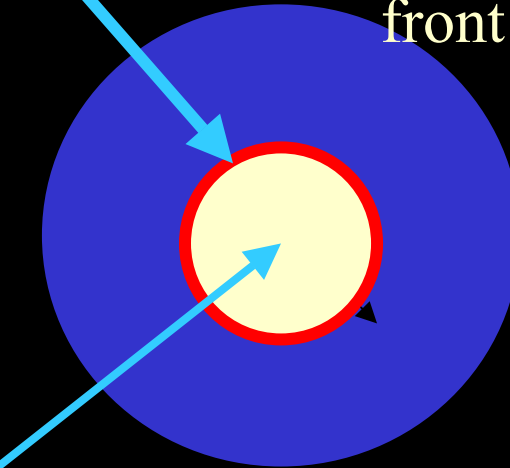
Thermonuclear explosion



$\{^{12}\text{C}, ^{16}\text{O}\} \rightarrow \{^{56}\text{Ni}\}$
 $q \sim 7 \times 10^{17} \text{ erg/g}$
 $1 \text{ Mo} \times q \sim 10^{51} \text{ erg}$
 $K \sim 10^{51} \text{ erg}$
 $E_{\text{em}} \sim 10^{49} \text{ erg}$
 $L_{\text{max}} \sim 10^{43} \text{ erg/s}$

Nuclear energy
release

Electron
captures



The energy losses by electron captures depend on the ignition density

The injected energy depends on the velocity of the burning front

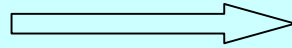
He cores always explode

CO cores can explode or collapse

ONe cores always collapse

Fe cores always collapse

$M < 0.8 M_{\odot}$



$\tau > 1/H_0$

$0.8 < M/M_{\odot} < 8$



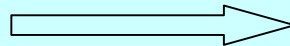
$\left\{ \begin{array}{l} 30 \text{ Myr} < \tau < 15 \text{ Gyr} \\ 0.5 < M_f/M_{\odot} < 1.1 \end{array} \right. \quad \text{CO WD}$

$8 < M/M_{\odot} < 11$



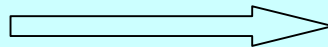
$\left\{ \begin{array}{l} \tau \sim 10\text{--}30 \text{ Myr} \\ M_f = 1.2\text{--}1.3 M_{\odot} \end{array} \right. \quad \text{ONe WD}$

$11 < M/M_{\odot} < 100$



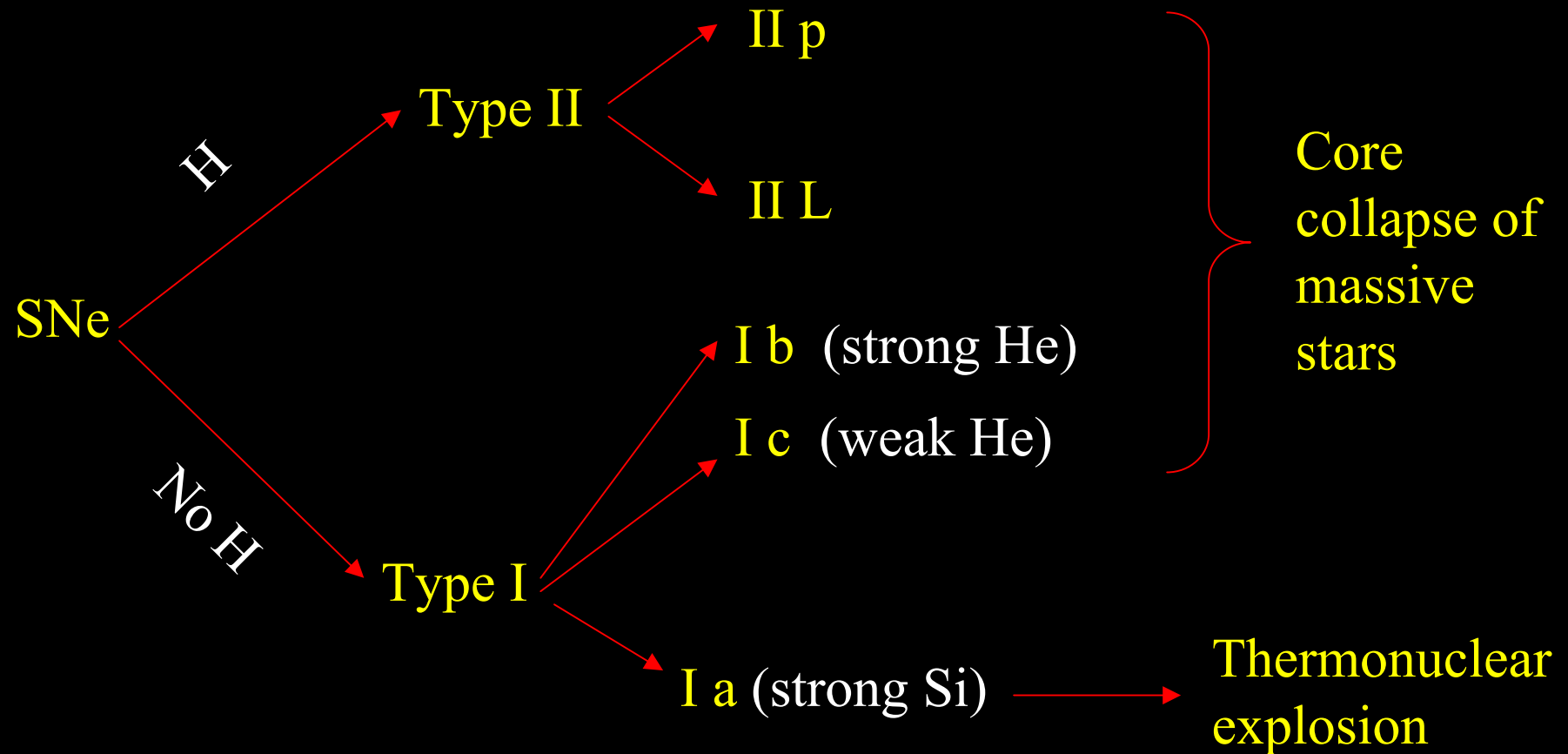
$\left\{ \begin{array}{l} \tau \sim 1\text{--}10 \text{ Myr} \\ M_f = 1.2\text{--}2.5 M_{\odot} \end{array} \right. \quad \text{Fe collapse NS/BH}$

$M > 100 M_{\odot}$



$\left\{ \begin{array}{l} \tau \sim 1 \text{ Myr} \\ \text{may or may not explode} \end{array} \right.$

SNe Classification



based on spectra and light curve morphology

SNe Statistics

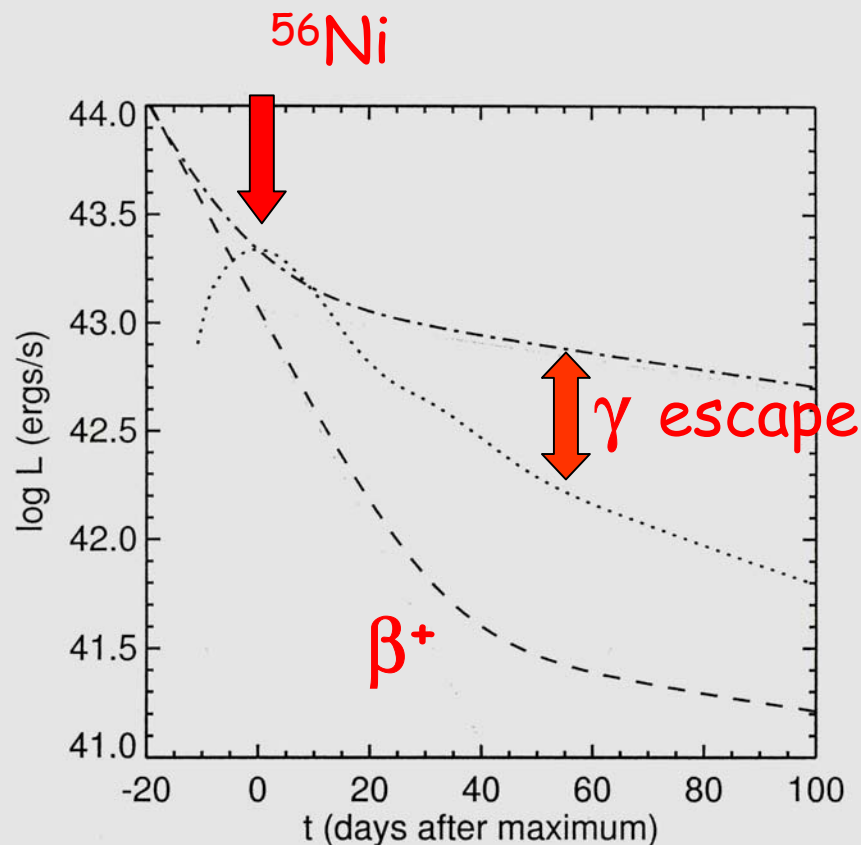
SN rate per unit Mass ($10^{-11} M_{\odot} 10^{-2} \text{ yr } (H_0/75)^2$)

Galaxy	Ia	Ib/c	II	All
E-S0	0.16 ± 0.03	< 0.01	< 0.01	0.16 ± 0.03
S0a-Sb	0.29 ± 0.07	0.16 ± 0.07	0.69 ± 0.17	1.14 ± 0.20
S0c-Sd	0.46 ± 0.10	0.30 ± 0.11	1.89 ± 0.34	2.65 ± 0.37
All	0.27 ± 0.03	0.11 ± 0.03	0.53 ± 0.07	0.91 ± 0.08

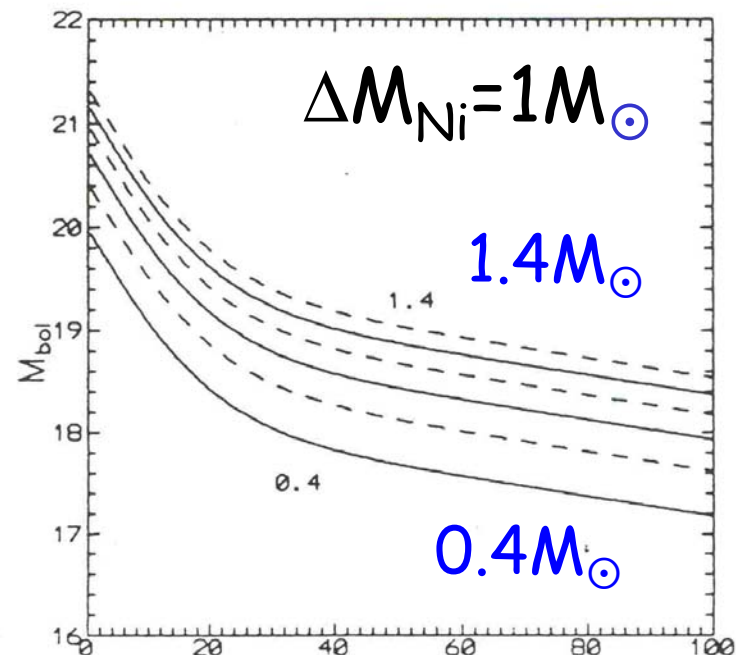
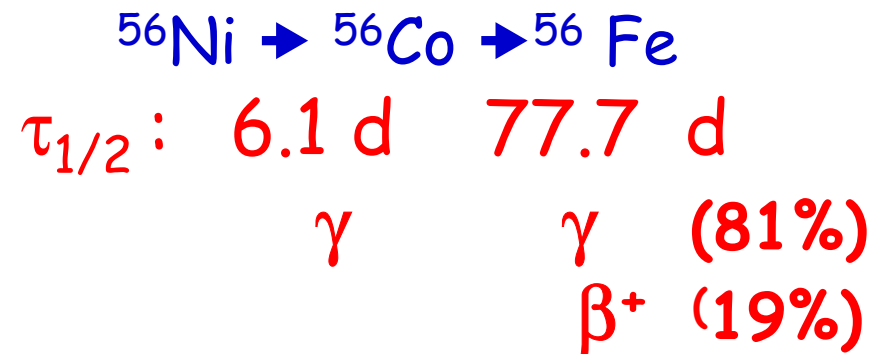
Cappellaro, Barbon, Turatto 2003

II. Light Curves

Bolometric LCs \leftrightarrow Radioactive energy



Leibundgut 2003



Observational constraints. I

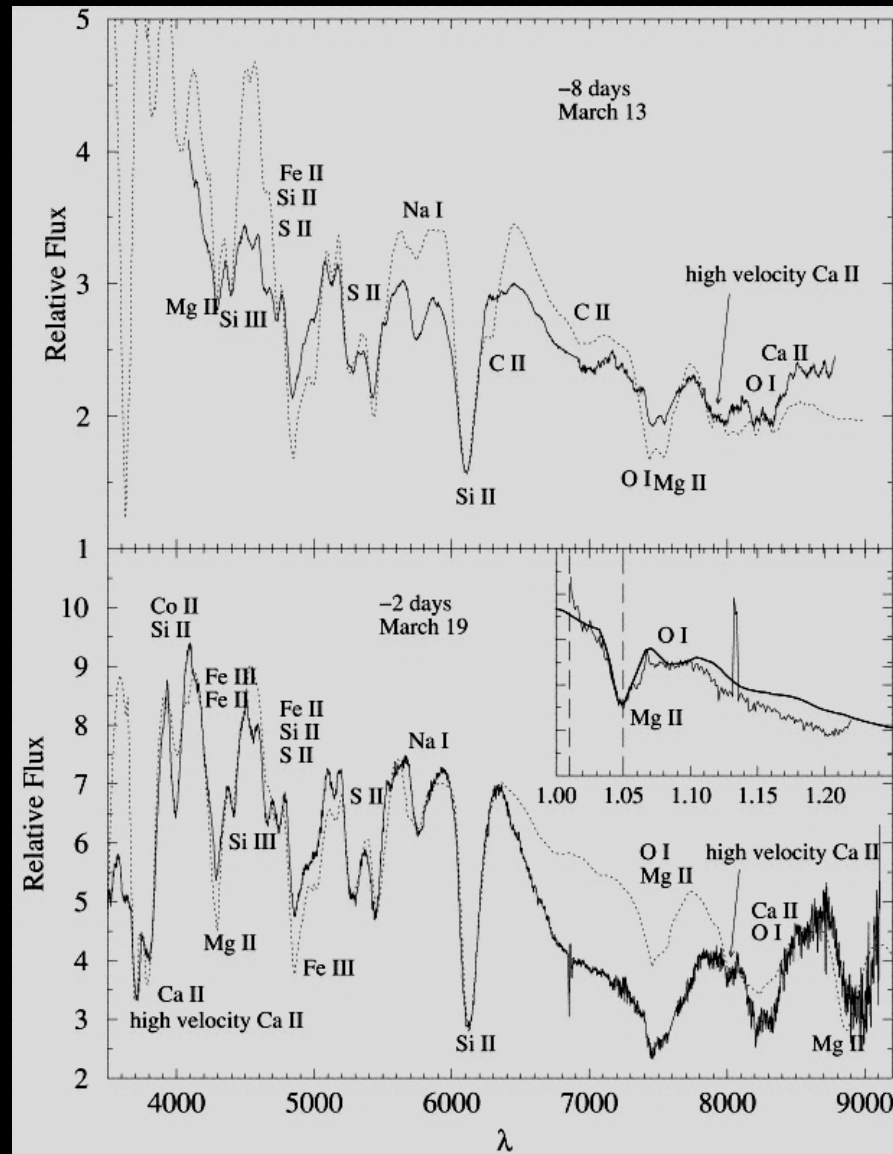
- H must be absent at the moment of the explosion
 - There are some evidences (weak) of H-lines before maximum or at late epochs
- Progenitors should be long lived to account for their presence in all galaxies, including ellipticals
- The explosion should produce at least $\sim 0.3 M_0$ of ^{56}Ni to account for the light curve and late time spectra



SNIa are caused by the explosion of a C/O white dwarf in a binary system

(He white dwarfs detonate and are converted in Fe and ONe collapse to a neutron star)

Spectra: abundances & velocities



Hatano et al. 1999

- Peak: absorption
CII OI SiII
SI CaII MgII

Incomplete
burning

10000 → 15000 km/s

Near-IR:

SiII CaII MgII
Fe peak

"small" polarization

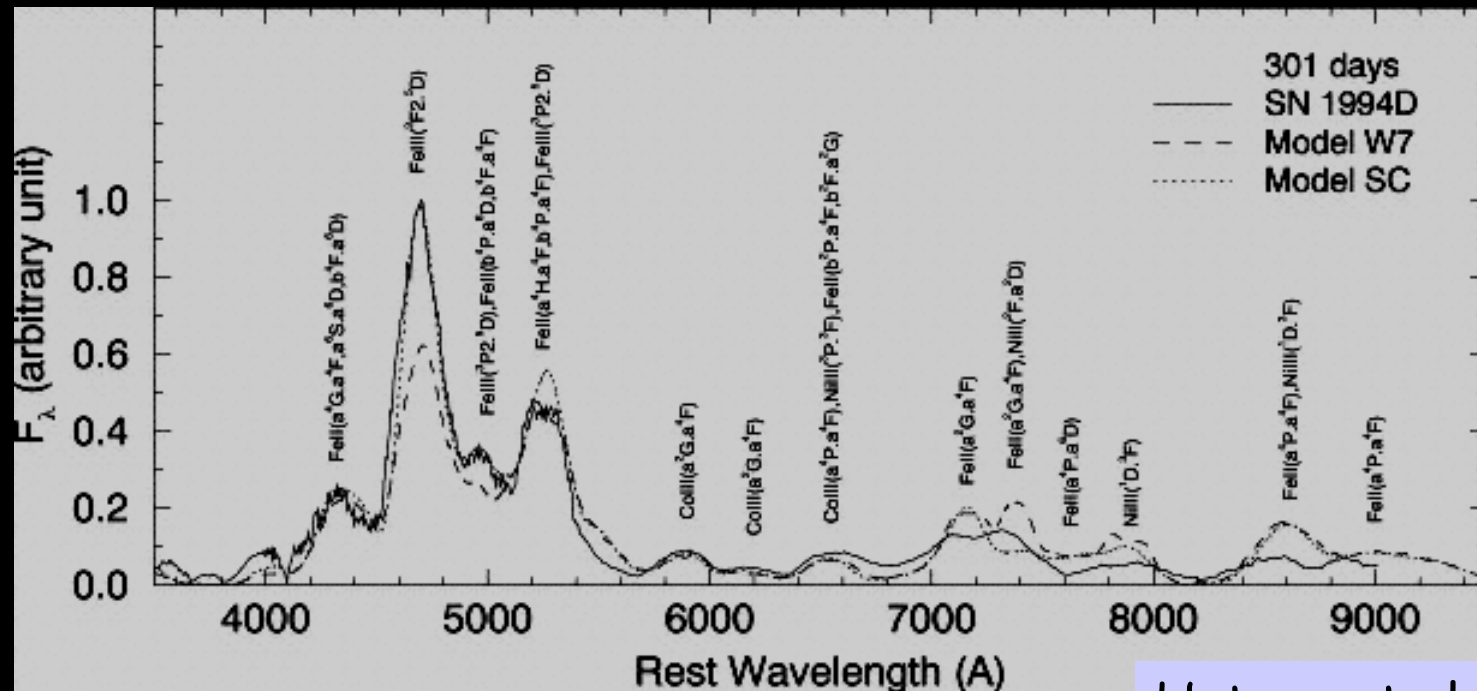
Nebular spectra

- Late time: emission

Fe Co

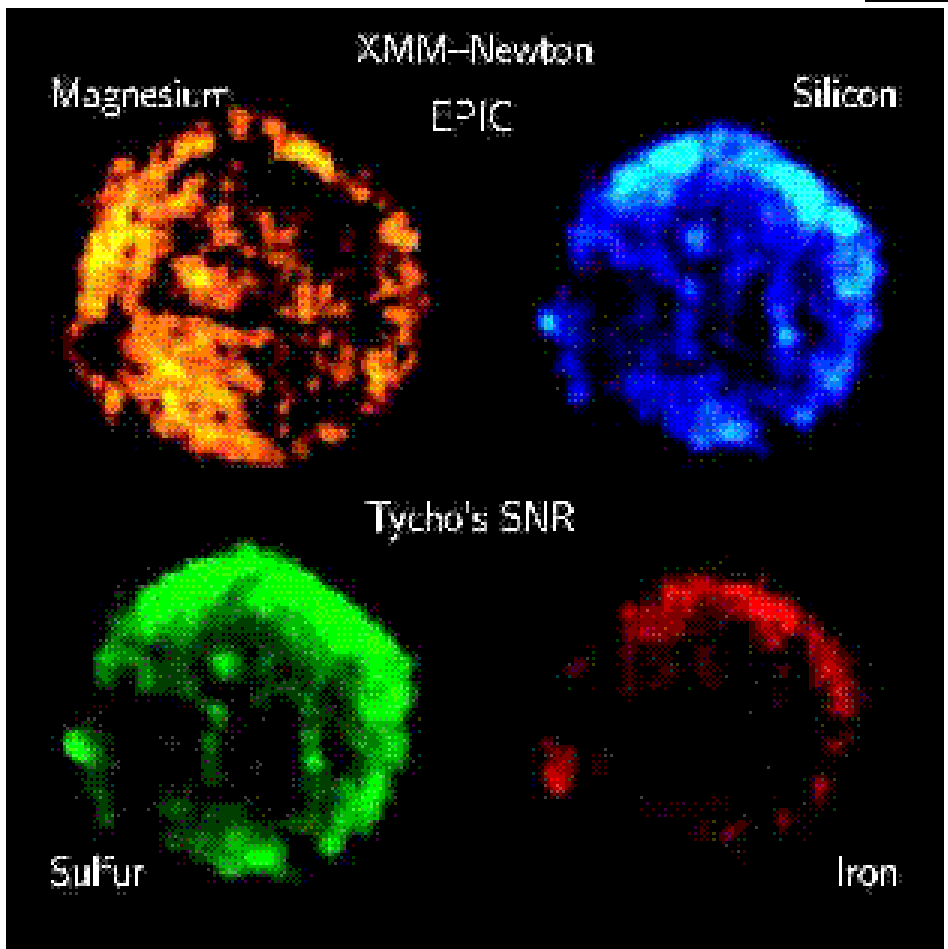
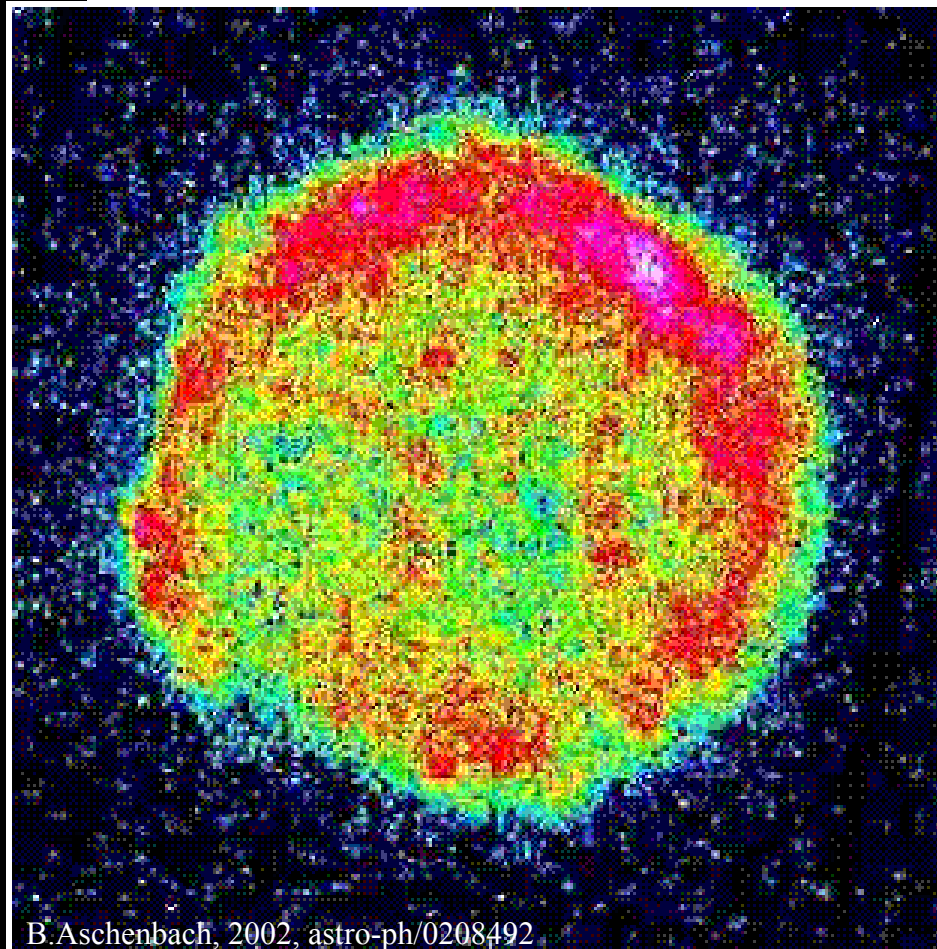
Complete
burning

< 10000 km/s



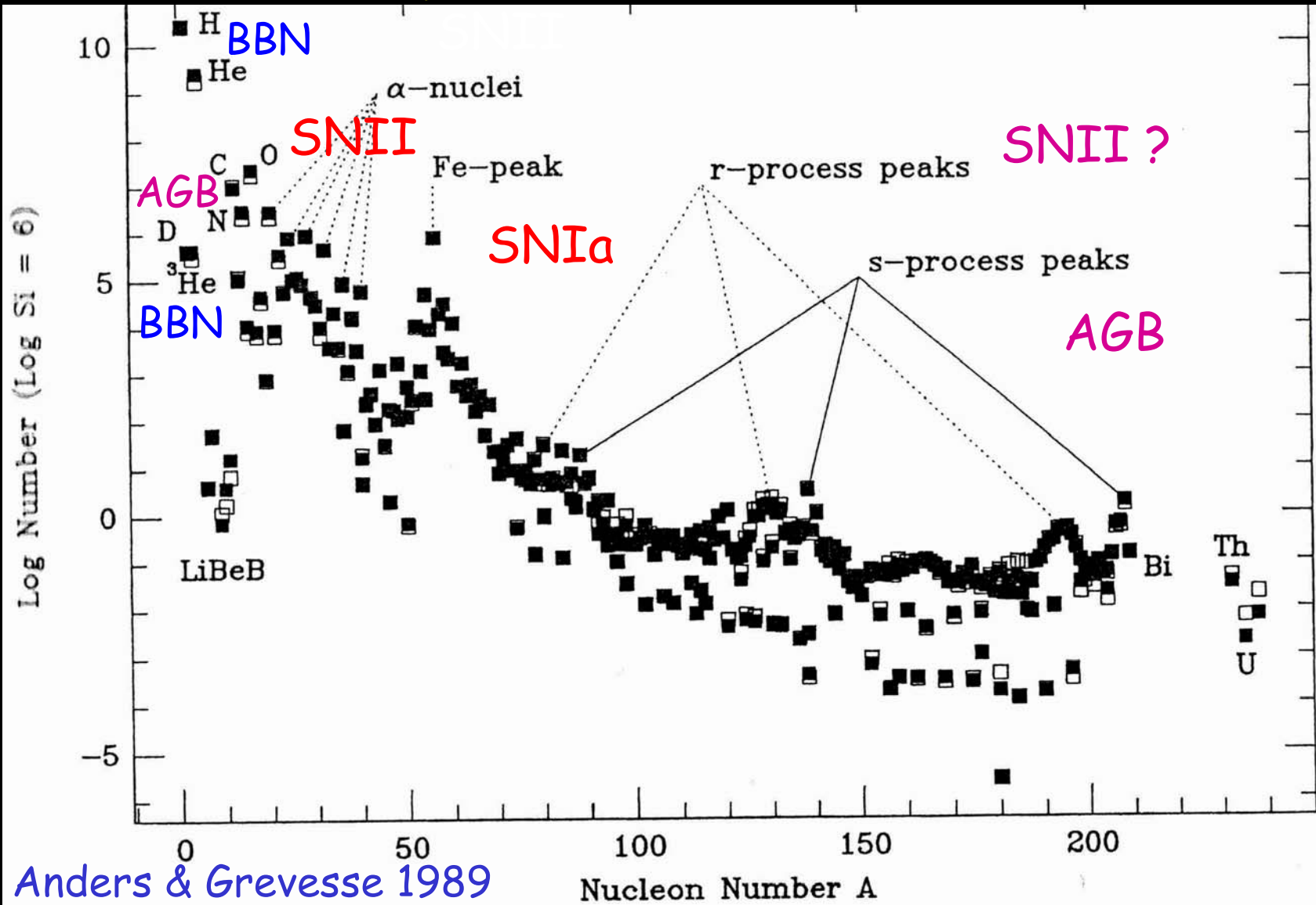
Hatano et al. 1999

Tycho Remnant (SN 1572)



XMM-Newton

Solar system abundances



Anders & Grevesse 1989

Cameron 1982 (Arnett 1996)

Observational constraints. II

- Intermediate elements must be present in the outer layers to account for the spectrum at maximum light



The burning must be subsonic. It can be supersonic only if $\rho < 10^7 \text{ g/cm}^3$

The abundances of the iron peak elements (^{54}Fe , ^{58}Ni , ^{54}Cr) must be compatible with the Solar System abundances after mixing with gravitational supernova products



Neutron excesses have to be avoided:

- Post-burning e^- -captures
- Neutrons stored as ^{22}Ne
- Decrease ignition density
- Decrease ^{22}Ne content
- Reduce the SNIa galactic contribution

Thermonuclear runaways

The necessary condition is that the energy must be released in a time shorter than the dynamical time

Nuclear heating time:

$$\tau_n = \frac{c_V T}{\dot{\mathcal{E}}_n}$$

$$c_V = \frac{3 \mathfrak{R}}{2 \mu}$$

$$\dot{\mathcal{E}}_n \propto T^\alpha e^{-(T_0/T)^\beta}$$

The hydrodynamical time:

$$\tau_{HD} = \frac{l}{c_s}$$

In hydrostatic equilibrium

$$\tau_{HD} = \tau_{ff}$$

$$\tau_{ff} = (24\pi G \bar{\rho})^{-1/2} = \frac{444}{\sqrt{\bar{\rho}}}$$

The instability condition is: $\tau_n < \tau_{HD}$

Deflagration temperature

$$\tau_n(T_D) = \tau_{HD}(T_D)$$

$$\frac{3(24\pi G)^{1/2} \mathfrak{R}}{3\mu Q_0 R_0} \rho^{1/2} T^{1-\alpha} e^{(T_0/T)^\beta} \leq 1$$

Why typical stars are stable?: They stabilize the fuel by means of adiabatic expansions

The efficiency of the adiabatic cooling is defined as the expansion, $\delta\rho$, experienced to restore pressure equilibrium

$$\frac{\delta\rho}{\rho_0} = \frac{1}{\Gamma_1\rho_0} \left(\frac{\partial P}{\partial T} \right)_\rho \frac{QN_A}{AC_V} \Delta X$$

Where ΔX is the amount of burned fuel

If the electronic degenerate component is dominant:

In the gas ideal case:

$$\frac{\delta\rho}{\rho_0} = \frac{2}{5} \Delta X \frac{\mu}{A} \frac{Q}{kT}$$

Since $Q \sim 1$ MeV and $kT \sim 1$ -100 keV
adiabatic cooling is very efficient and
stars are stable

$$\left(\frac{\partial P_e}{\partial T} \right)_\rho \ll \left(\frac{\partial P_i}{\partial T} \right)_\rho$$

$$\frac{\delta\rho}{\rho_0} = \left(\frac{\Delta X}{2} \frac{\mu}{A} \frac{Q}{kT} \right) \frac{P_i}{P_i + P_e} \approx \frac{P_i}{P_e} \ll 1$$

Cooling is only efficient if $P_i > P_e$

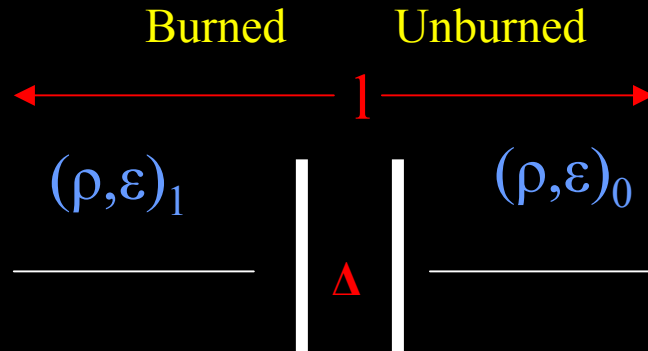
Thermonuclear runaways occur if: $T_{\text{def}} < T_F$

H is not a good explosive because it needs weak interactions to convert p in n (novae)

He and C are good explosives (supernovae)

$$\Delta \ll 1$$

The burning front



Mass, momentum and energy conservation

$$\rho_1 u_1 = \rho_0 u_0$$

$$P_1 + \rho_1 u_1^2 = P_0 + \rho_0 u_0^2$$

$$\varepsilon_1 + \frac{P_1}{\rho_1} + \frac{u_1^2}{2} = \varepsilon_0 + \frac{P_0}{\rho_0} + \frac{u_0^2}{2}$$

Two types of solutions

$$\begin{matrix} P_1 > P_0 \\ V_1 < V_0 \end{matrix}$$

Detonation: v_{front} supersonic versus the unburned material
sonic or subsonic versus the burned material

$$\begin{matrix} P_1 < P_0 \\ V_1 > V_0 \end{matrix}$$

Deflagration: v_{front} always subsonic versus the unburned & burned material

Deflagrations

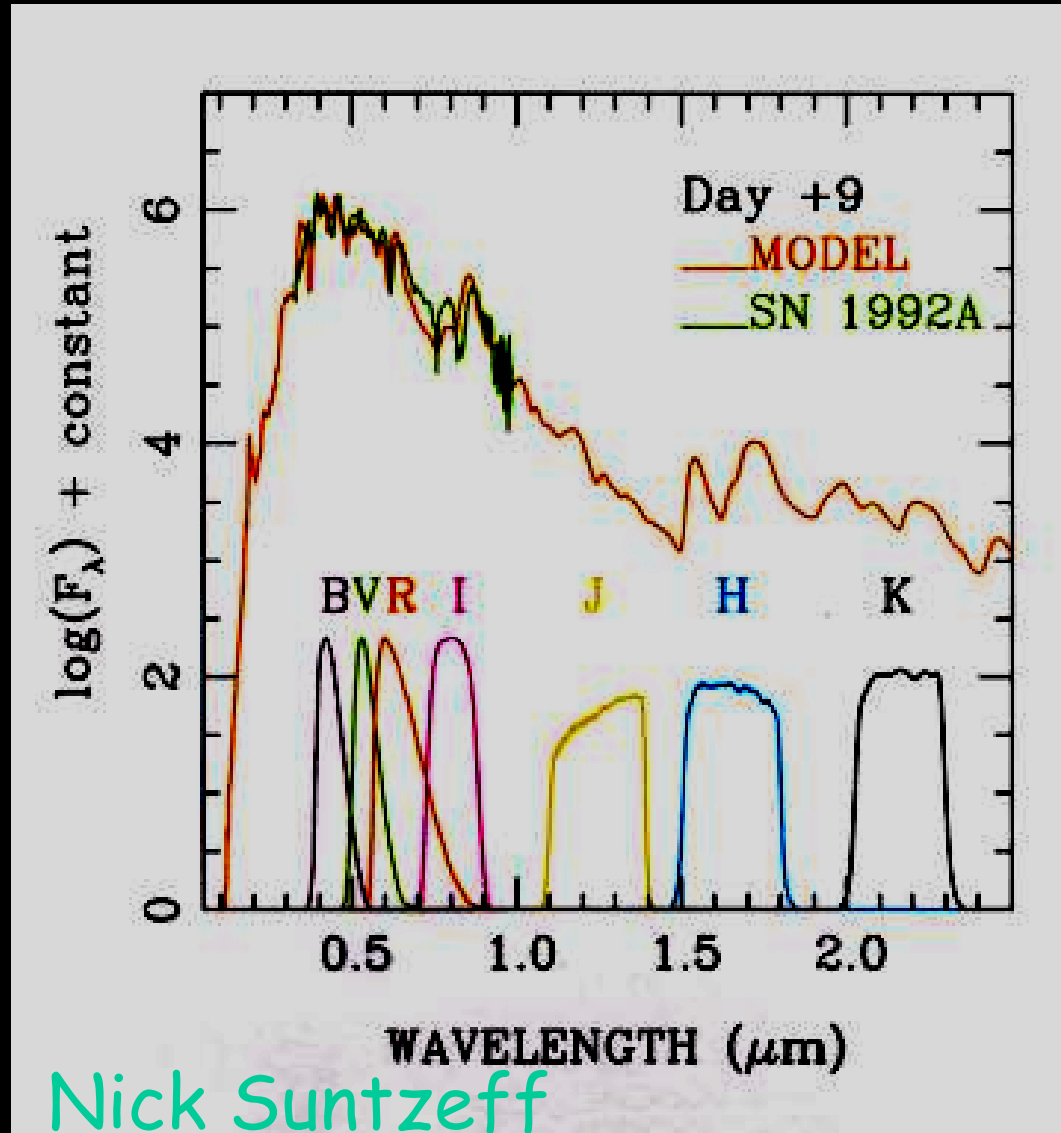
In spherical symmetry burned material is at rest at the center, $v_1 = 0$

Assume unburned material at rest, $v_0 = 0$
Mass and momentum conservation demands:
 $V_0 (P_1 - P_0) = u_0 (u_0 - u_1)$
or
 $V_0 (P_1 - P_0) = u_1 D$
in the frame at rest

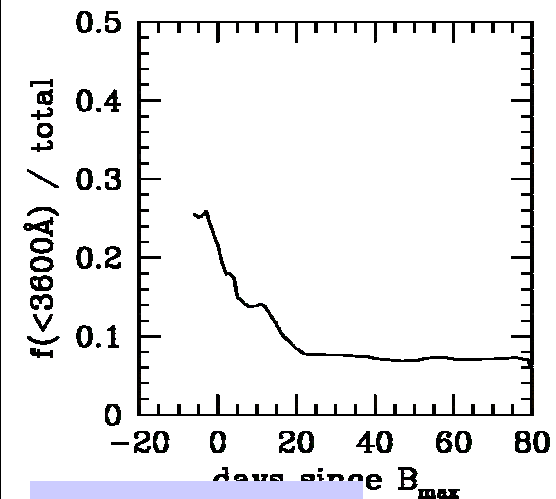
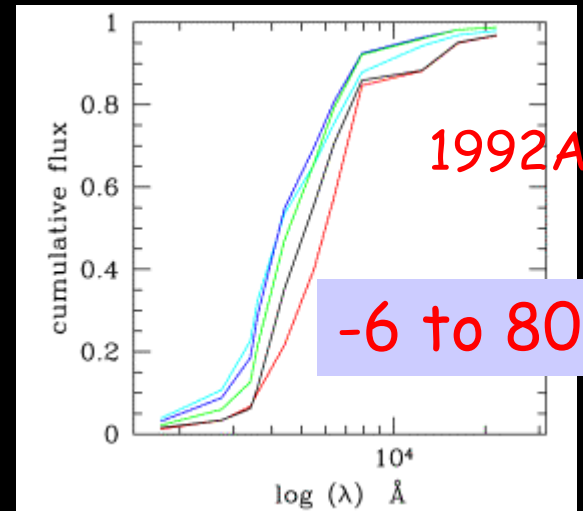
But if
 $P_1 - P_0 < 0$ & $D > 0$
then
 $v_1 < 0$
in contradiction with the
hypothesis

A deflagration can only exist if it generates a precursor shock that burst matter outwards!

Flux & Filters



>80% flux in the optical



UV < 10 %

I. Observations

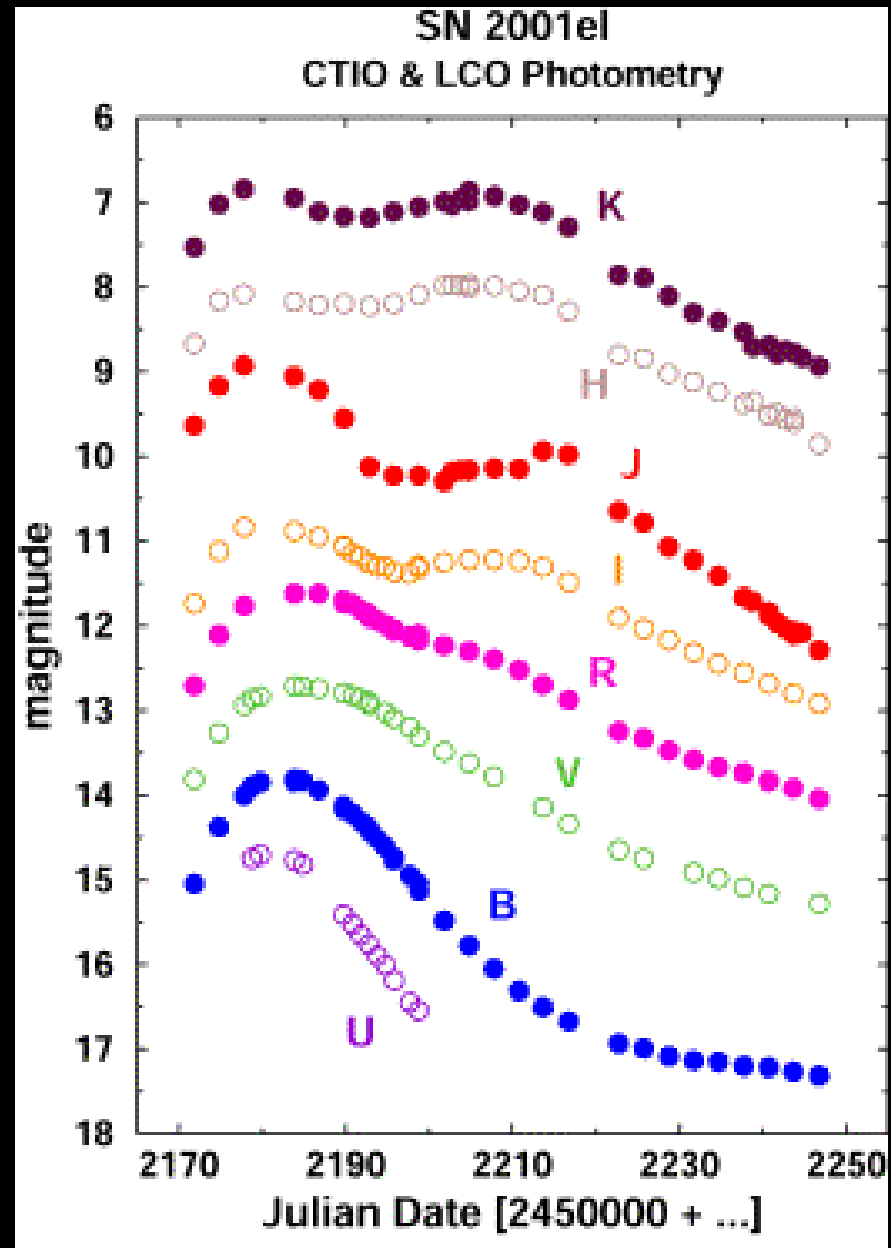
UBVRIJHK



Most of the emission
in the Optical and NIR

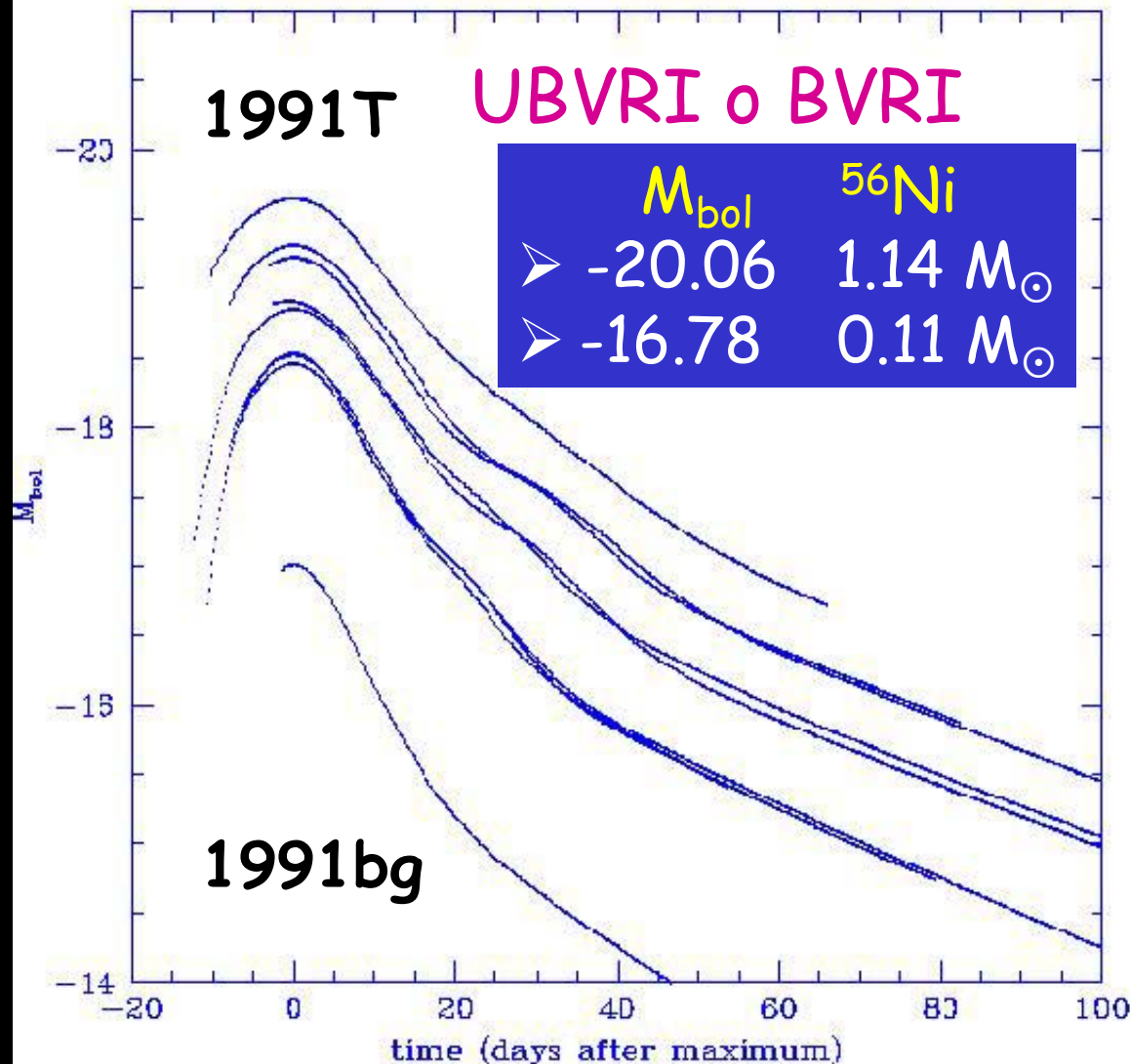
2nd peak IJHK

Elias 1981 Meikle 2000



Ni mass from observed M_{MAX}

Contardo, Leibundgut, Vacca, 2001



Time of maximum assumed:

$$\Delta t_{\text{expl}} = 17 \text{ d}$$

16 to 20 d \rightarrow 10% Ni

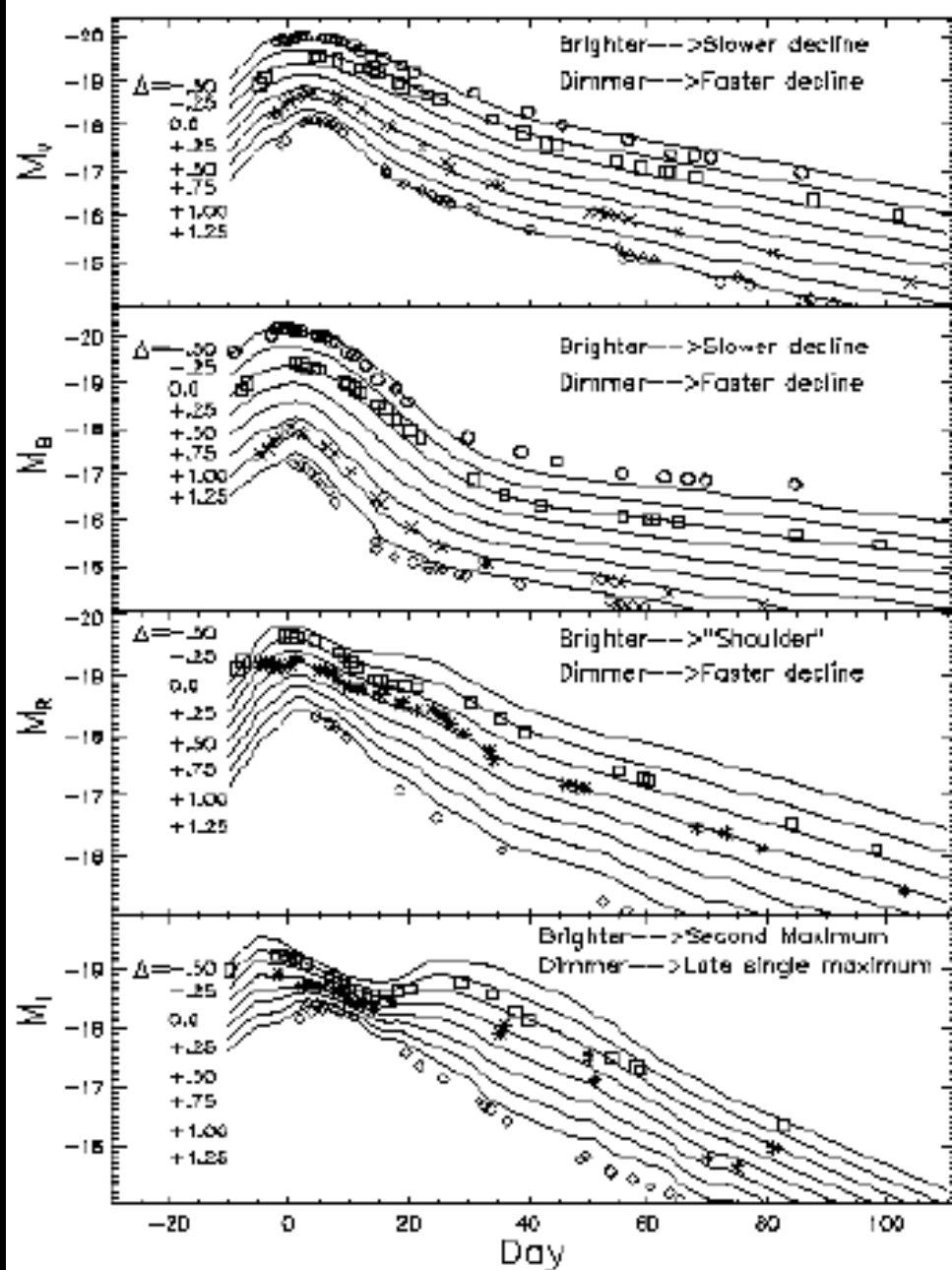
+ Problems:

- Distance
- Reddening

Other methods:

- LCs up to 800 d
Cappellaro et al 1997
- Late IR spectra (Fe)
Spyromilo et al 1992

MAX-LC Shape Relations



Correlation
 $M_{MAX} \leftrightarrow$ Decline rate

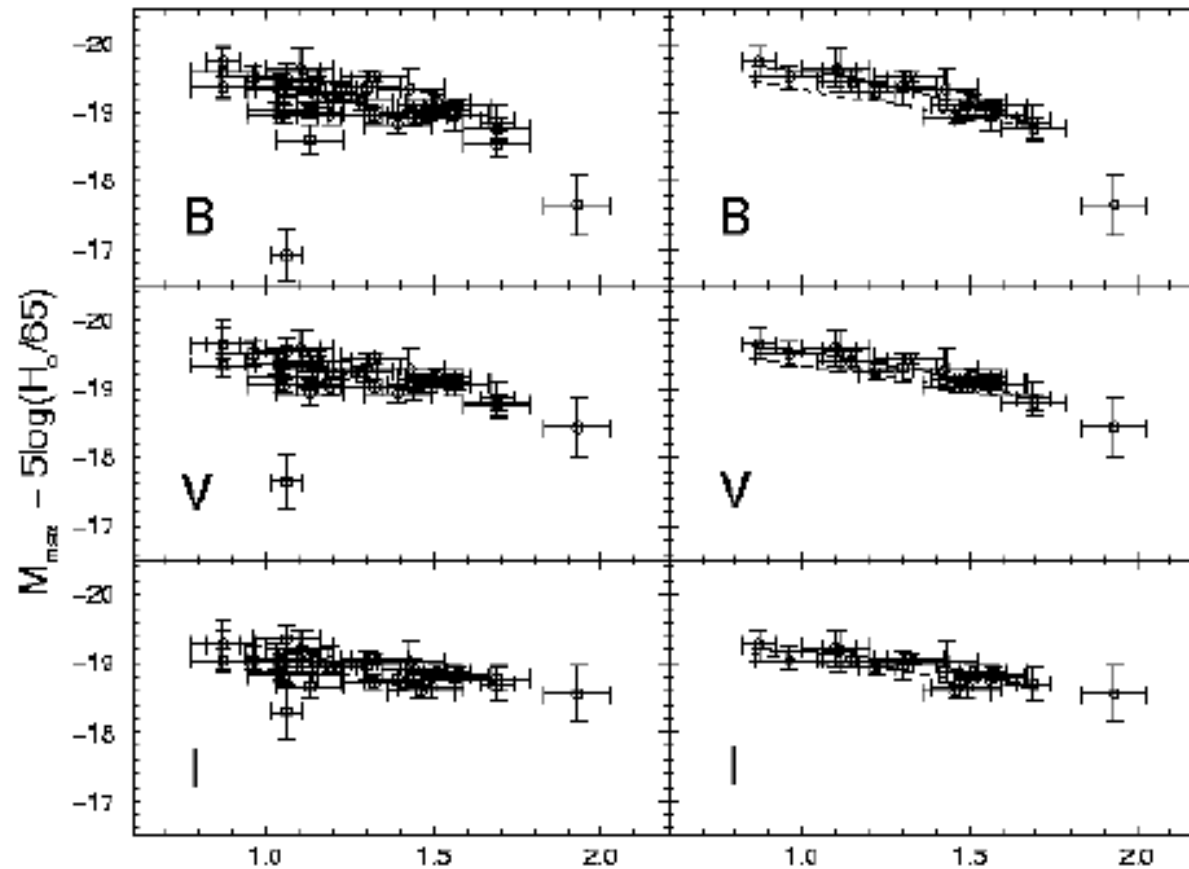
**Brighter
Slower Decline**

**Dimmer
Faster Decline**

Riess et al. , 1997

Maximum Brightness - Decline Relation

Phillips et al. 1996, 1999



$$M_{\text{max}} - \Delta m_{15}$$

$$\langle \sigma \rangle = 0.17 \text{ mag}$$

$$\Delta m_{15}$$

Caution: local calibrations

Cosmology & SN Ia

- Bright
- Homogeneous
- No evolutionary effects



**Standard
Candles**



Standard Model of Cosmology (SNe Ia + CMB)

$$\Omega_m \sim 0.3 \quad \Omega_\lambda \sim 0.7$$

$$60 \text{ km/s/Mpc} < H_0 < 70 \text{ km/s/Mpc}$$

Age of the Universe $\sim 14000 \text{ Myr}$

Observational constraints. III

- Homogeneity?
 - Differences in brightness: Overluminous (SN 1991T), underluminous (SN1991bg)
 - Differences in the expansion velocity ($v_{\text{exp}} \sim 10,000\text{-}15,000 \text{ km/s}$)
- Two points of view:
 - There is a bulk of homogeneous supernovae plus some peculiars
 - SNIa display a continuous range of values
- Is there a unique scenario & unique mechanism able to accommodate the normal behavior plus that of dissidents?
- Is there a mechanism able to produce a continuous range of situations?
- Can both mechanisms coexist?

Anything able to explode eventually do it !!!

The outcome depends on:

Accretion rate

Chemical composition of accreted matter

CO accreting WD

Merging of two CO WD.

The outcome depends on the rate. AIC?

He accreting WD

$10^{-9} < \dot{M}_t < 5 \times 10^{-8} \text{ M}_\odot \text{ yr}^{-1}$

off center detonation

CO+He star, normal or degenerate

H accreting WD

$\dot{M}_t < 10^{-9} \text{ M}_\odot \text{ yr}^{-1}$ Nova

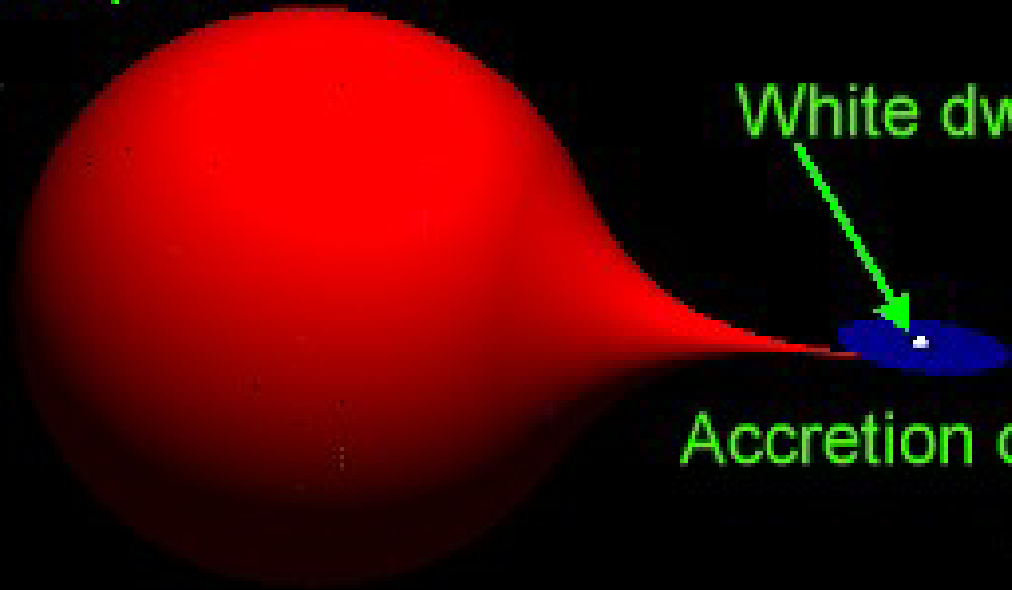
$10^{-9} < \dot{M}_t < 10^{-6} \text{ M}_\odot \text{ yr}^{-1}$ Steady burning or weak flashes. He detonation in some cases

$10^{-6} < \dot{M}_t < \dot{M}_t(\text{Eddington})$ Red giant and common envelope

Companion star

White dwarf

Accretion disk

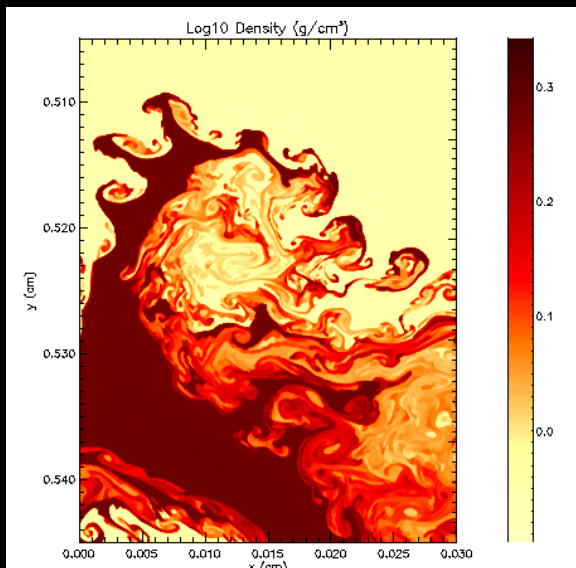


Exploding mechanisms

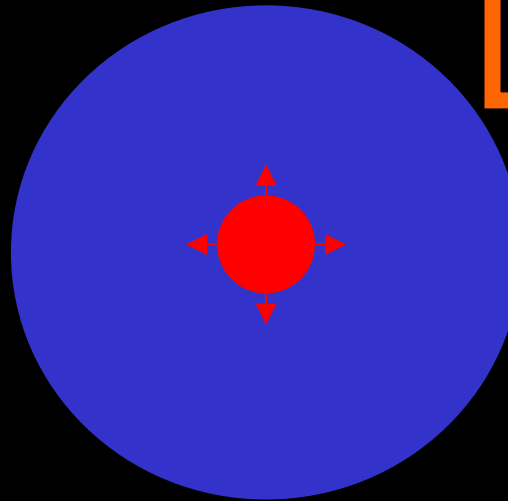
Detonation: supersonic flame

If $\rho > 10^7 \text{ g/cc} \Rightarrow \text{C, O} \rightarrow \text{Ni}$

If $\rho \leq 10^7 \text{ g/cc} \Rightarrow \text{C, O} \rightarrow \text{Si, Ca, S, ...}$



Other possibilities:
Deflagration + detonation
Pulsating delayed detonation



Deflagration: subsonic velocity

laminar flame: $v \sim 0.01 c_s$

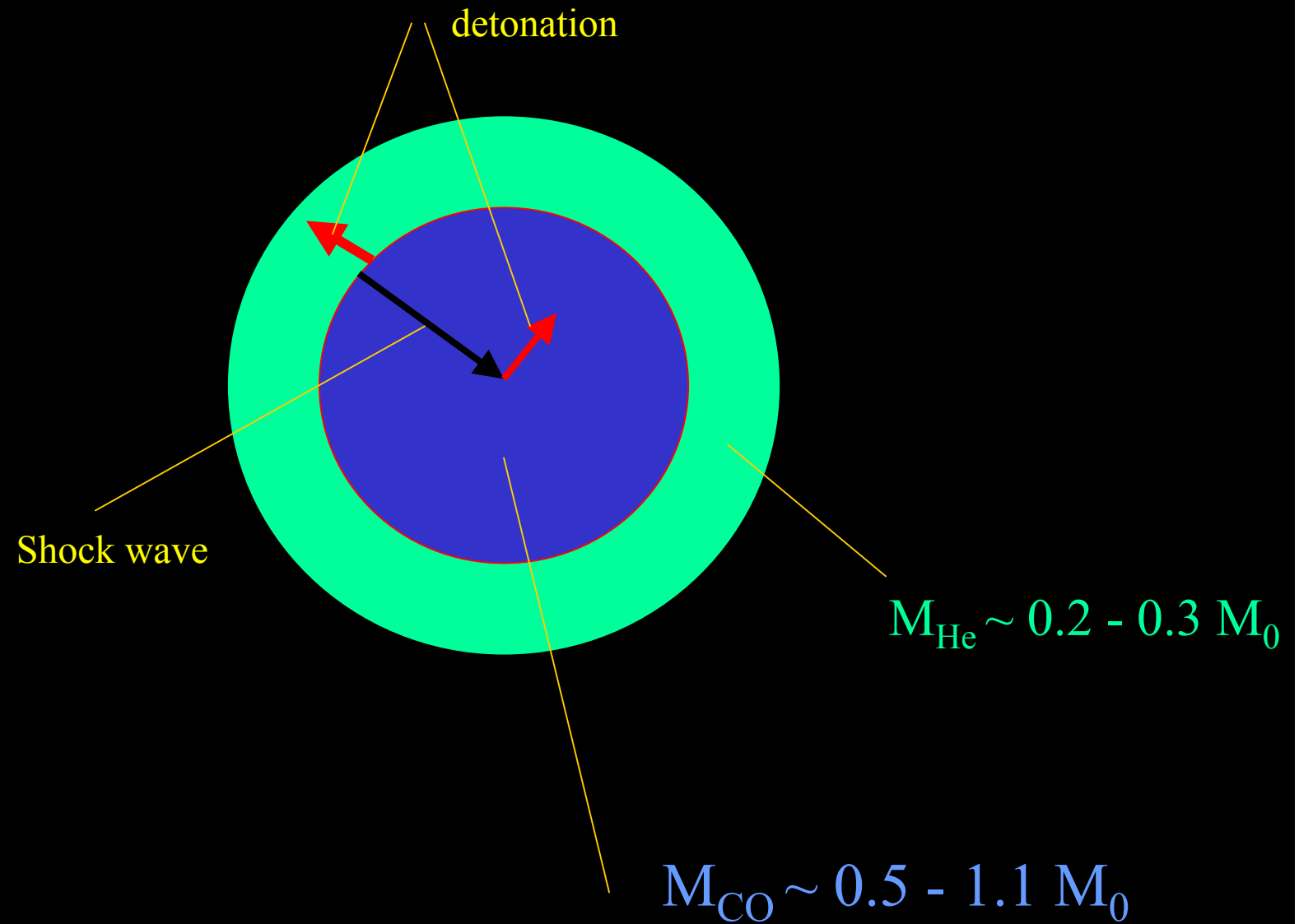
Turbulent flame: $v \sim 0.1 - 0.3 c_s$

The laminar flame becomes turbulent:

- * Rayleigh-Taylor instability
- * Kelvin-Helmholtz

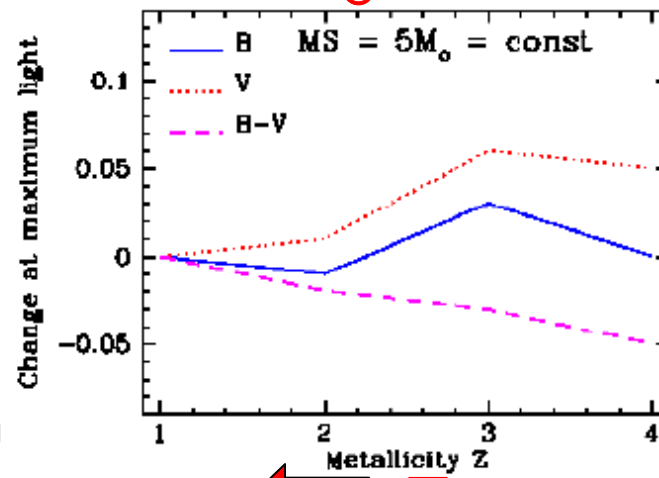
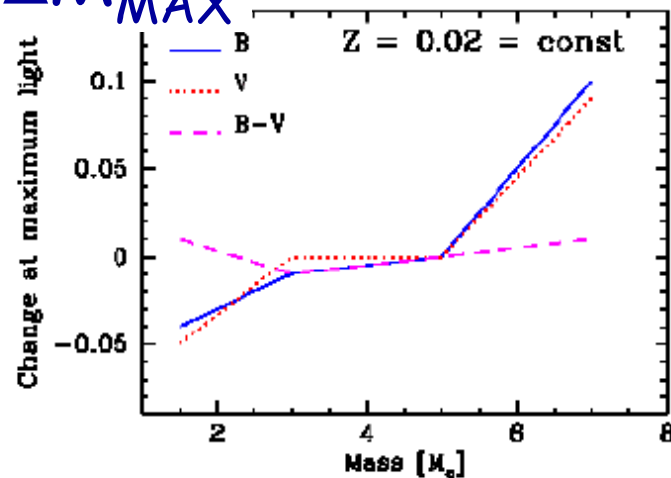
Flame surface increases
effective velocity increases

Exploding mechanisms: Off center ignition



ΔM_{MAX}

Reference: $5 M_{\odot}$ $Z=0.02$



$M_{MS} \rightarrow$

$Z: 0.02 \quad 10^{-3} \quad 10^{-4} \quad 10^{-10}$

Back in time

$Z \downarrow$

$t_{evol} \downarrow \quad M_{MS} \uparrow$

$M_{MS} \uparrow$

$C/O \leq 22\% \downarrow$

$Z \downarrow$

$C/O \leq 9\%$

$L \downarrow \leq 0.15 \text{ mag}$

$V_{ph} \downarrow 2000 \text{ km/s}$

$t_{Rise} \uparrow 1.7 \text{ days}$

$L \sim \leq 0.05 \text{ mag}$

but Umeda et al. 1999

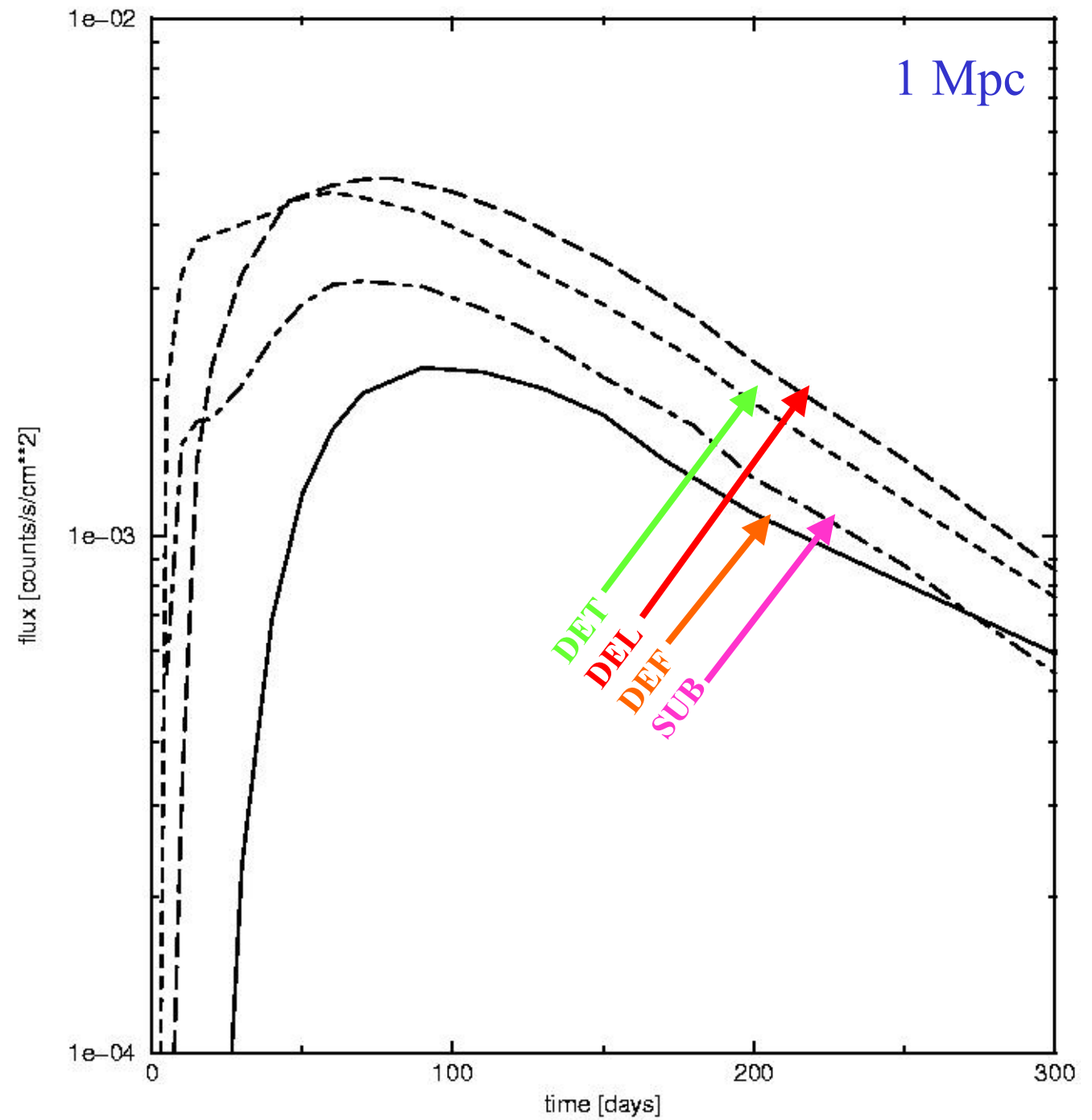
$B, U, UV \rightarrow B-V \downarrow$

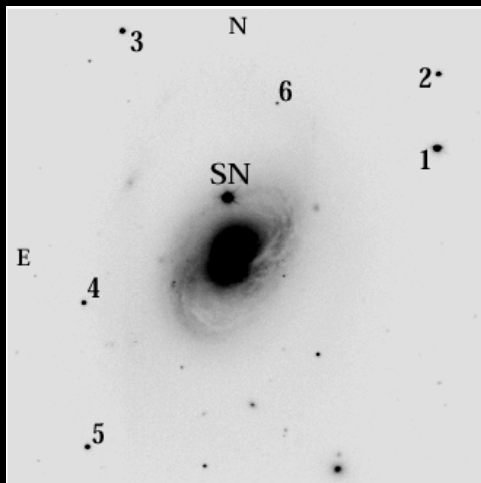
Dark Energy ?? $\sim 0.1 - 0.05 \text{ mag}$

Light curves

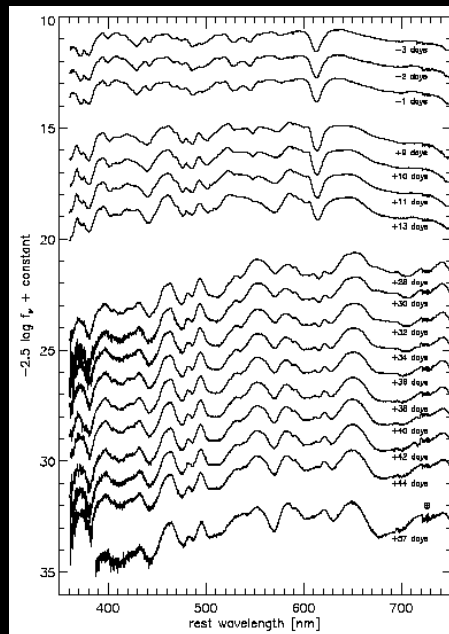
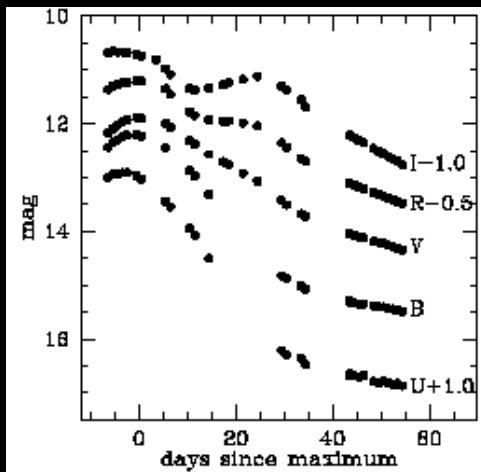
847 keV

^{56}Co



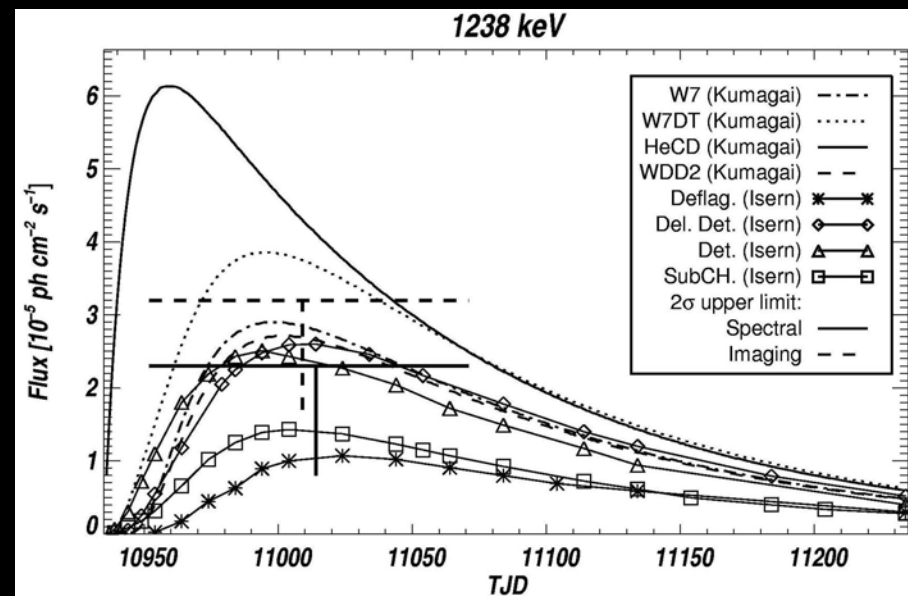
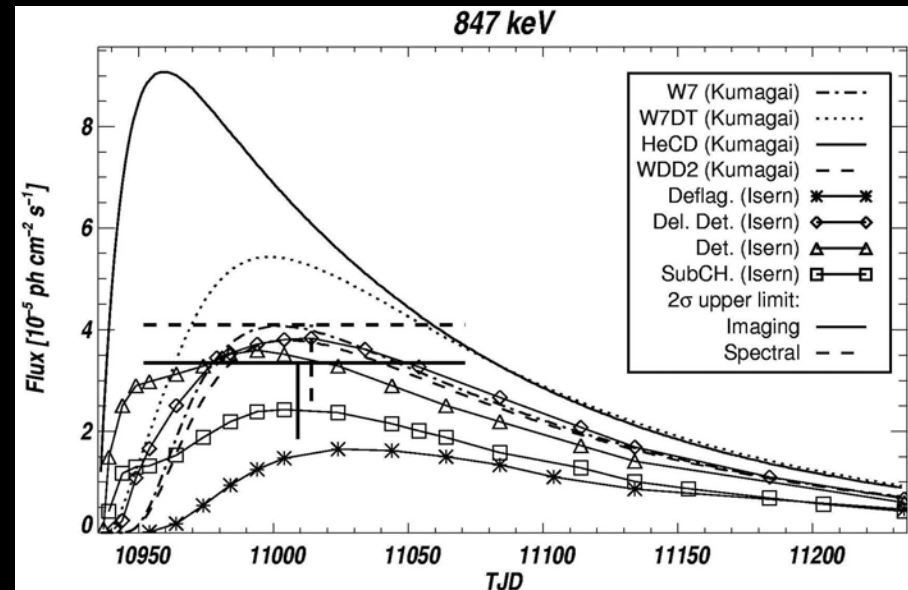


M96
d = 8- 12 Mpc



(From Diehl'02)

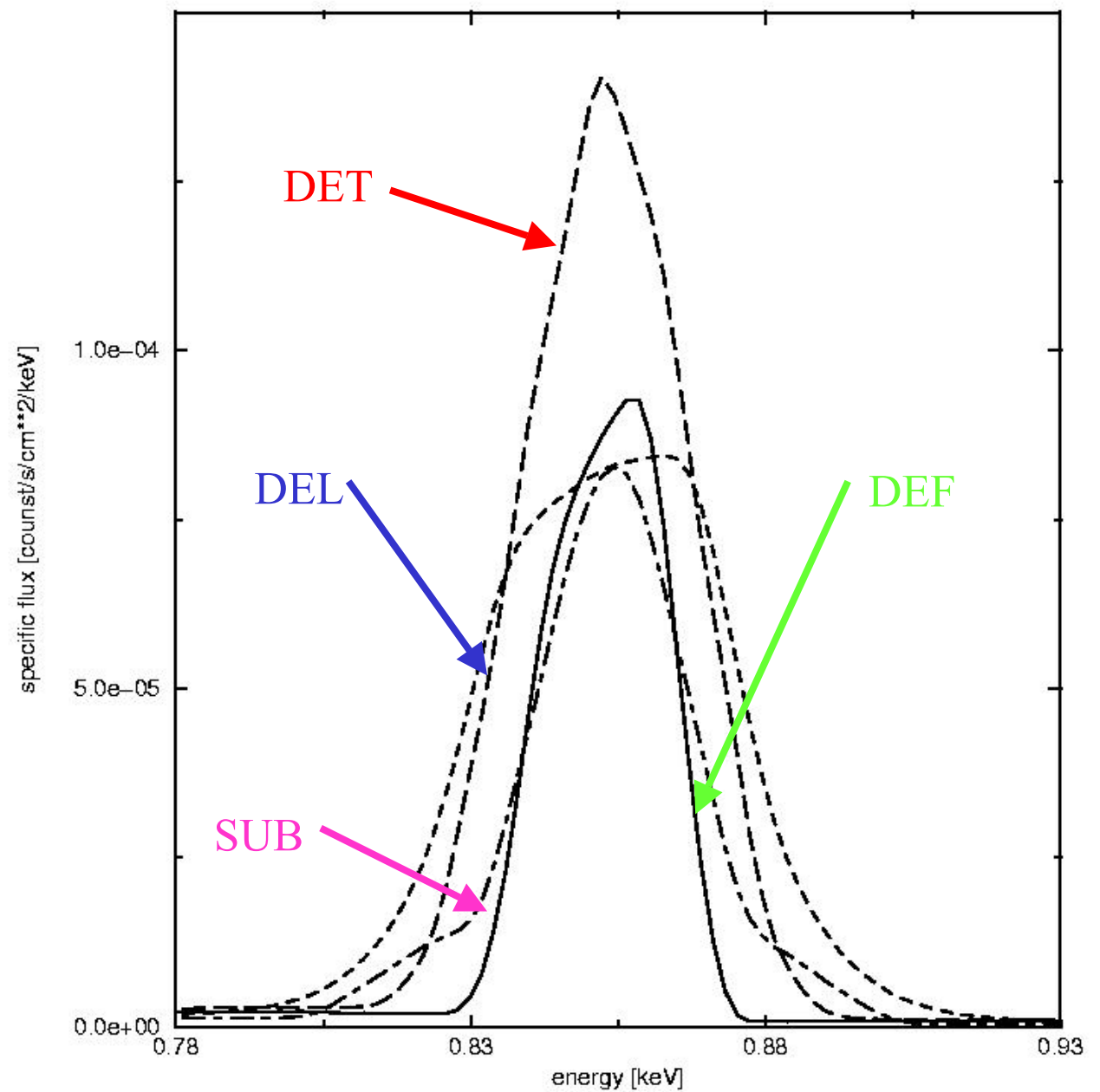
SN 1998bu



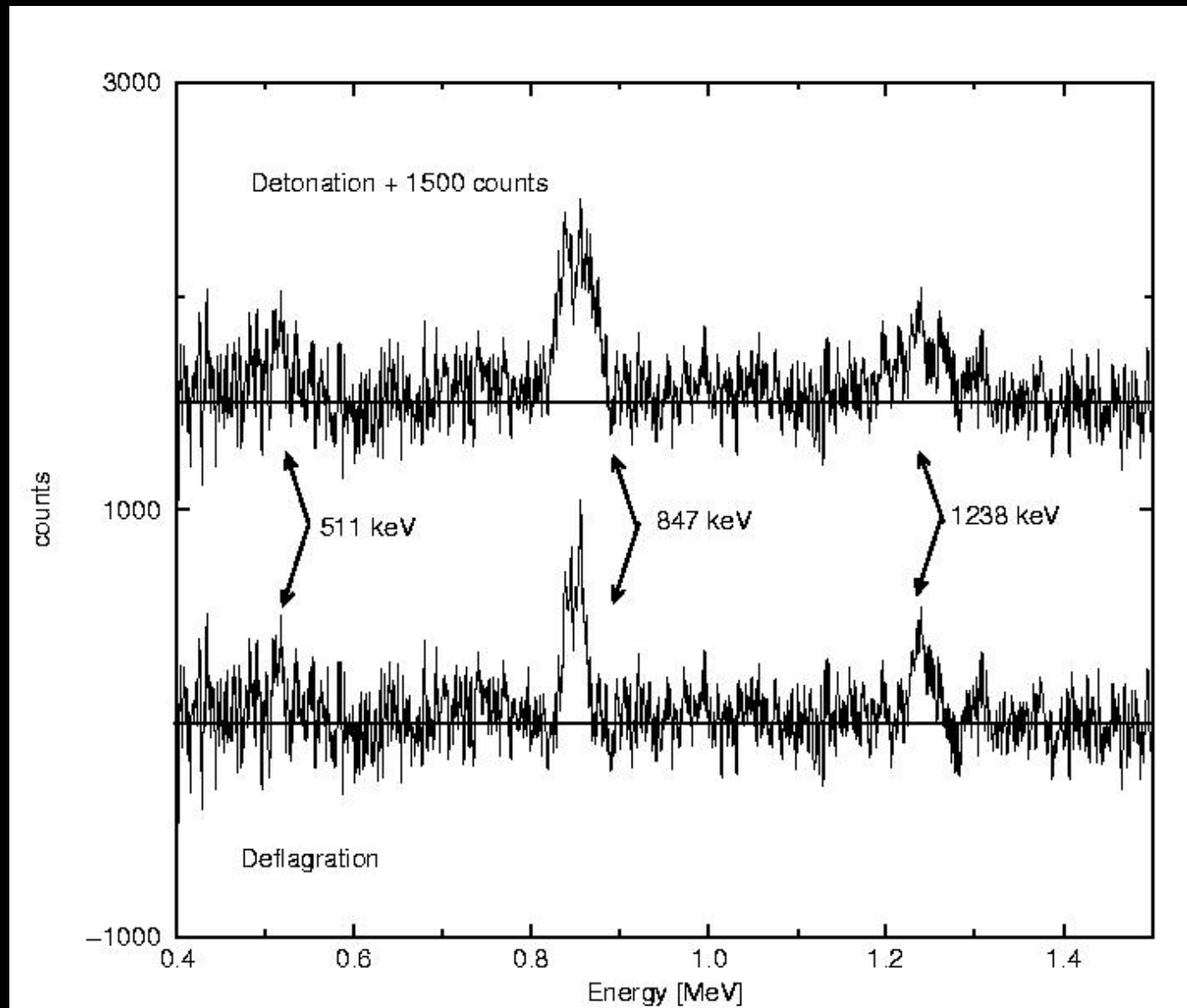
	Flux (phot/cm ² /s)
847 keV	<3.1-4.1 x 10 ⁻⁵
1238 keV	<2.3 – 3.1 x 10 ⁻⁵

Line profiles for the 847 keV line

$D = 1 \text{ Mpc}$
 $t = 120 \text{ d}$



Simulated observational spectra



$D = 5 \text{ Mpc}$
 $t_{\text{int}} = 10^6 \text{ s}$

SPI/INTEGRAL

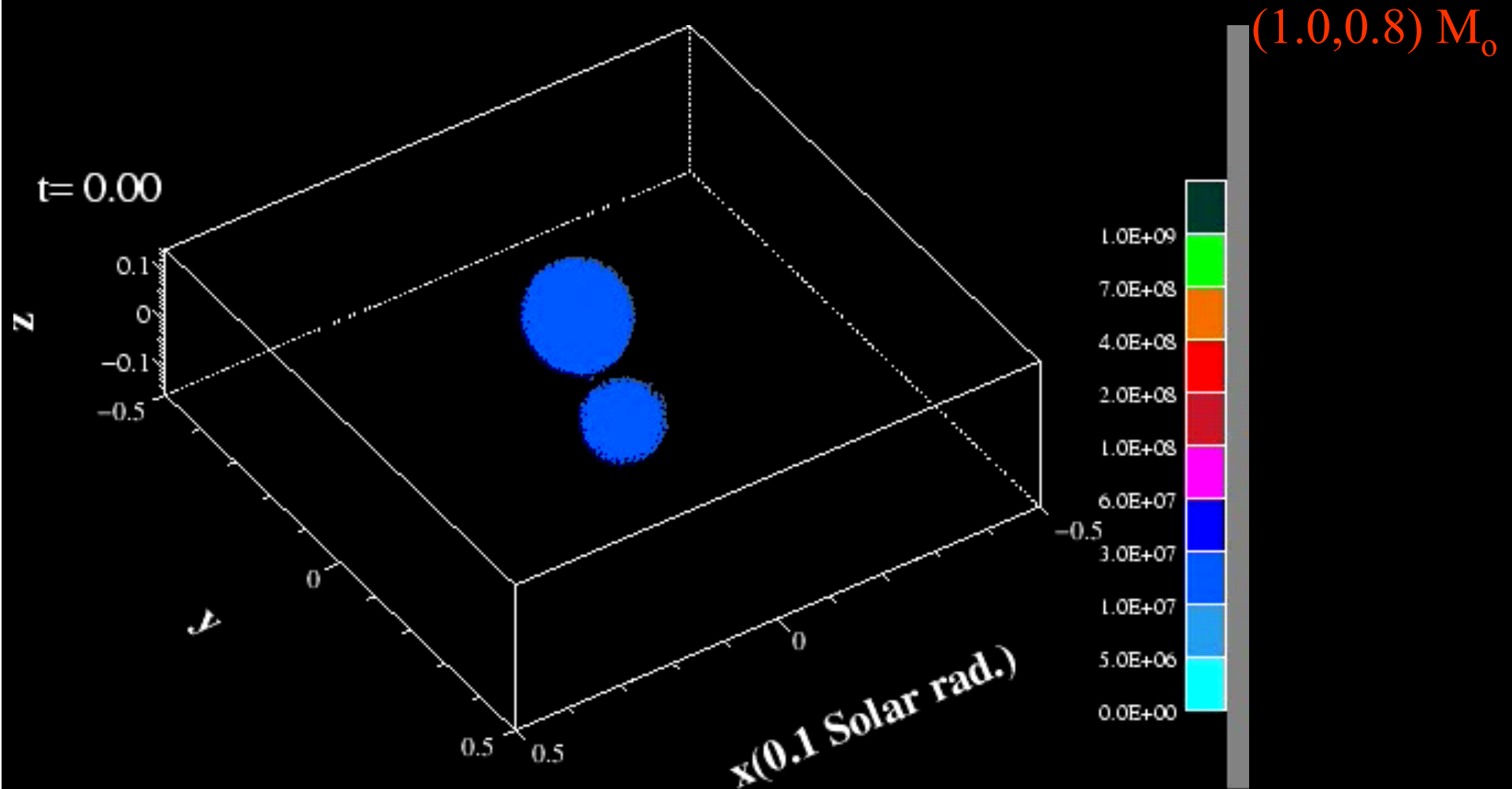
- **INTEGRAL** can provide useful information for
- **SN Ia**, provided they occur close enough, on the
- basis of:
 - Line light curves
 - Properties of the continuum
 - Line profiles
- Because of the poor understanding of the flame
- properties we have to use parametrized values.
- In this case there are ambiguities in the
- information provided by the gamma-rays alone.
- Independent information is necessary



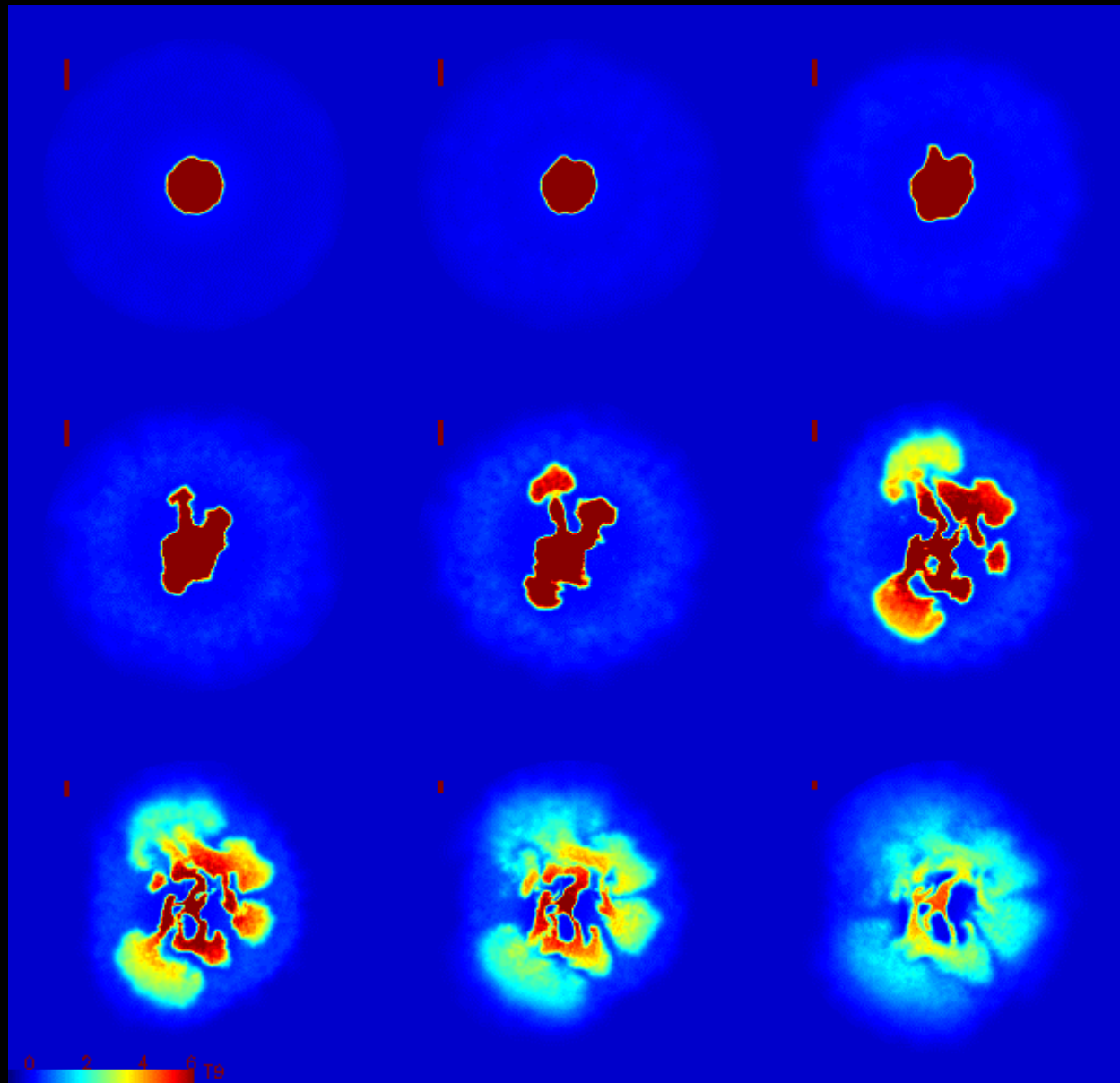
Departures from spherical symmetry?

- The physics of the flames indicates they are unstable and departures from spherical symmetry easily appear
- The scenarios in which the explosion occurs are not symmetric
- Nevertheless, observations suggest that these departures are small:
 - The homogeneity of the light curves & spectra indicates photospheric perturbations $< 10\%$
 - Standard SNIa show small polarizations (Wang et al 2001)
 - But subluminal display polarizations $\sim 0.7\%$ (Howell et al 2001)

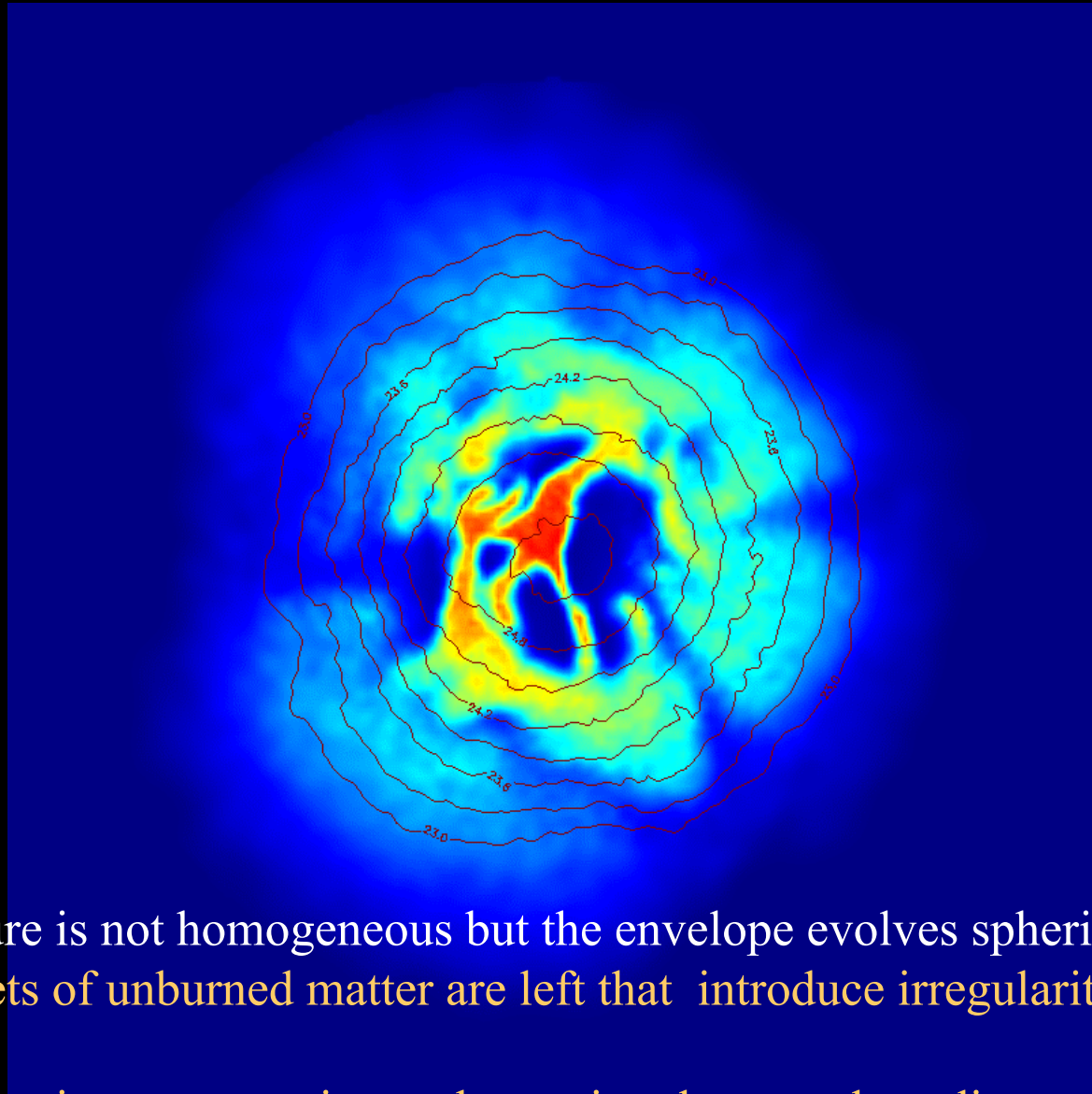
- Since SNIa occur in binary systems, large scale departures from sphericity can occur
- Double degenerate systems



Central deflagration: T; time = 0 – 1.55 s; (Bravo, Garcia-Senz, Serichol)
= 400 km



T & P at the end of the deflagration phase ($t=1.55$ s)



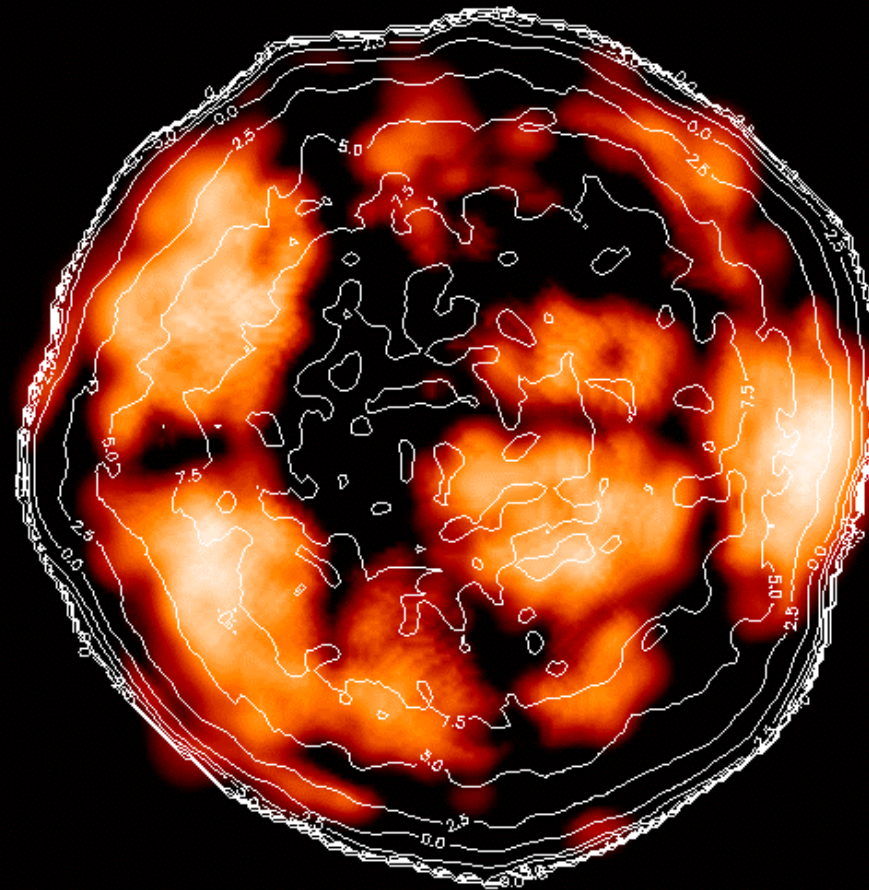
The front structure is not homogeneous but the envelope evolves spherically.


Large pockets of unburned matter are left that introduce irregularities in the line profiles

If the deflagration turns out into a detonation these pockets disappear

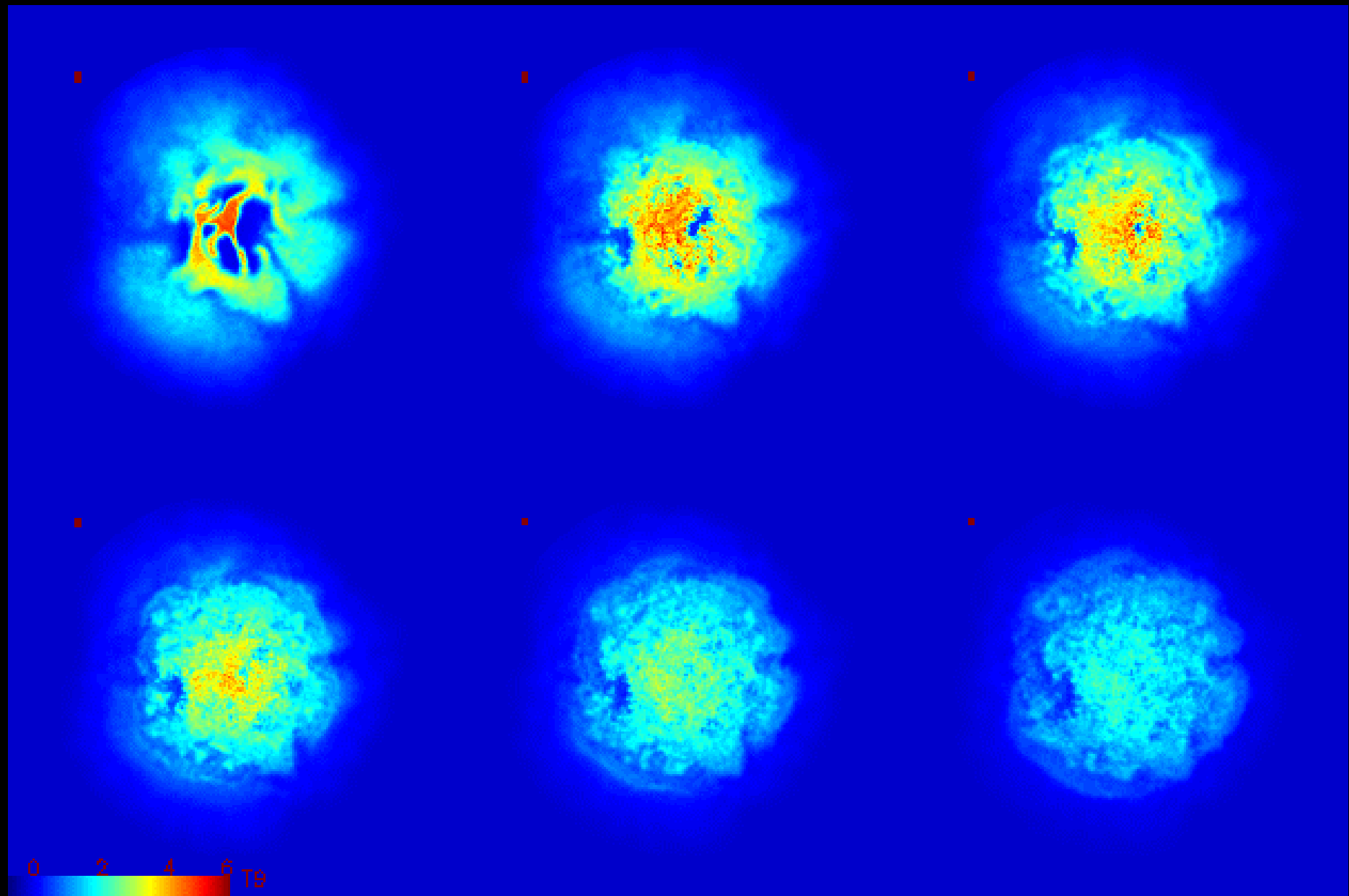
- The problem of the ^{56}Ni clumps (García-Senz & Bravo 2004):

B30U @ 15 days



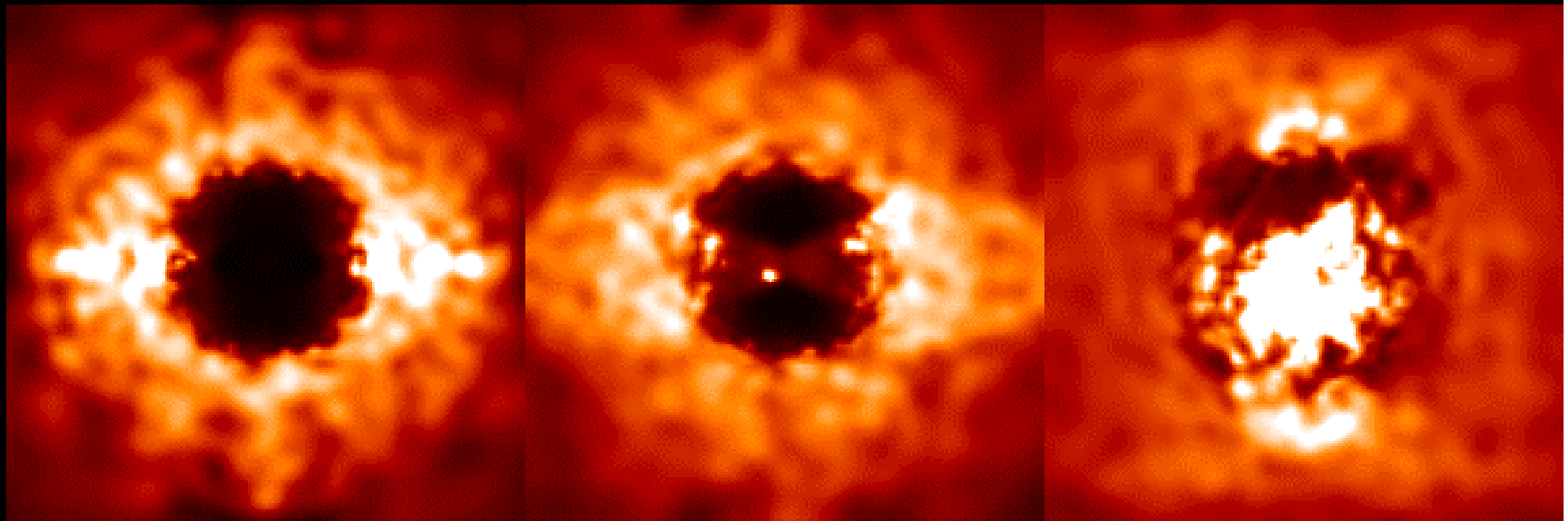
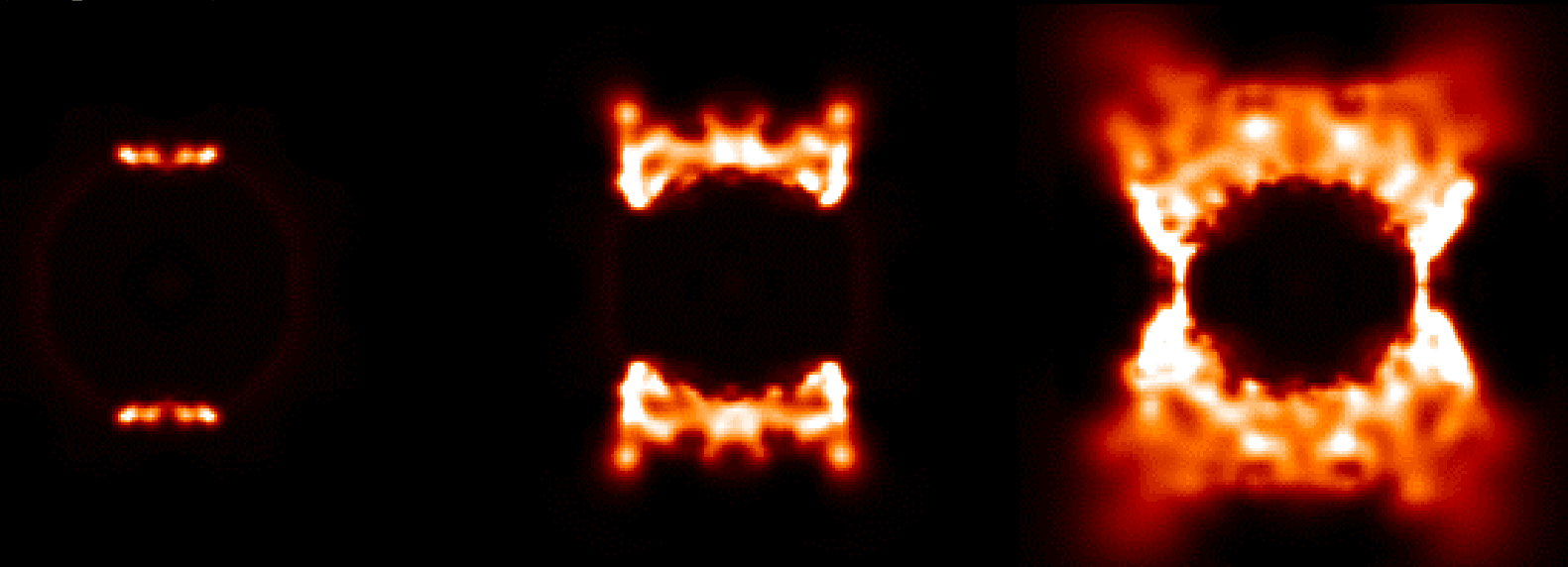
 log ^{56}Ni column-density ($-1.5: +0.5 \text{ g cm}^{-2}$)

The detonation starts: $t = 1.55 - 2.06$ s



Off center detonations (E. Bravo et al IEEC/UPC)

(temperature)

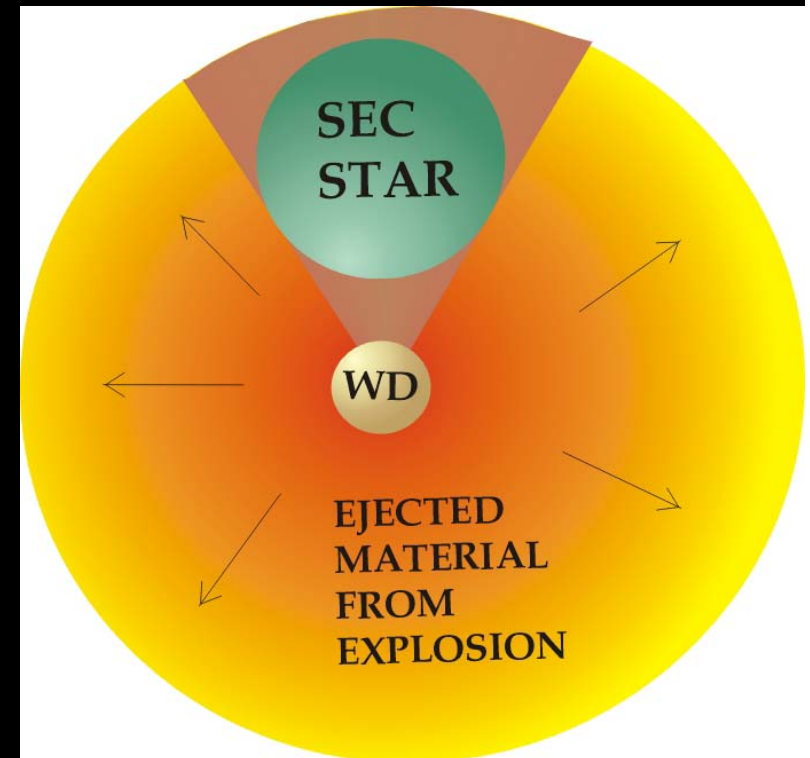


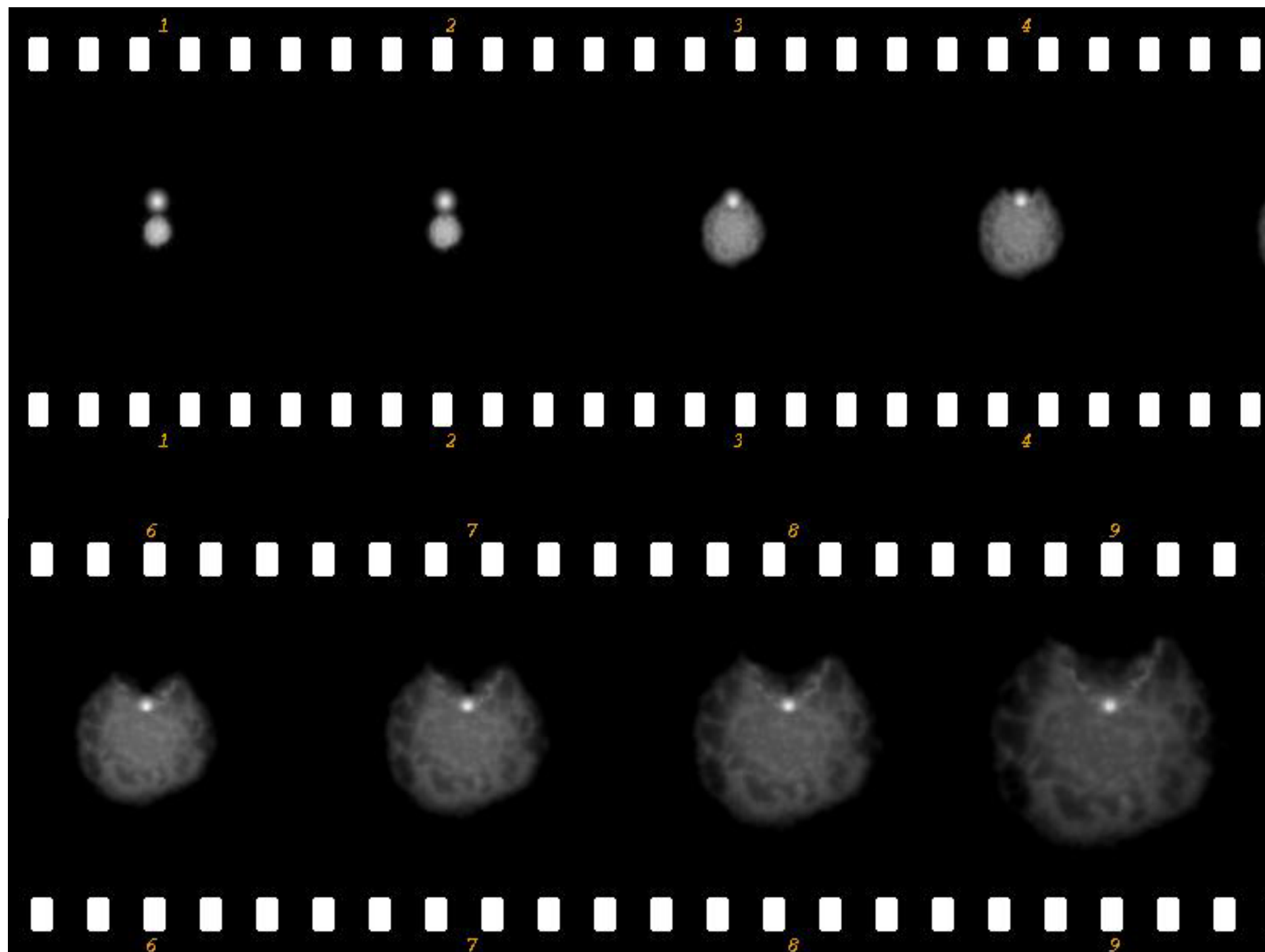
Single degenerate scenario

Companion star

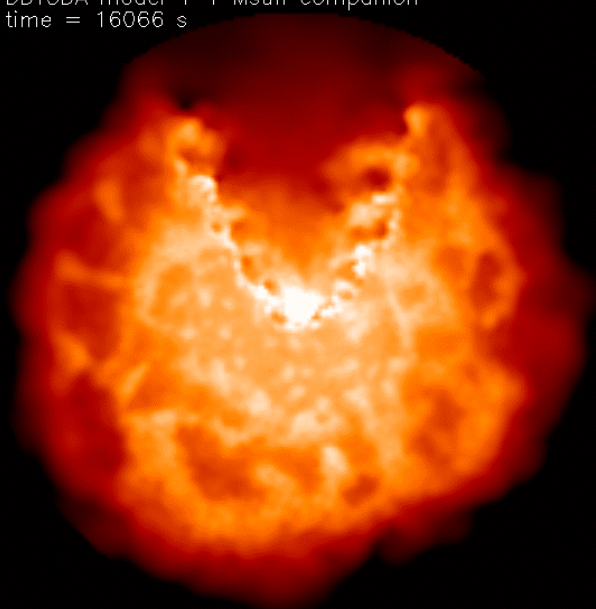
White dwarf

Accretion disk



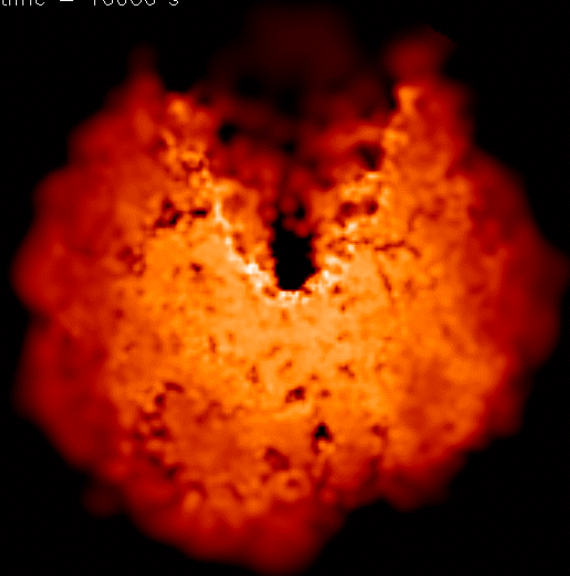


DDT3DA model + 1 Msun companion
time = 16066 s



$\log \rho$ (-10:-6)

DDT3DA model + 1 Msun companion
time = 16066 s

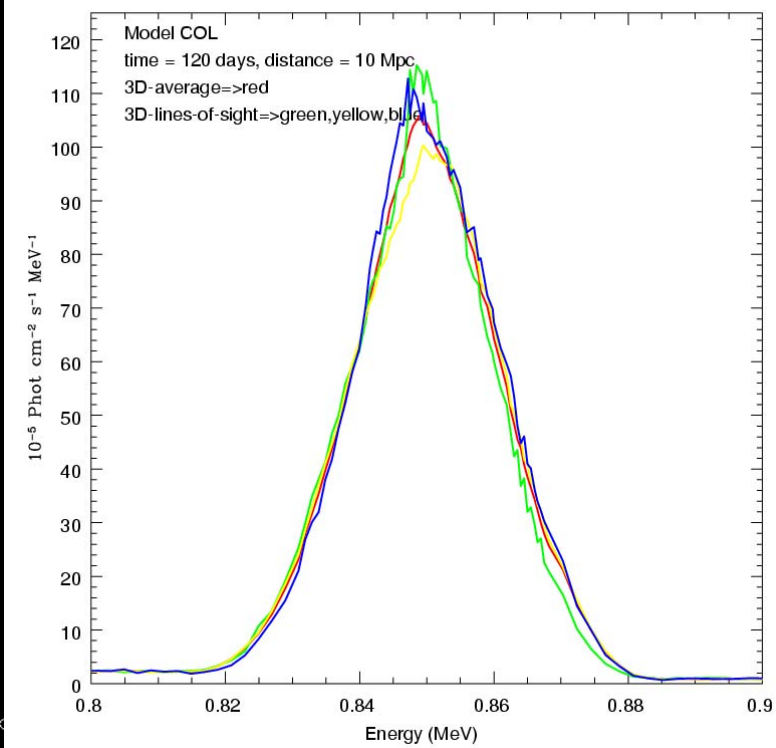


$\log \rho \cdot X(^{56}\text{Ni})$ (-10:-6)

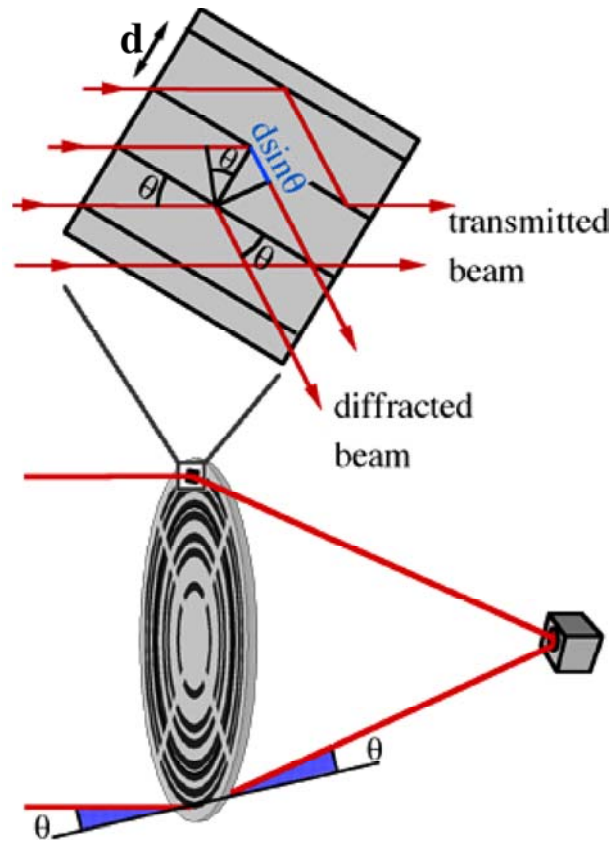
DDT3DA model + 1 Msun companion
time = 16066 s



$\log \rho \cdot X(\text{H})$ (-10:-6)



Focusing Gamma-Rays - how ?



$$\lambda(511 \text{ keV}) = 2.42632 \cdot 10^{-2} \text{ \AA}$$

Bragg condition

$$2d \sin \theta = n \lambda$$

$$d[220] = 2.0004 \text{ \AA}$$

$$\arcsin(\lambda/2d) = 0.347^\circ$$

Laue-type Gamma-ray lens

$$2\theta = 0.695^\circ$$

$$\text{ex. radius [220]} = 10.1 \text{ cm}$$

$$\Rightarrow \text{focal length} = 8.2 \text{ m}$$

narrow band Laue lens :

broad band Laue lens :

higher orders at larger radii (CLAIRE)

most efficient order at all radii (MAX)

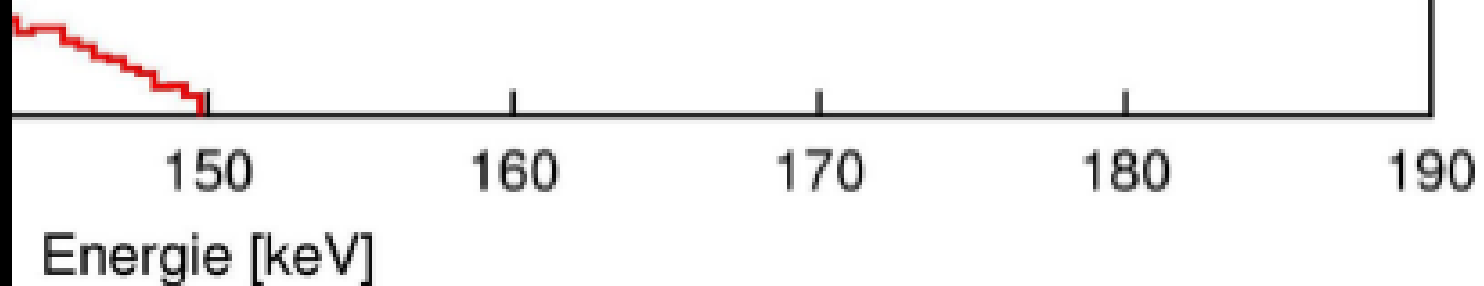
a gamma-ray lens for nuclear astrophysics

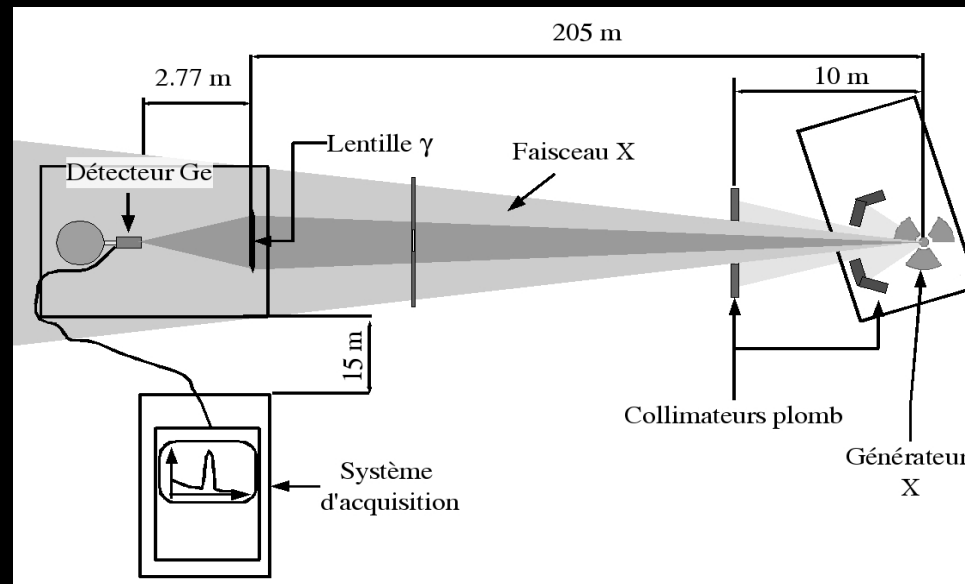


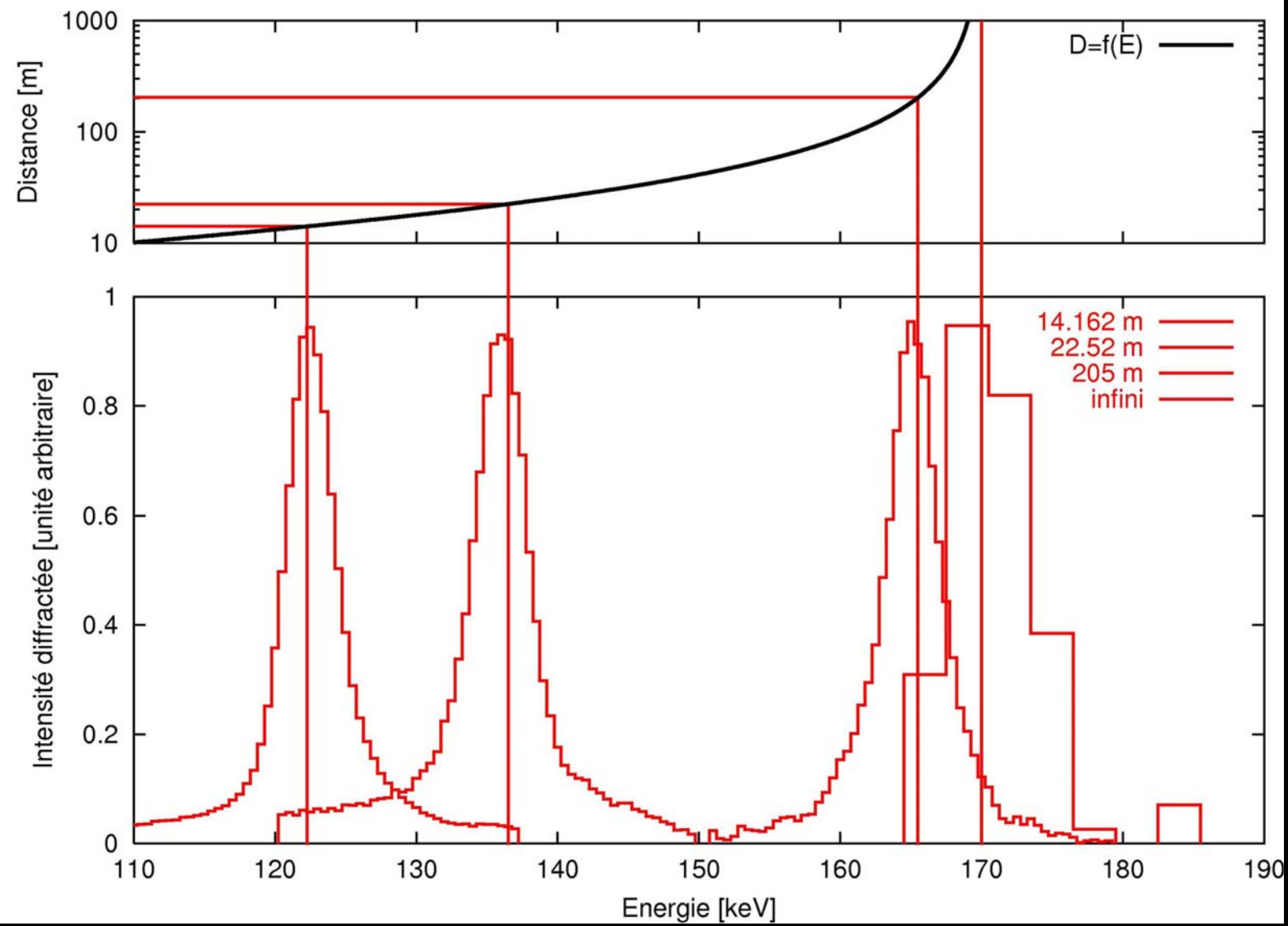
14.162 m —
22.52 m —



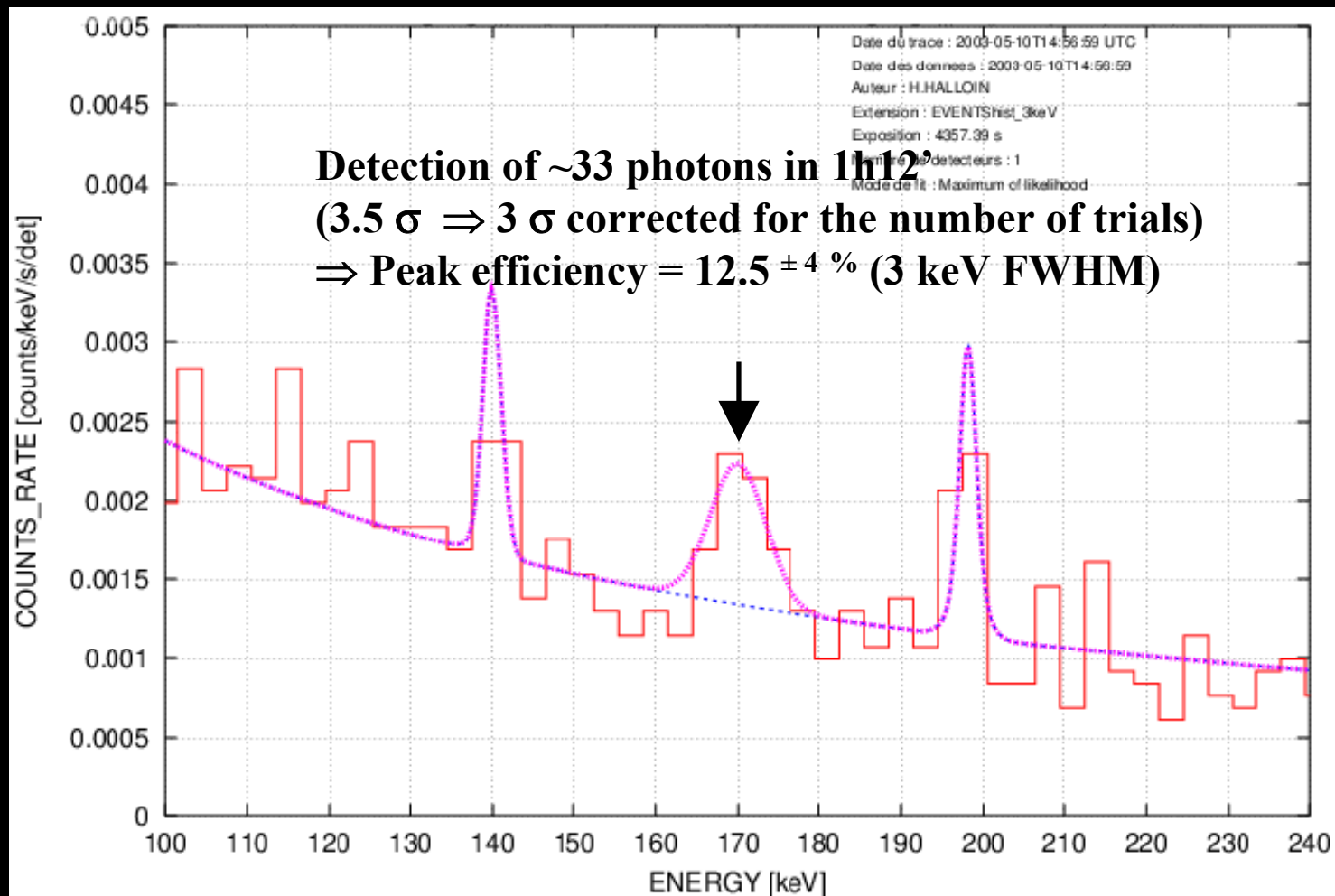
tuning and test line at CESR Toulouse











MAX/

10^{-7} /phot/cm²/s
Ge ring 511 keV
Cu ring 850 keV

MAX

